

# EOS – A Software for Flavour Physics Phenomenology

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*For the EOS authors*



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## EOS:

- **Main use cases:**

- 1) **infer theory parameters** from an extendable database of experimental and theoretical likelihoods;
- 2) produce **publication-quality theory predictions** for flavour observables;
- 3) produce **high-quality Monte Carlo samples** of flavour processes, e.g. for sensitivity studies.

- **C++** back-end, **python** front-end (Jupyter Notebook)

- Current version: **EOS v1.0.5**

- Developed since ~1000BC by **over 20 contributors**



<https://eos.github.io/>

# The EOS Software



How does EOS compare to other software?



<https://flav-io.github.io/>

<http://superiso.in2p3.fr/>

FlavBit: 1705.07933

(among others...)

EOS' "unique selling point":

- Simultaneous **inference of hadronic and BSM parameters**
- **Modularity of hadronic matrix elements** (models, parametrizations...)
- **Production of pseudo-events** for use in sensitivity studies and in preparation for experimental measurements
- Prediction of **hadronic matrix elements** from QCD sum rules



# 1. Brief overview



- **Installation is very simple** on Linux:  

```
pip3 install --user eoshep
```
- Then open a **Jupyter Notebook** and just run  

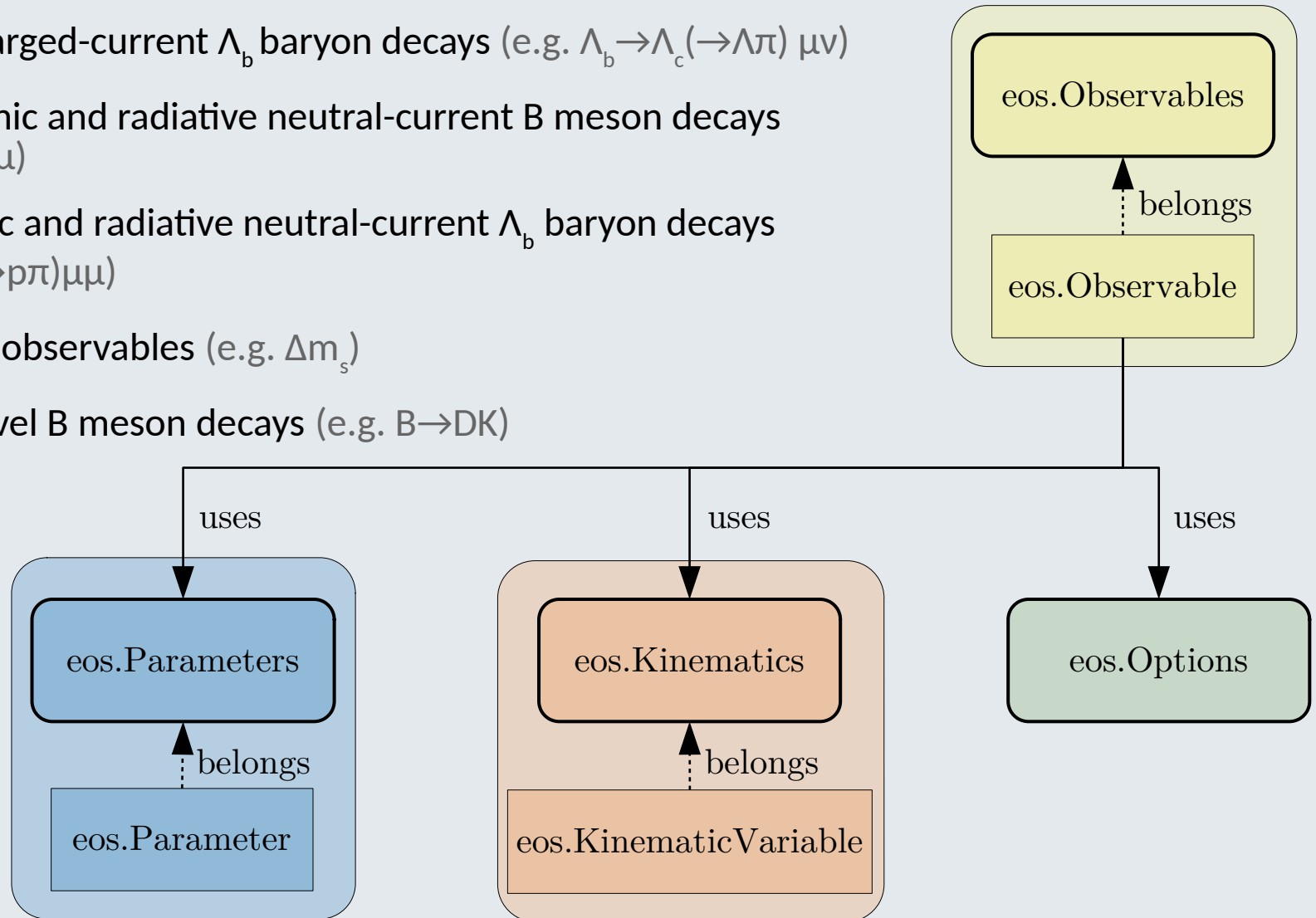
```
import eos
```
- For other platforms and **further details**:  
<https://eos.github.io/doc/installation.html>
- **Support** can be found here:  
<https://discord.com/invite/hyPu7f7K6W>

