

# SUBA-Jet

## A New Coherent Jet Energy Loss Model For Heavy Ion Collisions

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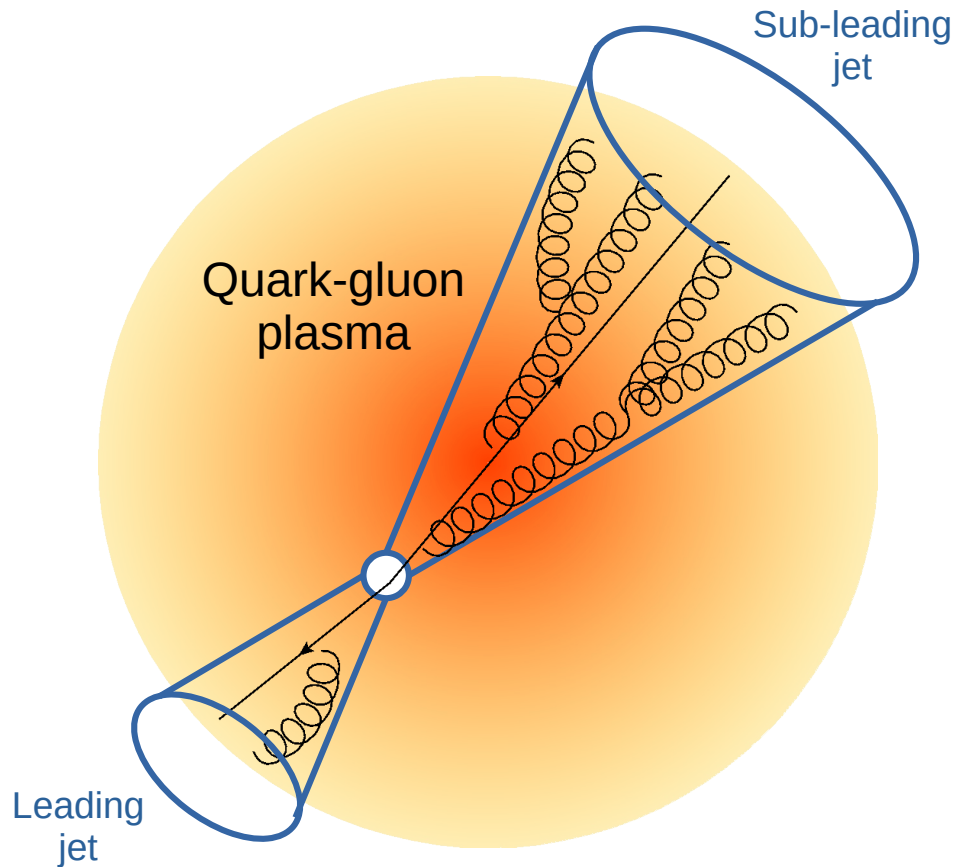
[arXiv:2404.14579 \[hep-ph\]](https://arxiv.org/abs/2404.14579)



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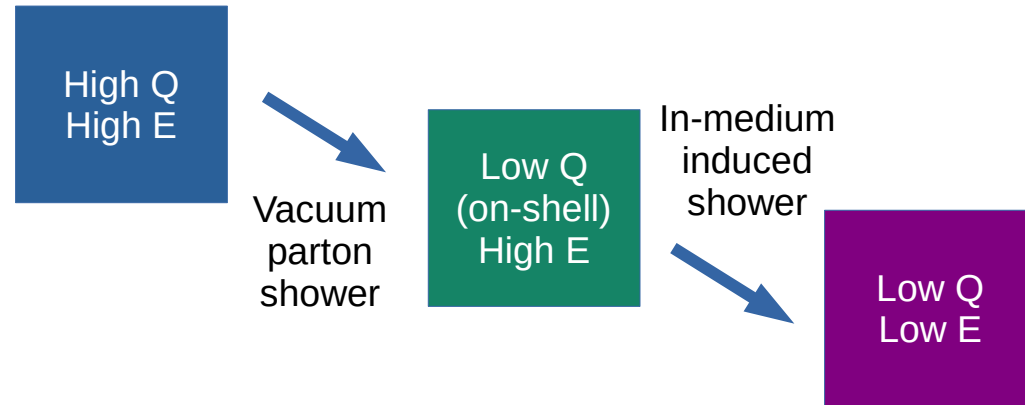
# Jets in Heavy Ion Collisions



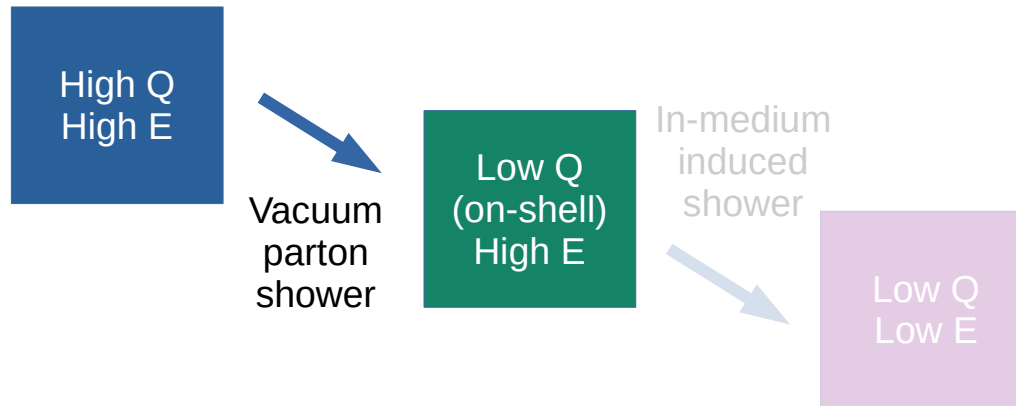
- Interactions between jet partons and the QGP medium leads to modifications of jet properties

→ **Jet Energy Loss / Quenching**

- **SUBA-Jet:**  
Monte Carlo for jet energy loss in heavy ion collisions



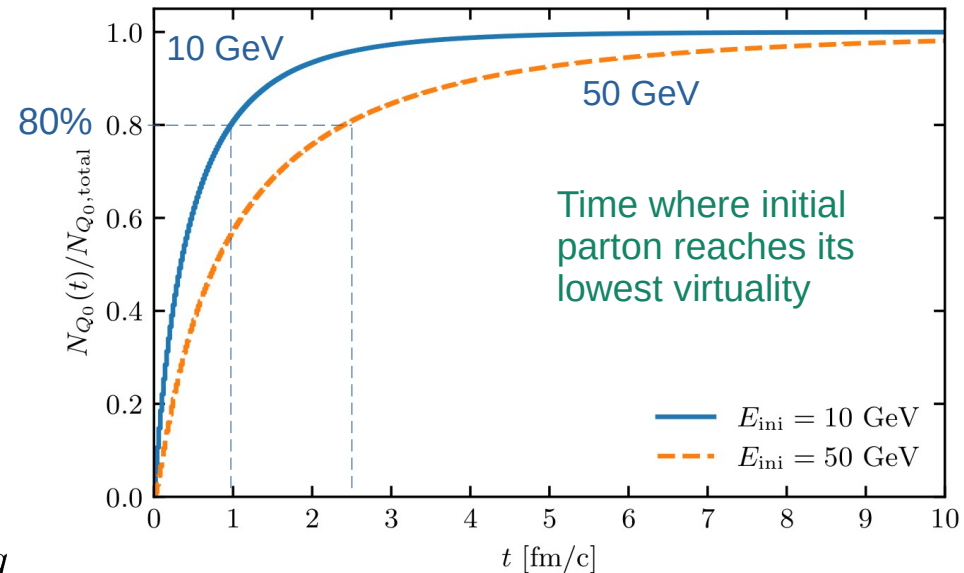
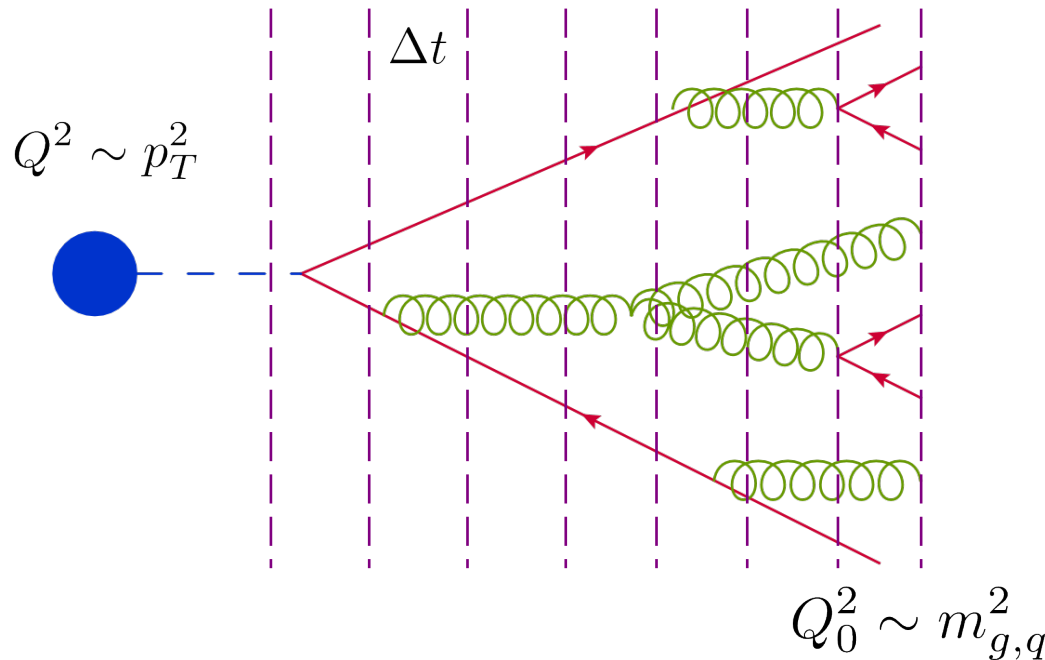
# High Virtuality Regime