# Observables and versatility



~1000 (pseudo-)observables covering:

- (semi)leptonic charged-current B meson decays (e.g.  $B \rightarrow D^* \tau \nu$ )
- semileptonic charged-current  $\Lambda_b$  baryon decays (e.g.  $\Lambda_b \rightarrow \Lambda_c (\rightarrow \Lambda \pi) \mu \nu$ )
- rare (semi)leptonic and radiative neutral-current B meson decays (e.g.  $B \rightarrow K^* \mu \mu$ )
- rare semileptonic and radiative neutral-current  $\Lambda_b$  baryon decays (e.g.  $\Lambda_b \rightarrow \Lambda (\rightarrow p \pi) \mu \mu$ )
- B-meson mixing observables (e.g.  $\Delta m_s$ )
- hadronic tree-level B meson decays (e.g.  $B \rightarrow DK$ )



# Predictions and Uncertainties



```
In [3]: eos.Observable.make('B->Dlnu::BR',
                             eos.Parameters.Defaults(),
                             eos.Kinematics(q2_min=0.02, q2_max=11.60),
                             eos.Options(l = 'mu')
                             )
```

executed in 69ms, finished 18:23:54 2021-11-20

```
Out[3]: B->Dlnu:BR (eos.Observable)
kinematics  q2_min  0.02
            q2_max  11.6
            l       1/2
options     U       c
            l       mu
current value 0.02417
```

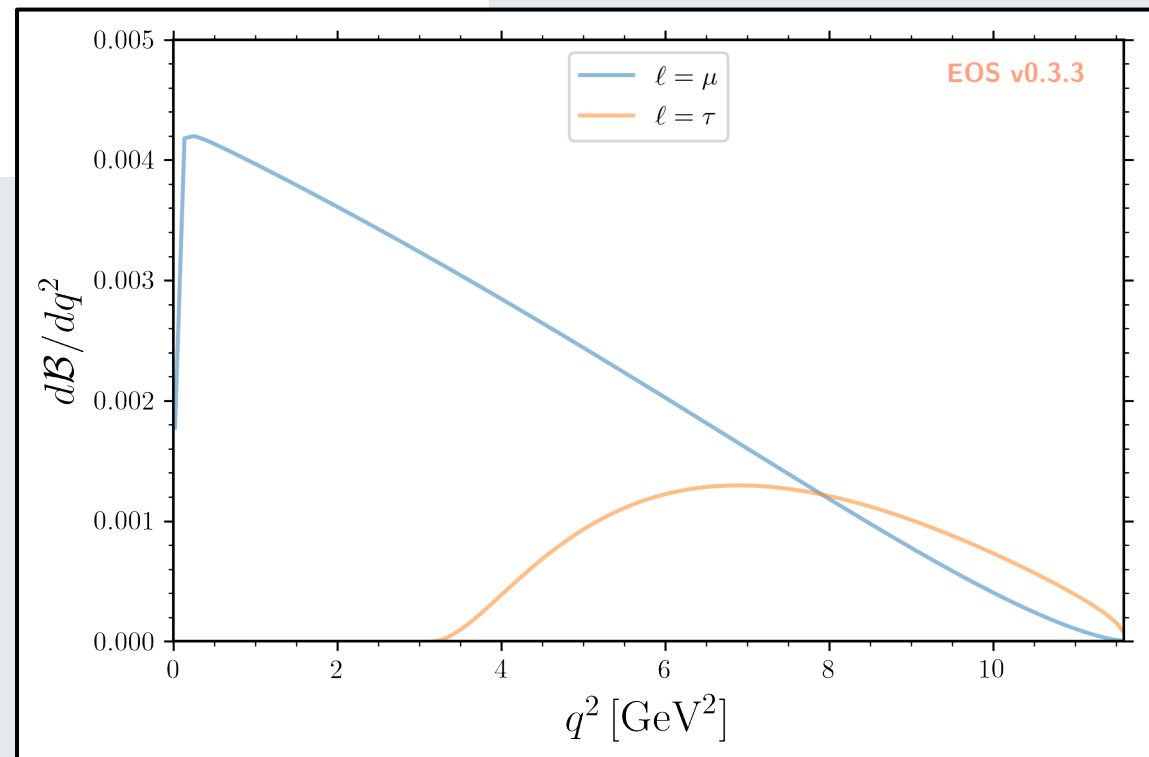
## Fast evaluation of observables:

- Multi-threading
- Observable cache

Versatile plotting  
framework  
based on



[EOS Repo: Tutorial 1](#)



# Predictions and Uncertainties

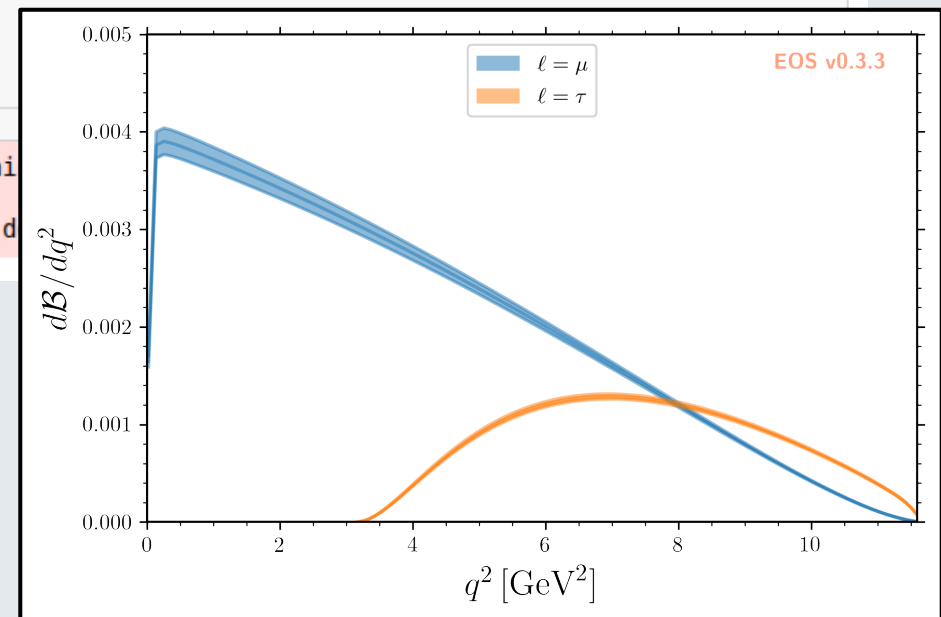


Theory **uncertainties** are estimated using **Monte Carlo techniques**, specifically importance sampling technique using **pypmc** (<https://pypmc.github.io/>)

```
In [7]: analysis_args = {
  'priors': [
    { 'parameter': 'B->D::alpha^f+_0@BSZ2015', 'min': 0.0, 'max': 1.0, 'type': 'uniform' },
    { 'parameter': 'B->D::alpha^f+_1@BSZ2015', 'min': -5.0, 'max': +5.0, 'type': 'uniform' },
    { 'parameter': 'B->D::alpha^f+_2@BSZ2015', 'min': -5.0, 'max': +5.0, 'type': 'uniform' },
    { 'parameter': 'B->D::alpha^f_0@BSZ2015', 'min': -5.0, 'max': +5.0, 'type': 'uniform' },
    { 'parameter': 'B->D::alpha^f_2@BSZ2015', 'min': -5.0, 'max': +5.0, 'type': 'uniform' }
  ],
  'likelihood': [
    'B->D::f_++f_0@HPQCD:2015A',
    'B->D::f_++f_0@FNAL+MILC:2015B'
  ]
}
analysis = eos.Analysis(**analysis_args)
```

executed in 725ms, finished 19:18:37 2021-11-20

INFO:EOS:Creating analysis with 5 priors, 2 EOS-wide constraints and 0 fixed parameters.  
INFO:EOS:likelihood probably depends on 3 parameter(s) that d