# Vacuum Parton Shower

- Monte Carlo of a vacuum parton shower originally developed by Martin Rohrmoser
- Evolution according to the DGLAP equations from high virtuality  $Q_{\max} \sim p_T$  to low virtuality  $Q_0$
- Time evolution split into time steps, mean life time

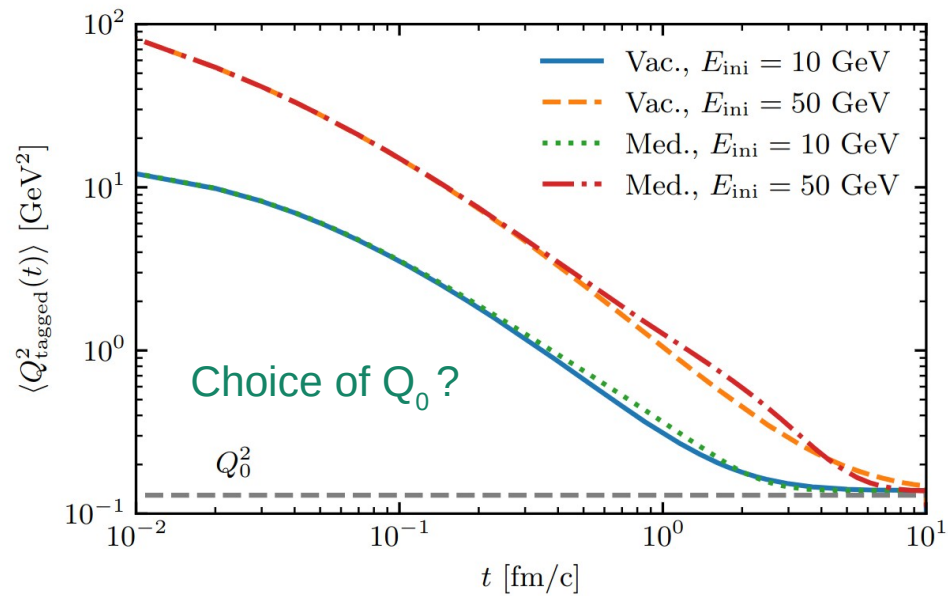
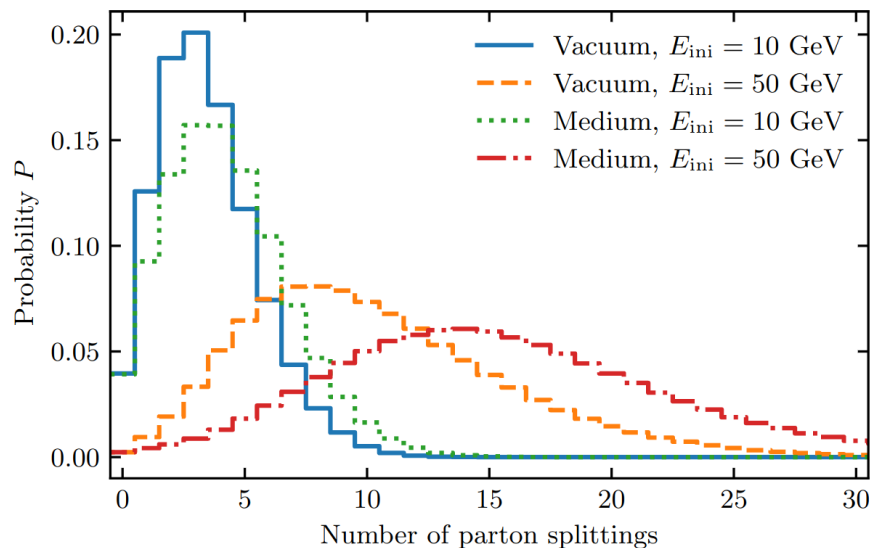
$$\Delta t = \tau = \frac{E}{Q^2}$$



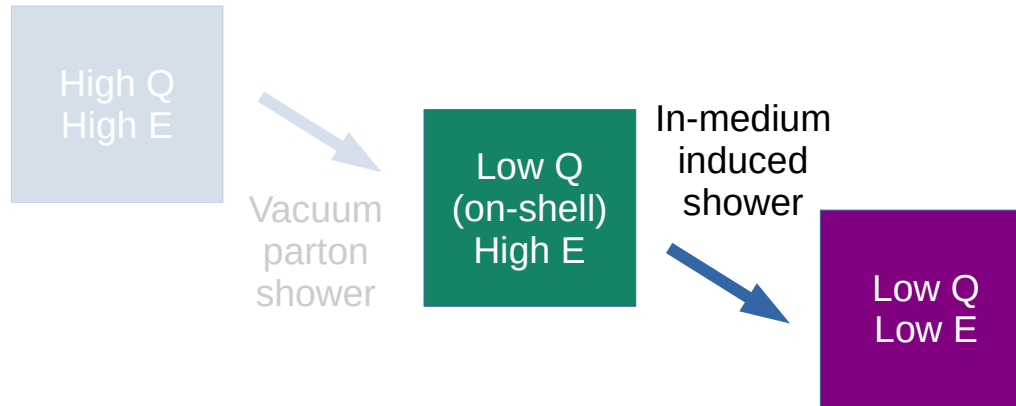
# “Vacuum” Parton Shower in Medium

- Medium interactions for high  $Q$  regime resulting in virtuality increase, similar to YaJEM (T. Renk, 2008)