Markov Chains

EOS Repo: Tutorial 1



# Parameter Inference

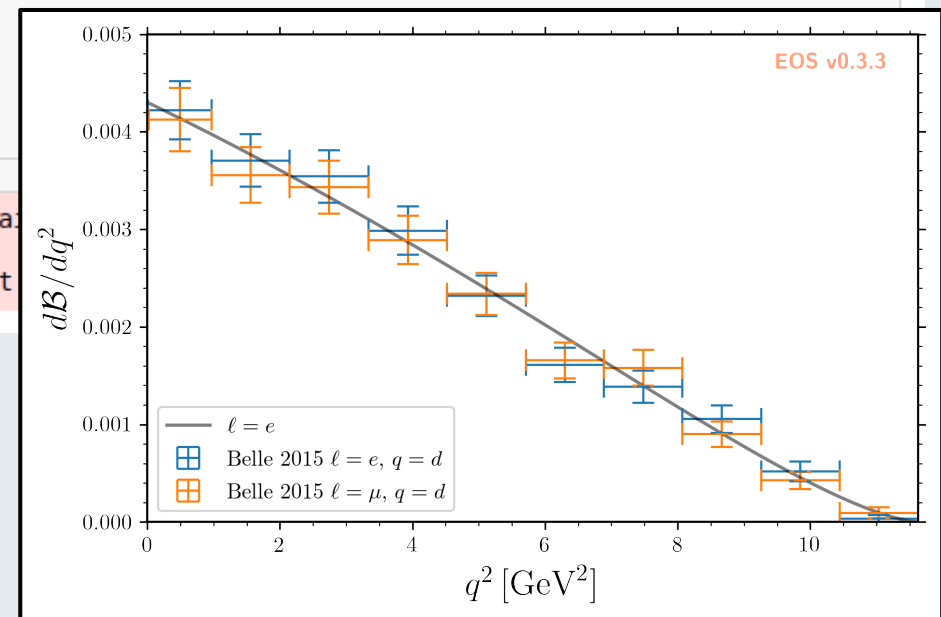


Parameters can be inferred from a **database of experimental or theoretical constraints**

```
In [5]: analysis_args = {
'global_options': { 'form-factors': 'BSZ2015', 'model': 'CKM' },
'priors': [
{ 'parameter': 'CKM::abs(V_cb)', 'min': 38e-3, 'max': 45e-3, 'type': 'uniform'},
{ 'parameter': 'B->D::alpha^f+_0@BSZ2015', 'min': 0.0, 'max': 1.0, 'type': 'uniform'},
{ 'parameter': 'B->D::alpha^f+_1@BSZ2015', 'min': -4.0, 'max': -1.0, 'type': 'uniform'},
{ 'parameter': 'B->D::alpha^f+_2@BSZ2015', 'min': +4.0, 'max': +6.0, 'type': 'uniform'},
{ 'parameter': 'B->D::alpha^f0_1@BSZ2015', 'min': -1.0, 'max': +2.0, 'type': 'uniform'},
{ 'parameter': 'B->D::alpha^f0_2@BSZ2015', 'min': -2.0, 'max': 0.0, 'type': 'uniform'}
],
'likelihood': [
'B->D::f_++f_0@HPQCD:2015A',
'B->D::f_++f_0@FNAL+MILC:2015B',
'B^0->D^+e^-nu::BRs@Belle:2015A',
'B^0->D^+mu^-nu::BRs@Belle:2015A'
]
}
analysis = eos.Analysis(**analysis_args)
analysis.parameters['CKM::abs(V_cb)'].set(42.0e-3)
```

executed in 310ms, finished 11:23:40 2021-11-21

INFO:EOS:Creating analysis with 6 priors, 4 EOS-wide constraints and 0 fixed parameters.  
likelihood probably depends on 48 parameter(s) that

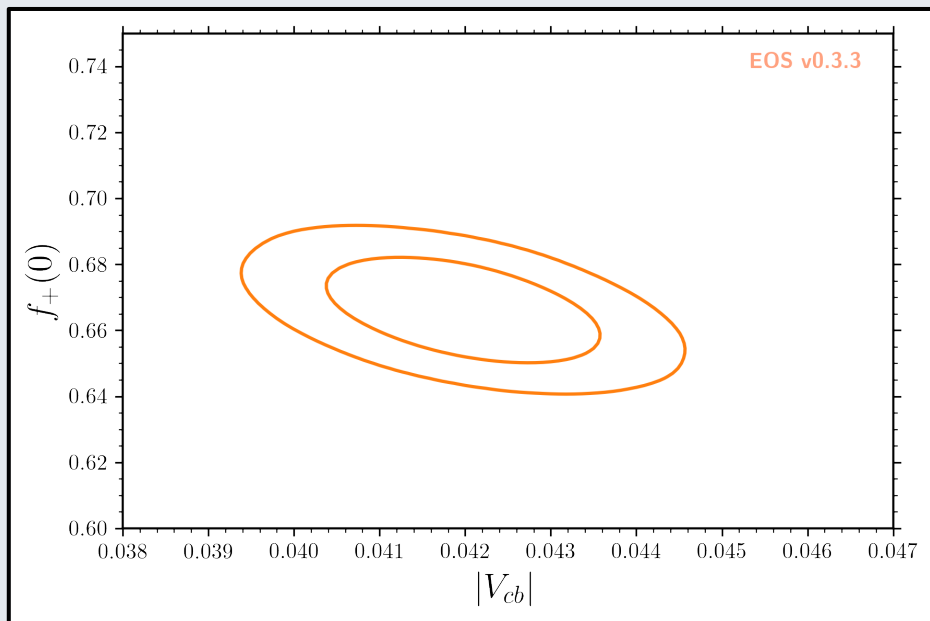


SciPy  
optimization



EOS Repo: Tutorial 2

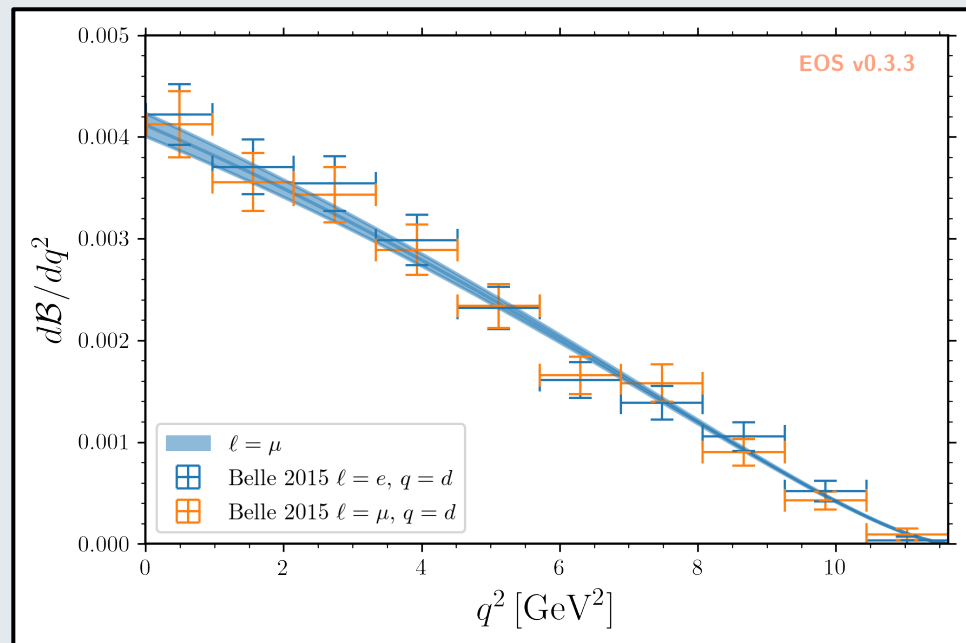
# Parameter Inference



Output of the sampling are **genuine python objects**

$$|V_{cb}| = 0.0420 \pm 0.0009$$

**Publication-quality plots**



EOS Repo: Tutorial 2

# Simulation of Pseudo Events



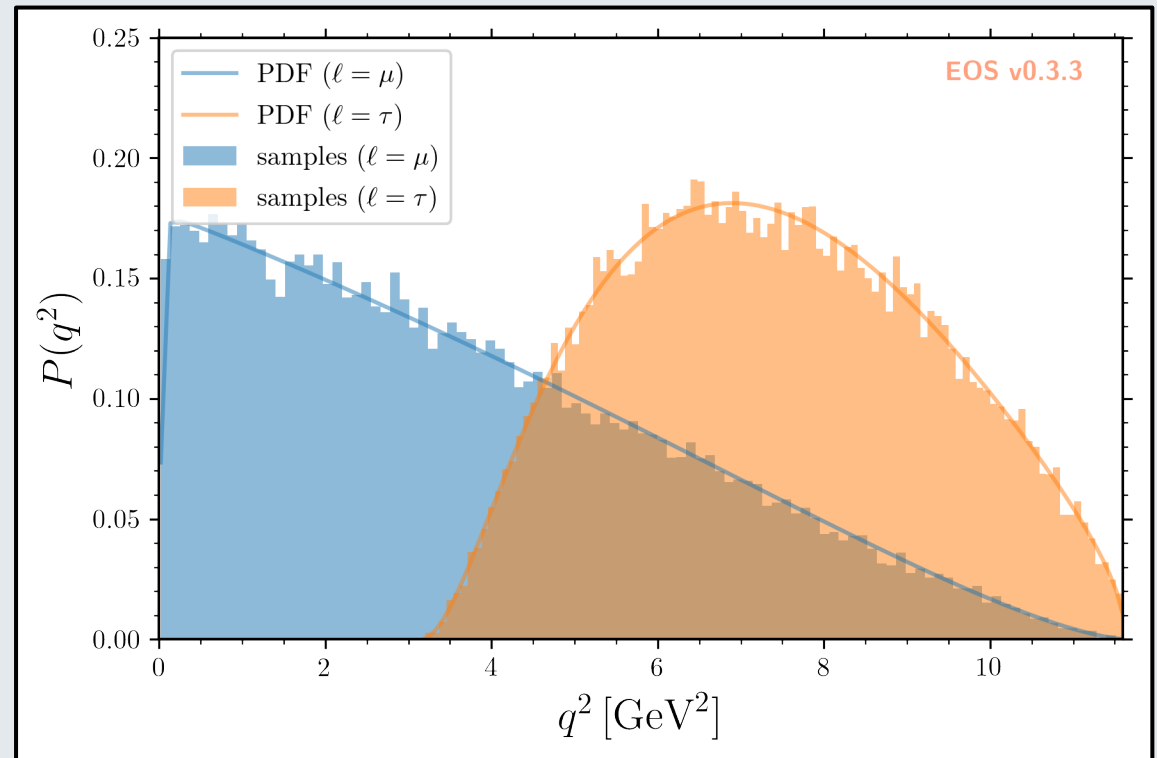
Event simulation from a set of **built-in PDFs** using Markov chain Monte Carlo techniques.

→ **Sensitivity studies**

**Excellent matching**  
between produced  
samples and built-in PDFs



[EOS Repo: Tutorial 3](#)





## 2. Applications

See <https://eos.github.io/publications/>

From *Improved Theory Predictions and Global Analysis of Exclusive  $b \rightarrow s \mu + \mu^-$  Processes* (2206.03797)

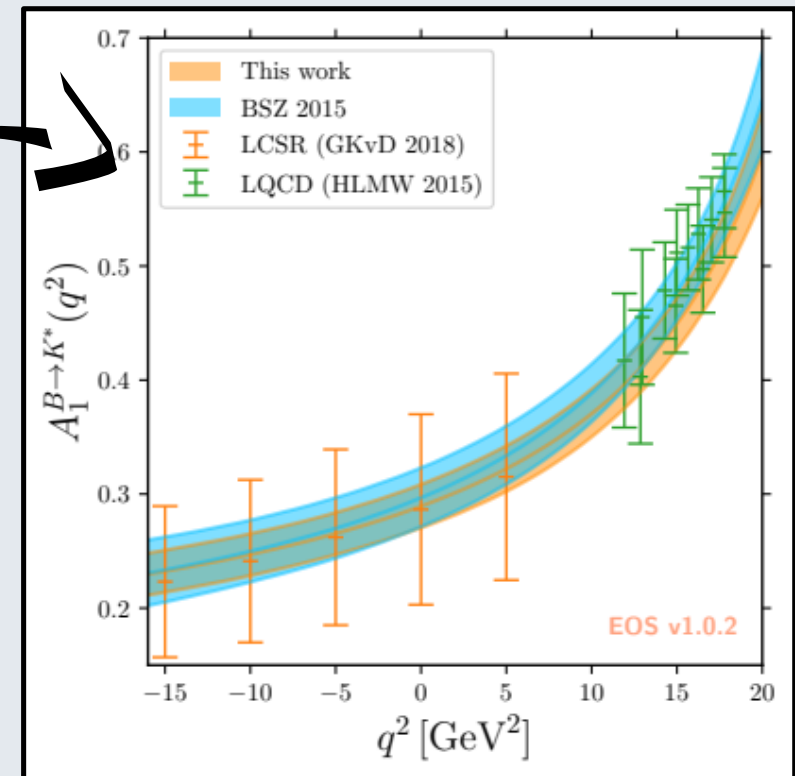
[N. Gubernari, MR, D. van Dyk, J. Virto]