$$\frac{dQ^2}{dt} = \hat{q}(T)$$

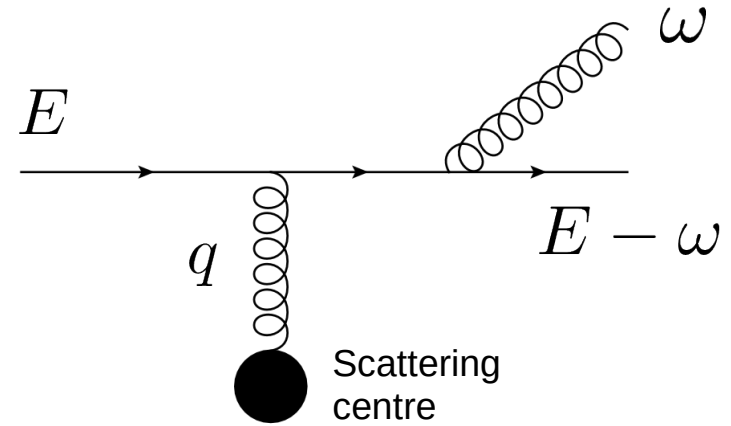


# Low Virtuality Regime



# Medium-Induced Single Radiation

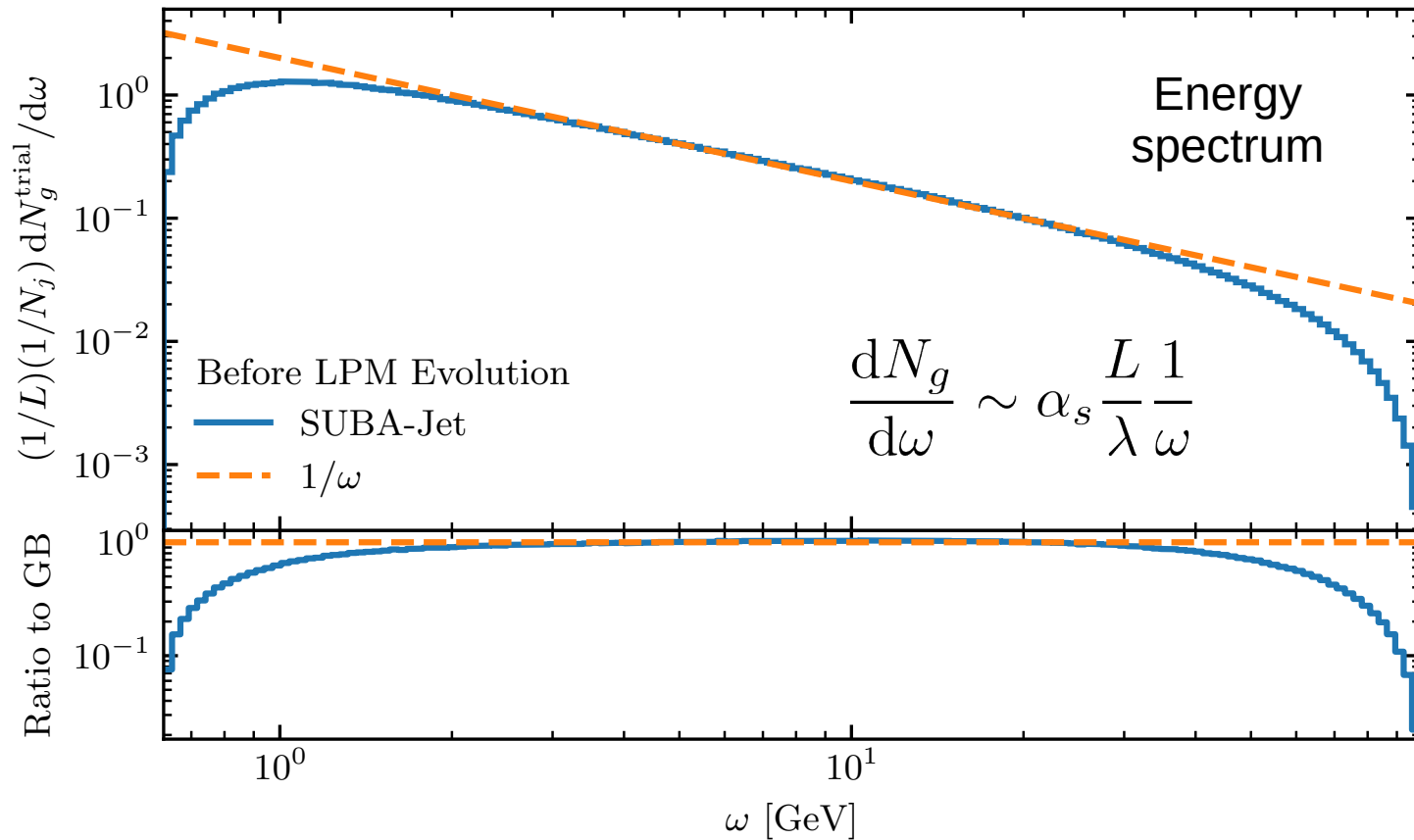
- **Inelastic collision:**  
Single gluon emission from single medium scattering
- **Original result from Gunion-Bertsch (1982)**  
Generalised to massive case by Aichelin, Gossiaux, Gousset (2014)
- **Initial Gunion-Bertsch seed:** i.e. radiation of a **preformed gluon** from a single scattering (Each parton can generate a number of preformed gluons)
- Gunion-Bertsch cross-section from scalar QCD



$$\frac{d\sigma^{Qq \rightarrow Qqg}}{dx d^2k_T d^2l_t} = \frac{d\sigma_{\text{el}}}{d^2l_t} P_g(x, k_T, l_T) \theta(\Delta)$$

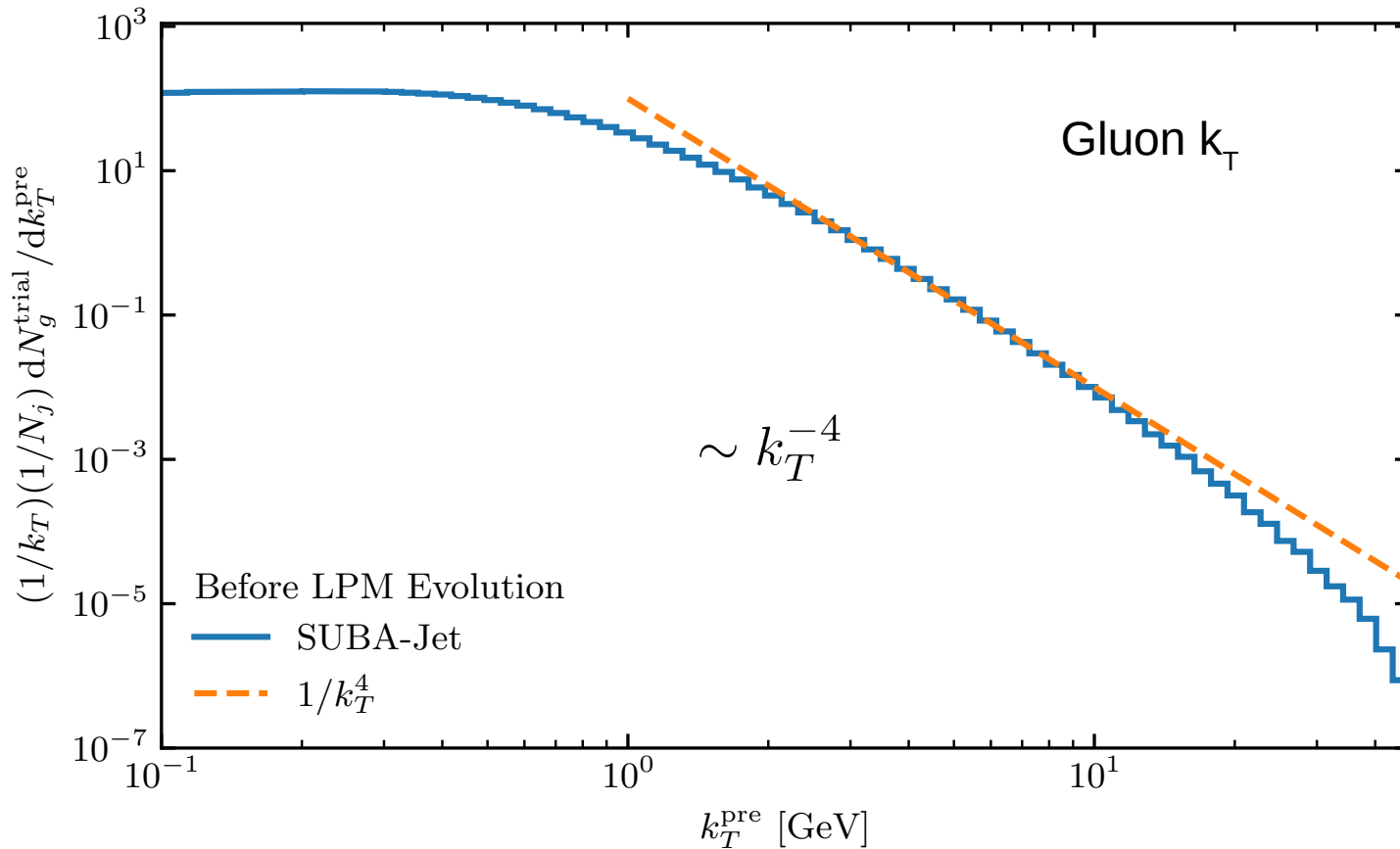
$$\frac{d\sigma_{\text{el}}}{d^2l_t} \sim \frac{8\alpha_s^2}{9(l_T^2 + \mu^2)^2}$$

# Medium-Induced Single Radiation





# Medium-Induced Single Radiation



# Coherency and the LPM Effect

- The formation of the radiated gluon is a quantum mechanical process

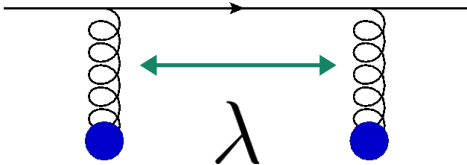
**Formation time:**  $t_f \sim \sqrt{\frac{\omega}{\hat{q}}}$

- Coherence effects:  
Landau-Pomeranchuk-Migdal (LPM) effect

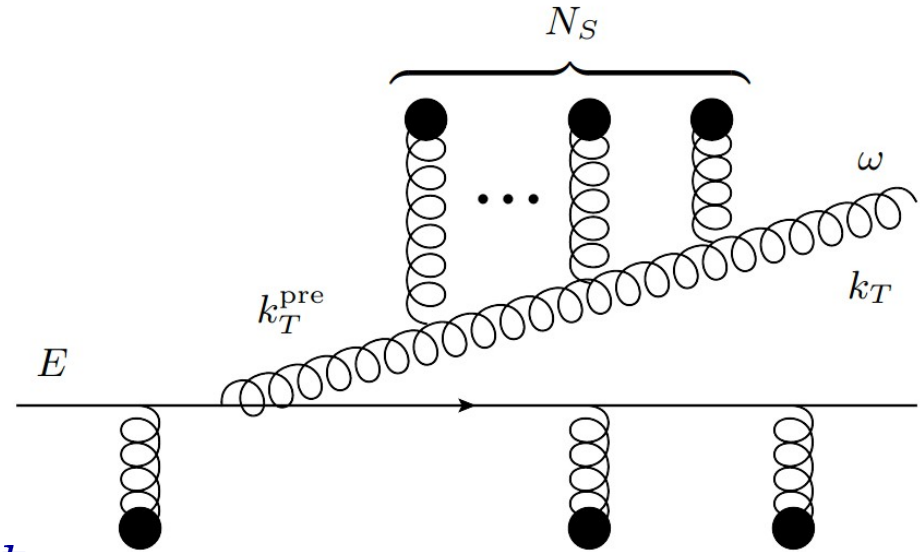
- Have to take into account multiple scatterings with the medium during the formation time

$\omega$  = gluon energy

$\hat{q}$  = medium modifications

$$N_s = \frac{t_f}{\lambda}$$


$$\lambda \simeq \frac{\hbar c}{\alpha_s T}$$



$L$  = path length of medium

# Implementation of the LPM Effect

- At each timestep:

- Elastic scattering with prob.  $\Gamma_{\text{el}}\Delta t$

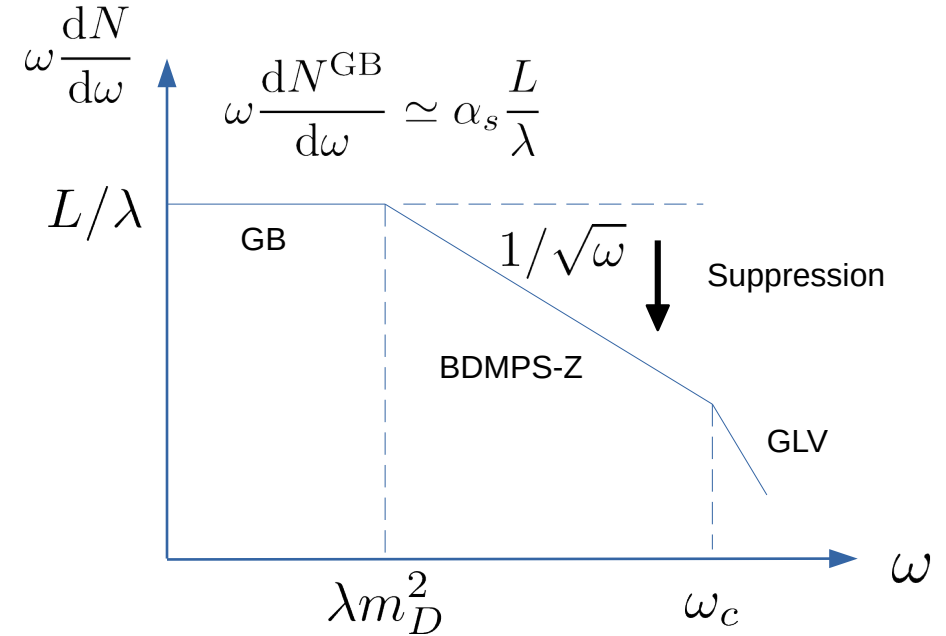
$$\Gamma_{\text{el}}^q = \left(1 + \frac{N_f}{N}\right) \frac{(N^2 - 1)T^3}{\pi\hbar c} \frac{4\alpha_s^2}{\mu^2}$$

- Radiation of preformed gluon with prob.  $\Gamma_{\text{inel}}\Delta t$

- BDMPS-Z spectrum at intermediate energies achieved by suppressing GB seed by  $1/N_s$

Like in Zapp, Stachel, Wiedemann, JHEP 07 (2011), 118

Radiation energy spectrum:



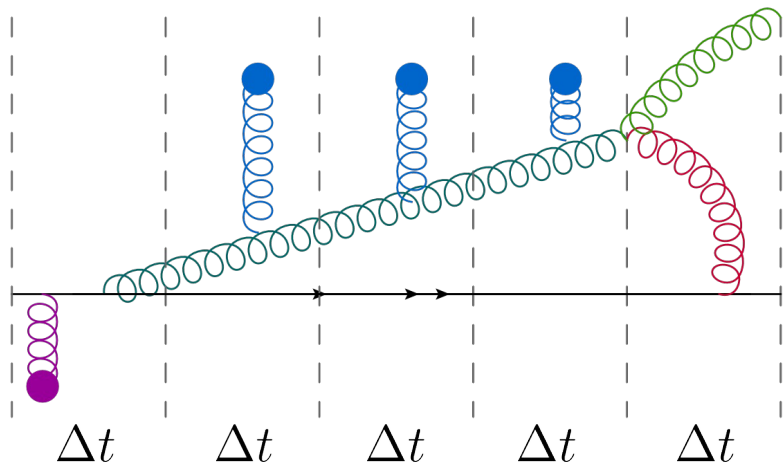
$$\omega \frac{dN^{\text{BDMPS-Z}}}{d\omega} \simeq \alpha_s \sqrt{\frac{\hat{q} L^2}{\omega}}$$