- 1) Fit **local** form-factors of  $B \rightarrow K^{(*)}$ ,  
 $B_s \rightarrow \varphi$  (46 parameters)

GKvD:2018A

## Database of references

Gubernari, N. and Kokulu, A. van Dyk, D. -  $B \rightarrow P$  and  $B \rightarrow V$  Form Factors from  $B$ -Meson Light-Cone Sum Rules beyond Leading Twist - [arXiv:1811.00983](https://arxiv.org/abs/1811.00983)



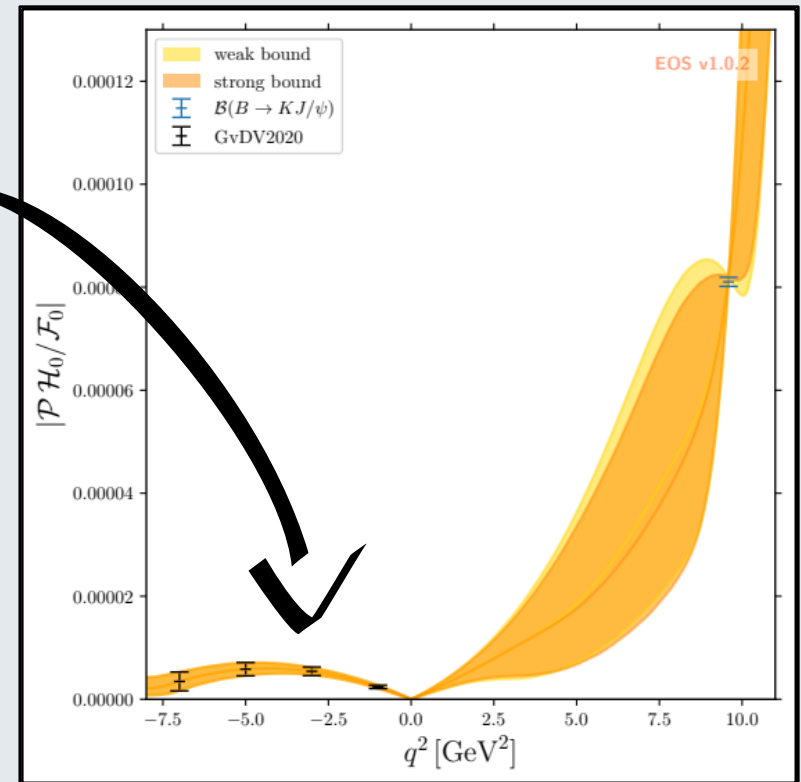
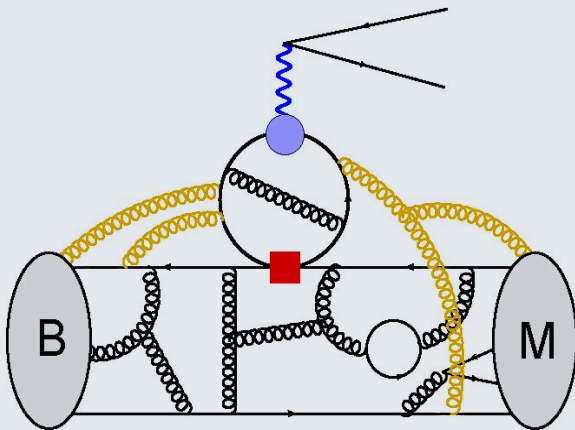
# Multi-steps fits



From *Improved Theory Predictions and Global Analysis of Exclusive  $b \rightarrow s \mu + \mu^-$  Processes* (2206.03797)

[N. Gubernari, MR, D. van Dyk, J. Virto]