# The Algorithm

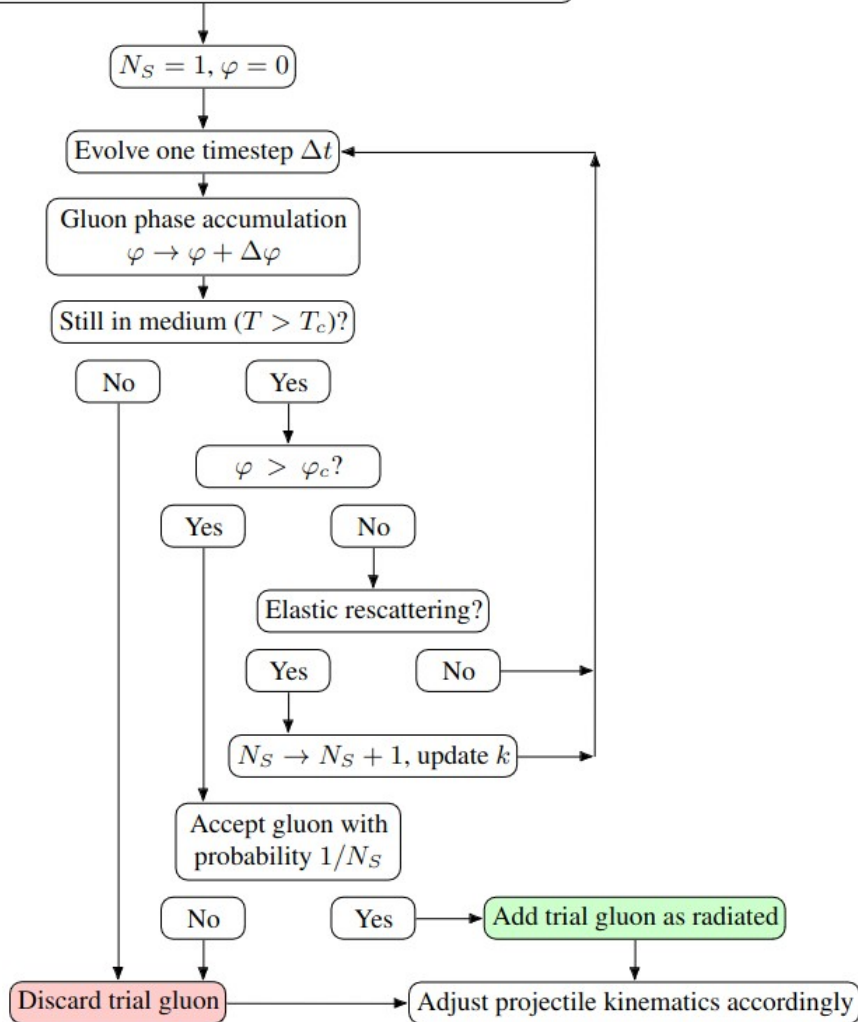
Flow diagram:

Algorithm for the coherent medium-induced gluon radiation in our model

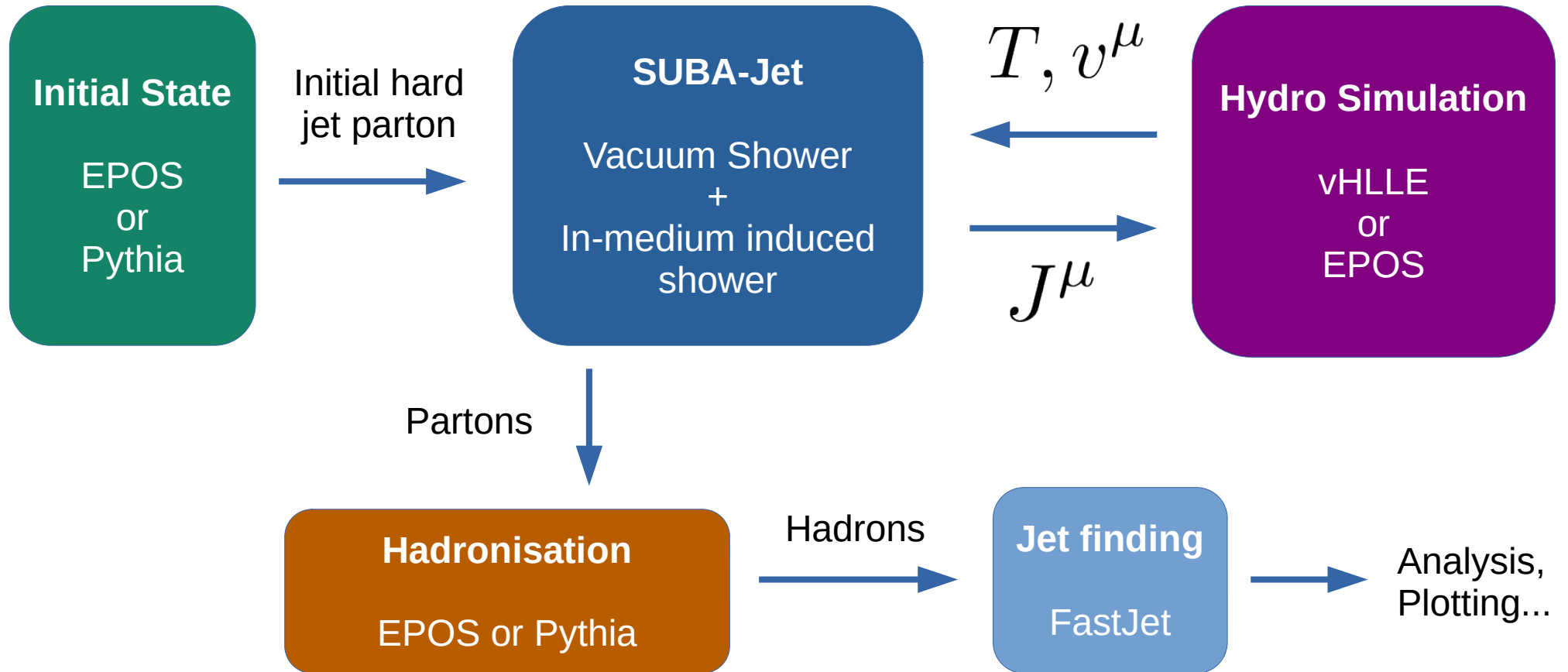
Various parameters and settings can be changed and tuned to compare distributions



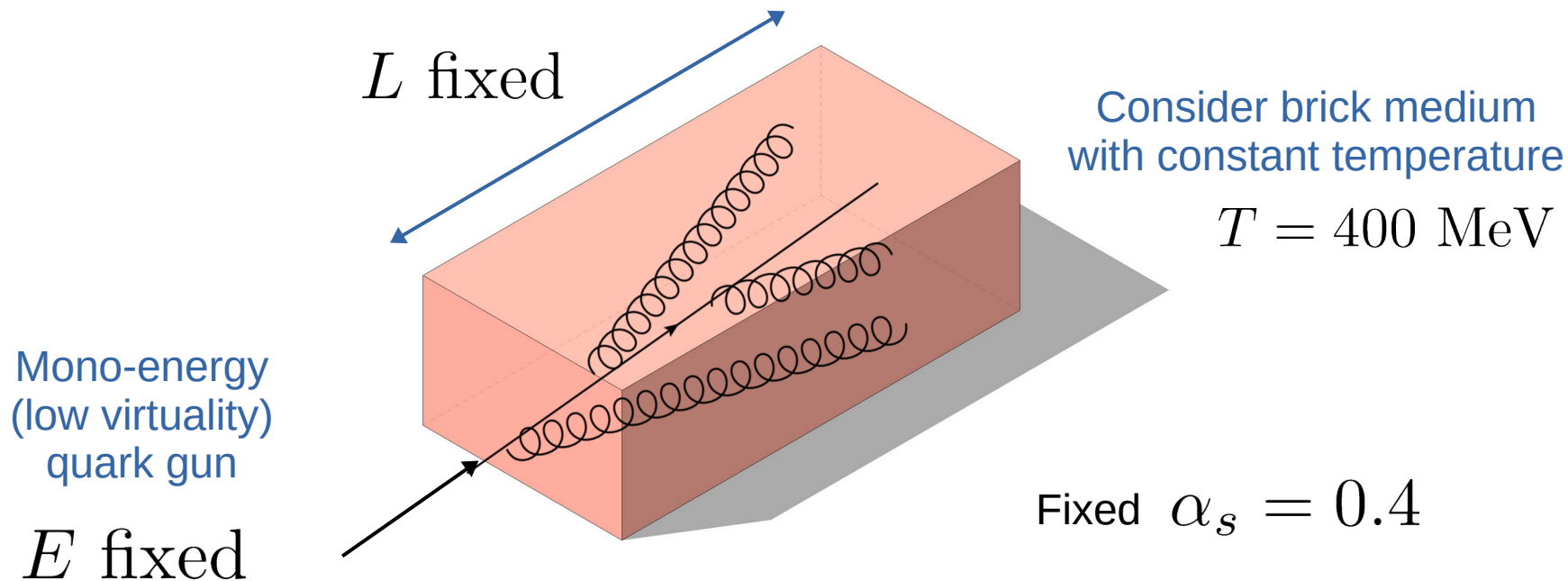
Trial (preformed) incoherent gluon formation according to GB seed



# The Monte Carlo

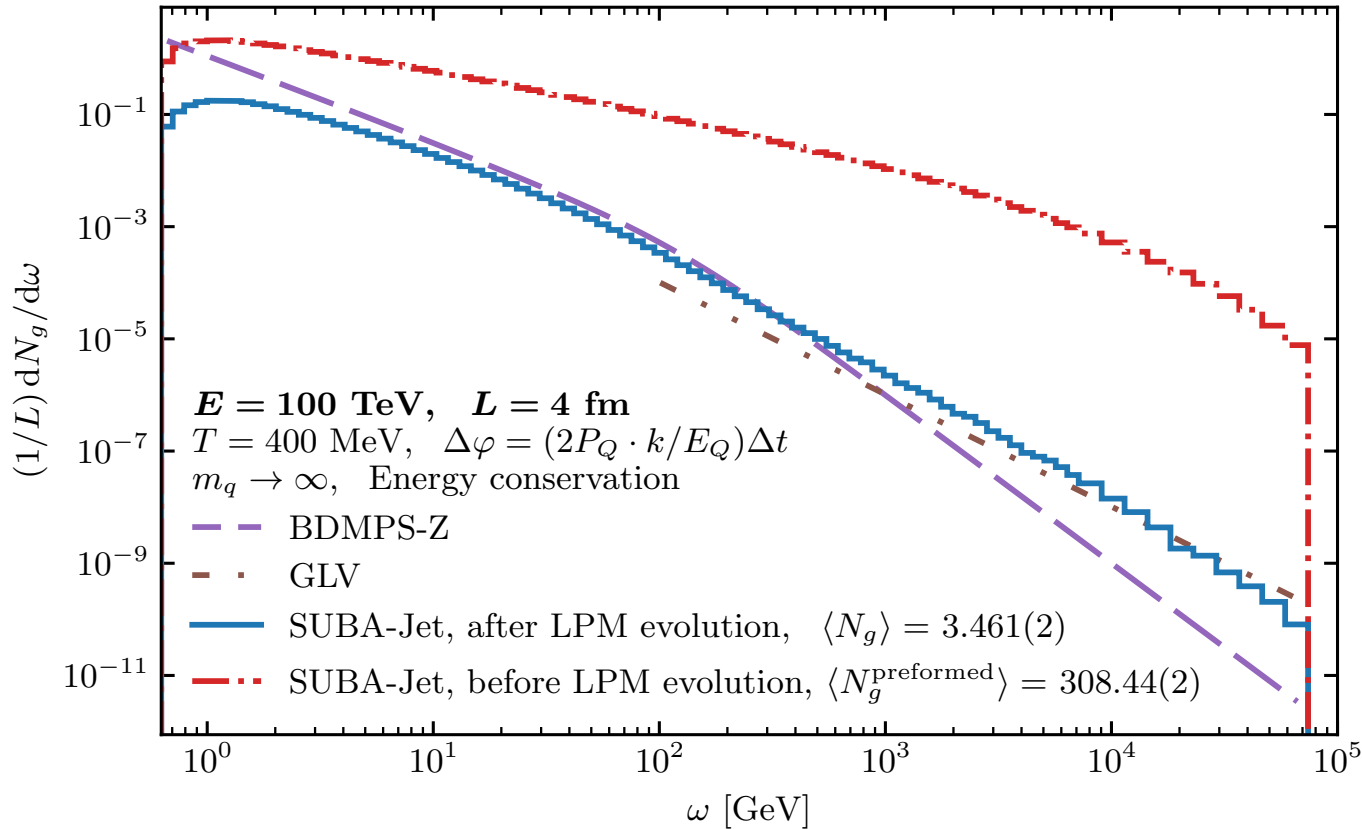


# First Results



**We want to reproduce theoretical expectations**

# Reproduction of the LPM and GLV regimes



Gluon energy  $\omega$  spectrum

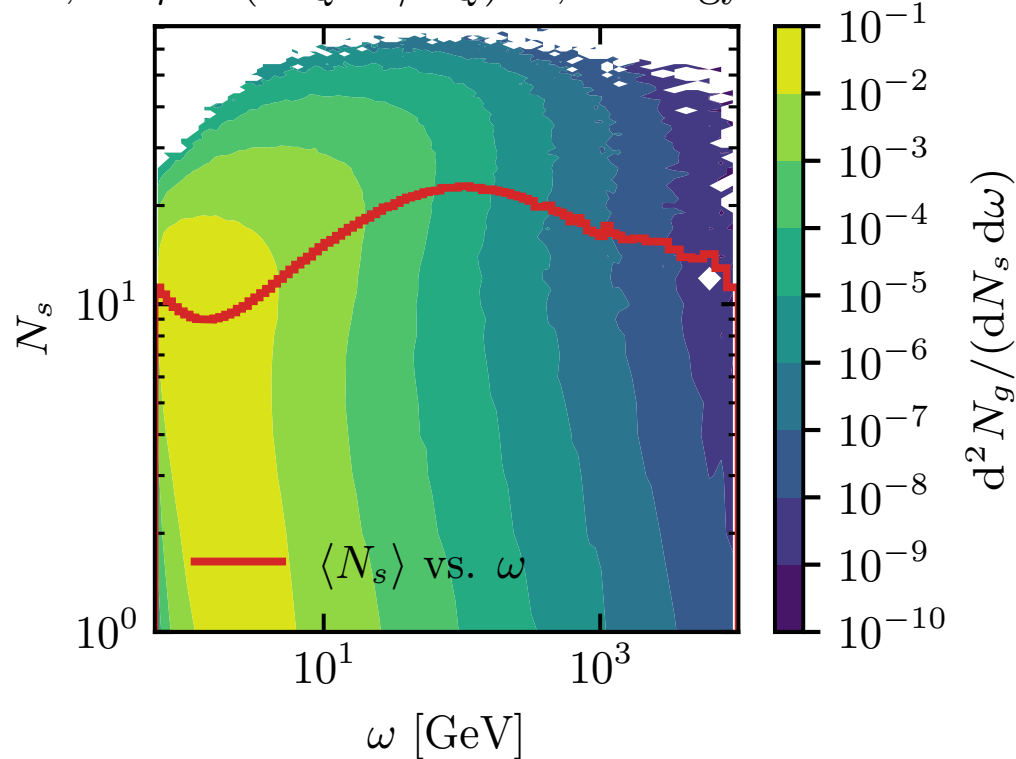
$$\frac{dN^{\text{LPM}}}{d\omega} \sim \frac{1}{\omega^{3/2}}$$

$$\frac{dN^{\text{GLV}}}{d\omega} \sim \frac{1}{\omega^2}$$

# Reproduction of the LPM and GLV regimes

$E = 100 \text{ TeV}$ ,  $L = 4 \text{ fm}$ ,  $T = 400 \text{ MeV}$

$m_q \rightarrow \infty$ ,  $\Delta\varphi = (2P_Q \cdot k/E_Q)\Delta t$ , Energy conservation