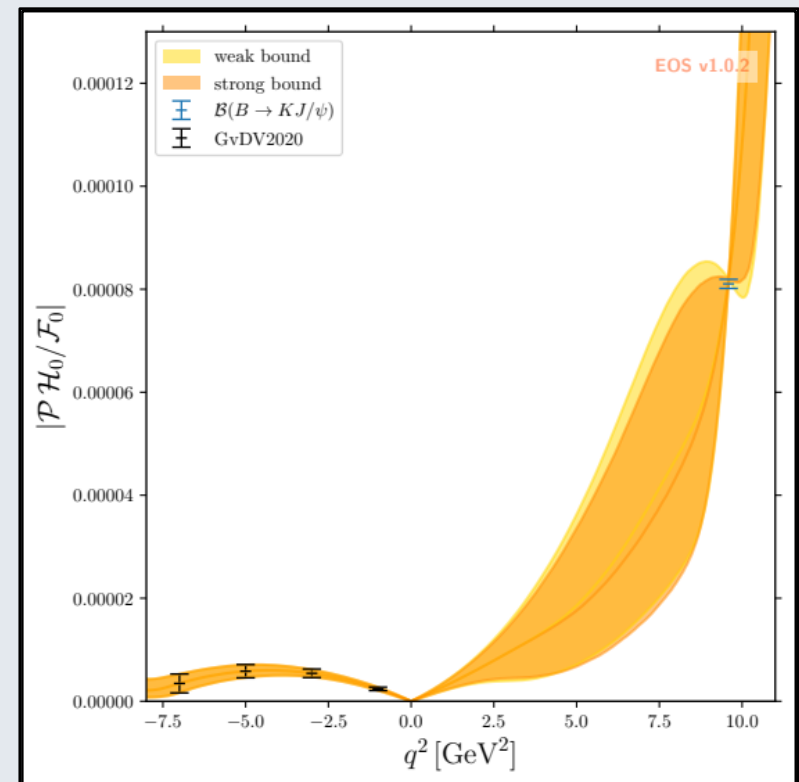
- 1) Fit **local** form-factors of  $B \rightarrow K^{(*)}$ ,  
 $B_s \rightarrow \varphi$  (46 parameters)
- 2) Use step 1 to **constrain the non-local** form factors (charm-loops)



From *Improved Theory Predictions and Global Analysis of Exclusive  $b \rightarrow s \mu + \mu^-$  Processes* (2206.03797)

[N. Gubernari, MR, D. van Dyk, J. Virto]

- 1) Fit **local** form-factors of  $B \rightarrow K^{(*)}$ ,  
 $B_s \rightarrow \varphi$  (46 parameters)
- 2) Use step 1 to **constrain** the **non-local** form factors (charm-loops)
- 3) Fit them in a new parametrization (84 parameters)
  - **130 nuisance parameters**
  - 'Proof of concept' fit to the WET's WC

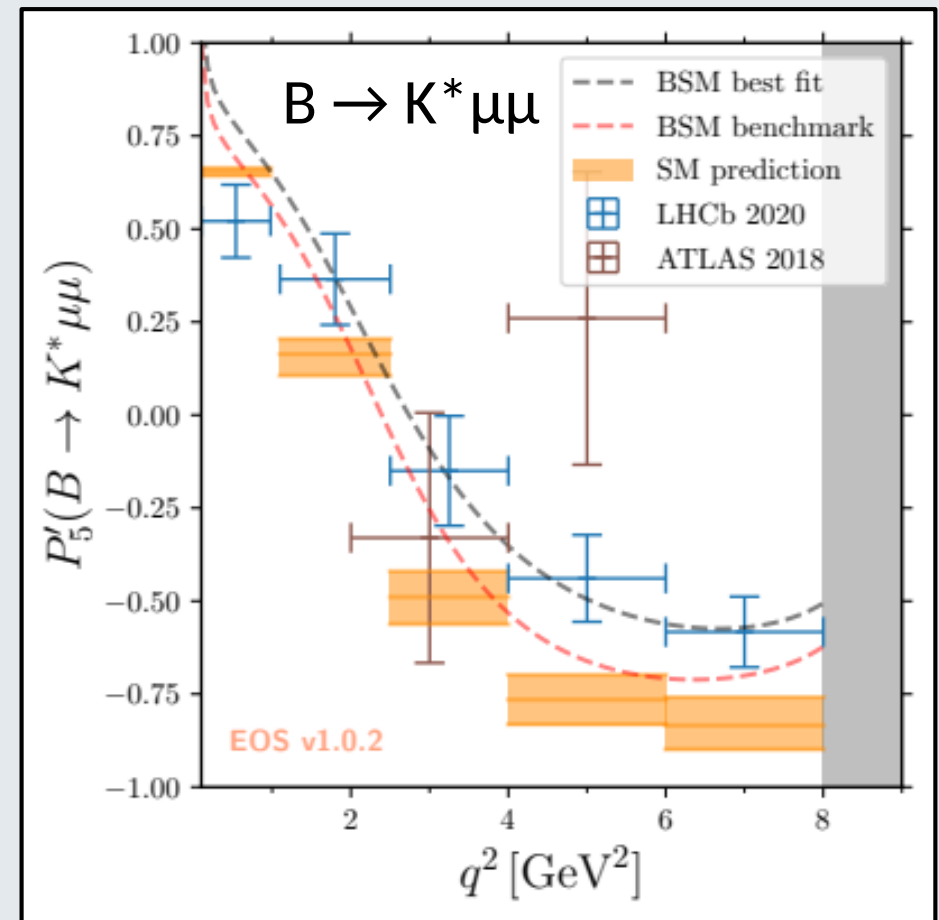
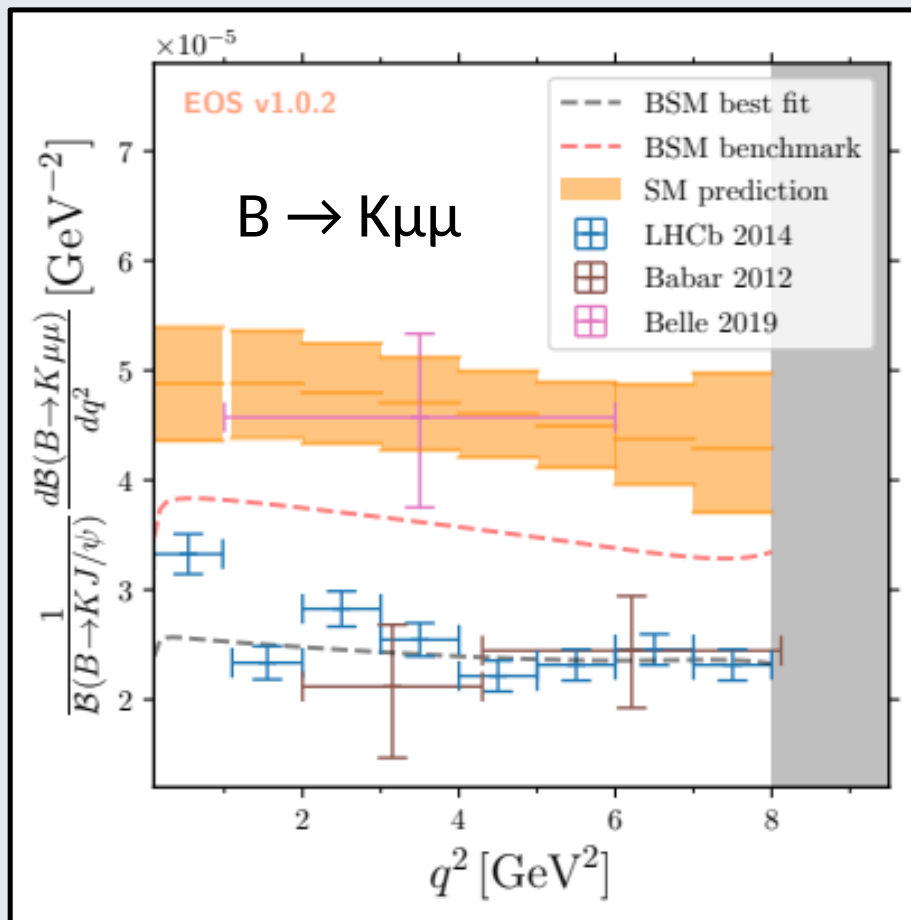