Double differential plot  
in  $N_s$  and  $\omega$

Red line:  $\langle N_s \rangle$  vs.  $\omega$

$$N_s \sim t_f \sim \sqrt{\omega}$$

Convolution of different  
distributions



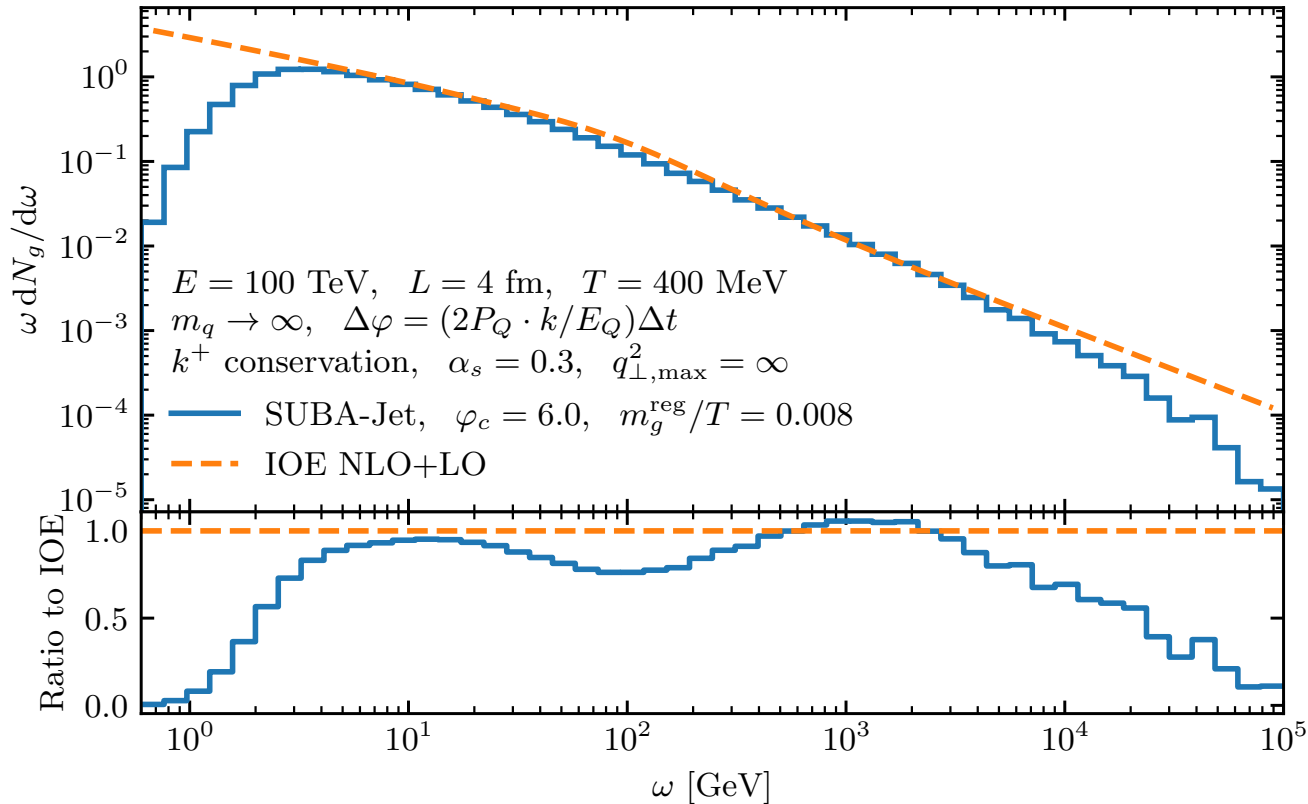
# Reproduction of the IOE

Improved Opacity Expansion

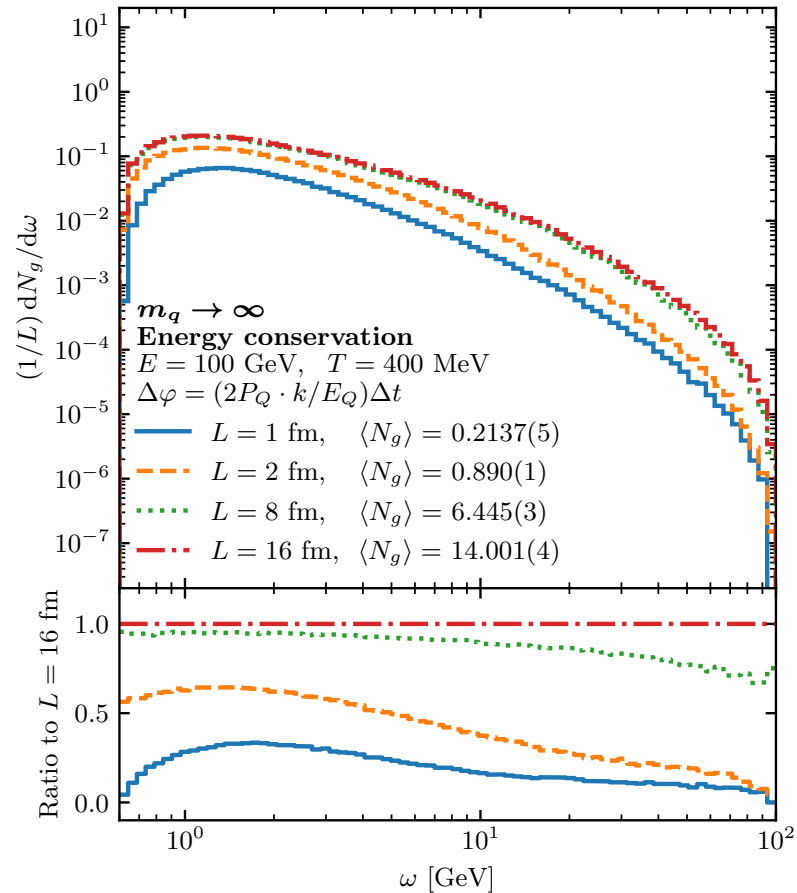
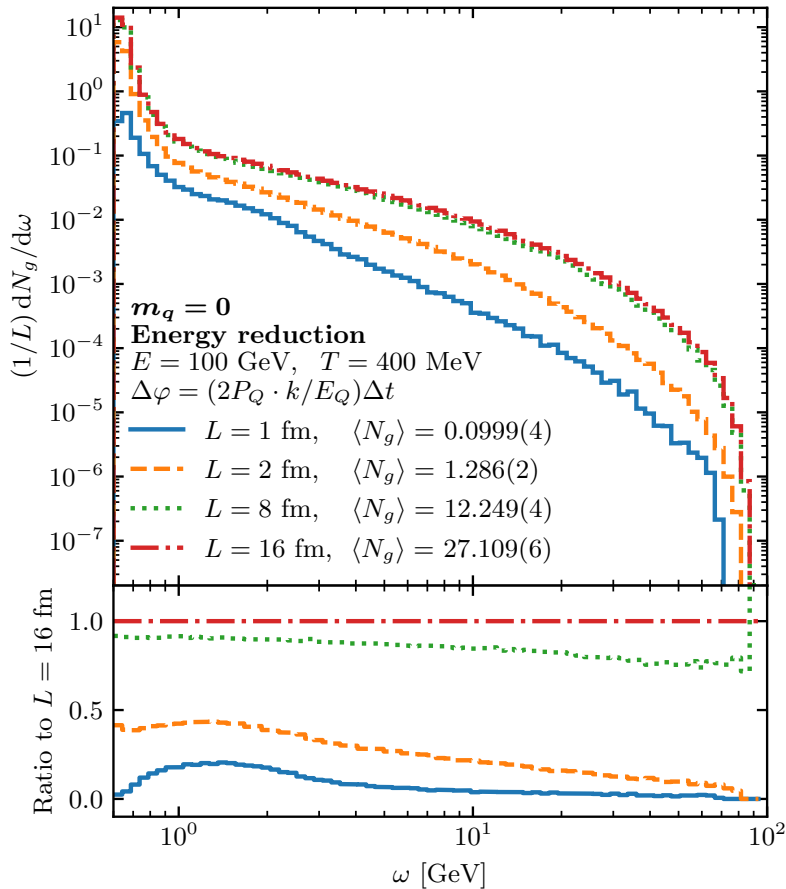
arXiv:1910.02032 [hep-ph]

$$\frac{dN^{\text{IOE}}}{d\omega} = \frac{dN_{\text{LO}}^{\text{IOE}}}{d\omega} + \frac{dN_{\text{NLO}}^{\text{IOE}}}{d\omega}$$

$$\omega \frac{dN_{\text{NLO}}^{\text{IOE}}}{d\omega} \simeq \frac{1}{2} \frac{\alpha_s C_R}{\pi} \hat{q}_0 \text{Re} \int_0^L ds \frac{1}{k^2(s)} \left[ \ln \frac{k^2(s)}{Q^2} + \gamma_E \right]$$