# Summary plots



From *Improved Theory Predictions and Global Analysis of Exclusive  $b \rightarrow s \mu^+ \mu^-$  Processes* (2206.03797)

[N. Gubernari, MR, D. van Dyk, J. Virto]







From *The Flavor of UV Physics* 2101.07273

[S. Bruggisser, R. Schäfer, D. van Dyk, S. Westhoff]

- **Simplify observables** to keep only the parameters of interest:

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) \times 10^9 = \underbrace{[3.57 - 1.71 C_{10} + 0.21 C_{10}^2]}_{\text{Wilson polynomial}} \times \underbrace{(1 \pm 1.2\%|_{f_{B_s}} \pm 1.5\%|_{\text{CKM}})}_{\text{Other uncertainties}},$$

Wilson polynomial

Other uncertainties

$$\mathcal{B}(B \rightarrow X_s \gamma) \times 10^4 = \underbrace{[3.26 - 15.17 C_7 - 0.77 C_8 + 1.66 C_7 C_8 + 1.36 C_{7'} C_{8'} + 18.03 (C_7^2 + C_{7'}^2) + 0.20 C_8^2 + 0.09 C_{8'}^2]}_{\text{Wilson polynomial}} \times \underbrace{(1 \pm 5\%)}_{\text{Other uncertainties}},$$

- Part of **WCxf** (<https://wcf.github.io/assets/pdf/WET.EOS.pdf>)  
→ Simple connection to SMEFT tools





### 3. EOS' Future



- Improve **statistical tools**
  - preparing for global analyses with  **$O(100)$  nuisance parameters**
  - interfacing to `dynesty` to make full use of **nested sampling** algorithm <https://dynesty.readthedocs.io>
- Constantly adding **new observables, form-factor parametrizations, ...**



- “Pre-packaged” low-energy analyses
  - **Remove nuisance parameters** to reduce complexity
  - Disseminate as a **Gaussian Mixture Model** of the WET coefficients
    - Do the hard work once :)
  - **Interface to**  **wilson** and  **smelli** for ease of use by model-building community



# Conclusion



- **EOS is open source**, the current version is **v1.0.5**
  - **~1000 (pseudo-)observables**, **~1000 parameters**, **~500 constraints**
  - Development on **github** <https://github.com/eos/eos/>
  - Used in **~35 theory papers** and many experimental papers; part of Belle II external software
- **Online documentation** and nice tutorials:  
<https://eos.github.io/doc/>
- We are happy to discuss how to **add further observables**

**Thank you!**