# The Role of the Path Length



$$\frac{dN}{d\omega} \stackrel{L \rightarrow \infty}{\approx} L$$

# Looking Forward: Towards More Realism

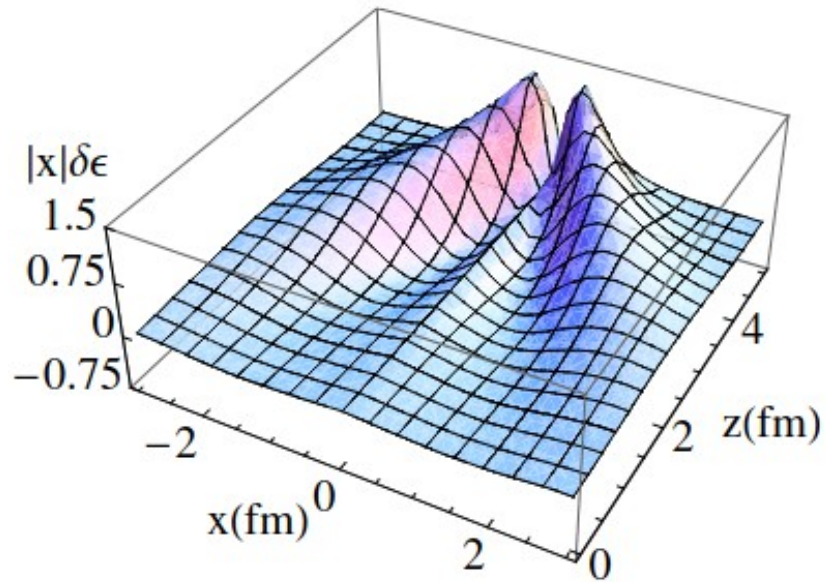
## Next step:

- **Implementation in two different MC frameworks:**
  - SUBA-Jet + EPOS4
  - SUBA-Jet + Pythia 8
- Realistic QGP evolution
- Pre-equilibrium stage
- Hadronisation
- Hadronic phase



# Looking Forward: Effect on the Medium

The jet also affects the medium



'Wake wave'  
in the medium  
due to the jet



G.-Y. Qin, A. Majumder, H. Song, U. Heinz  
0903.2255 [nucl-th]

# Summary

- We have presented a new model for jet energy loss in heavy ion collisions
- Implementation in a Monte Carlo framework
- **First step done:**
  - Reproduction of the BDMPS-Z and GLV limits
- **Next step:** Implementation within the new EPOS4
  - **EPOS4+JETS** – Initial state, hydro, and hadronisation from EPOS4

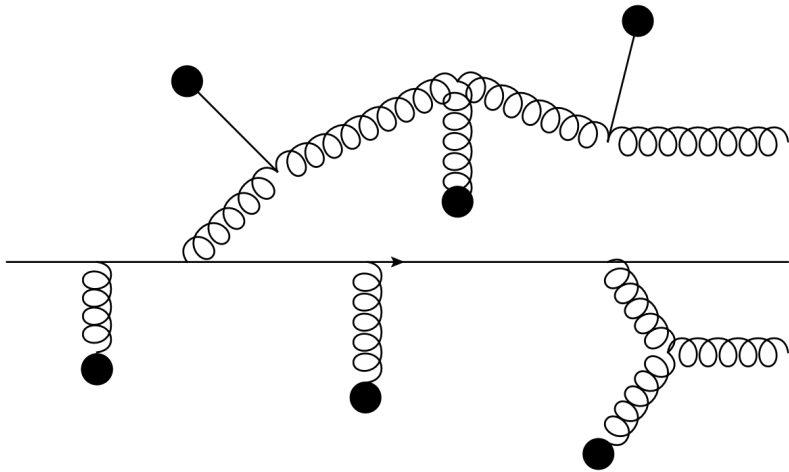
A low-angle, upward-looking photograph of a basketball hoop and net. The hoop is a dark, thick metal ring, and the net is a light-colored, woven mesh. The background is a clear, bright blue sky with a few wispy white clouds. The perspective is from below, looking up at the hoop.

Thank you for  
your attention!

# Backup Slides

# The Role of the Phase Accumulation

Choice of phase accumulation  
of the preformed (trial) gluons:



- **More general formula:**

$$\Delta\varphi = \frac{2P_Q \cdot k}{E_Q} \Delta t$$

- **What is used in JEWEL:**

$$\Delta\varphi = \frac{k_T^2}{\omega} \Delta t$$

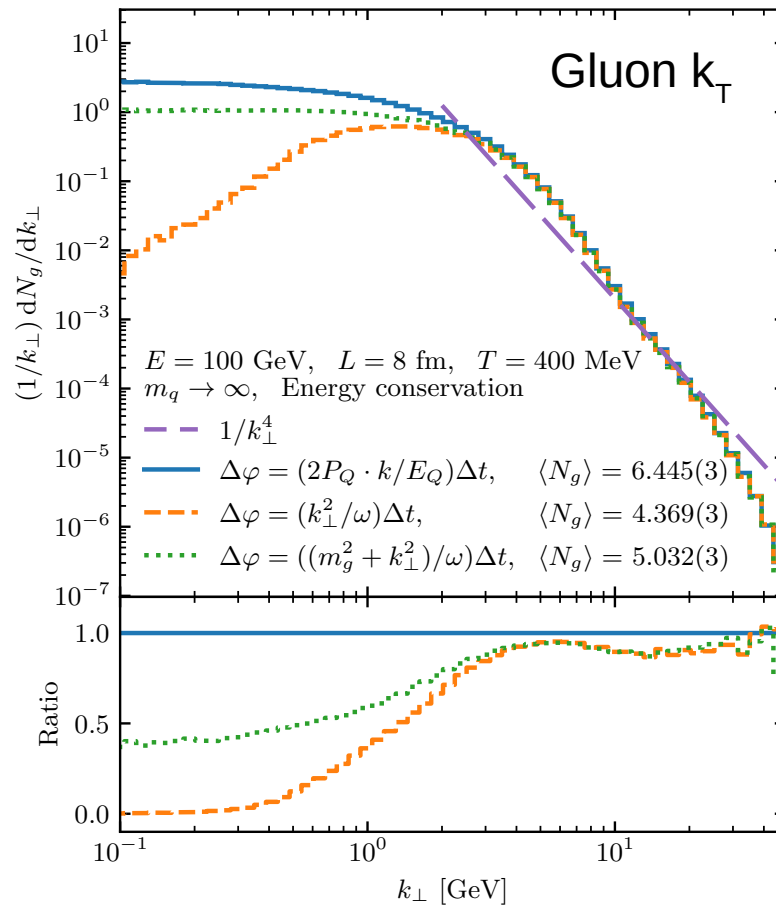
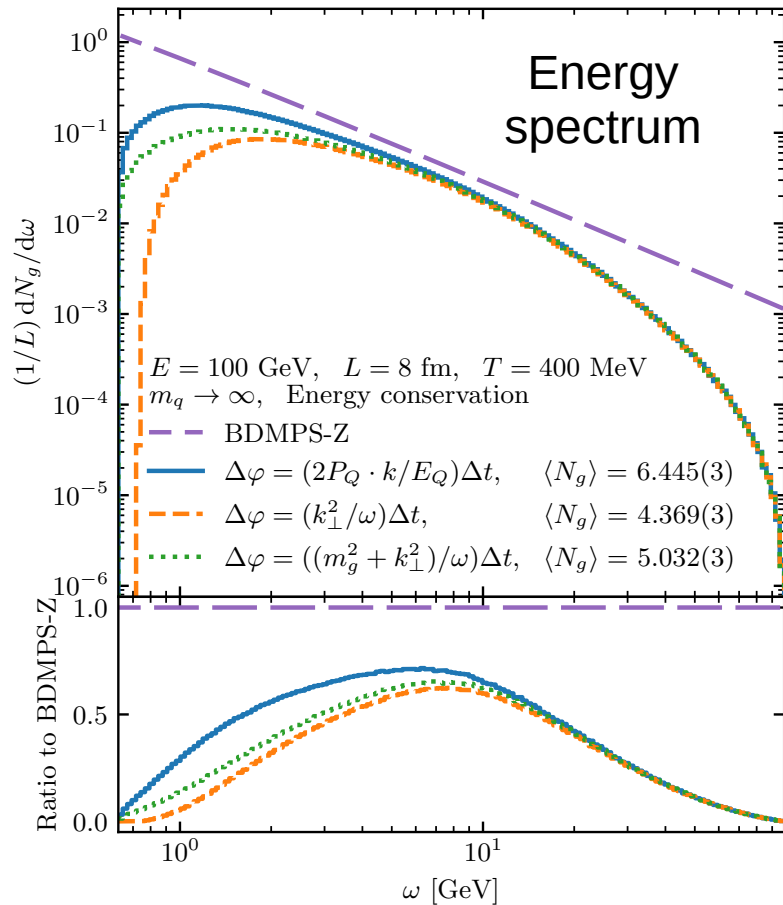
- **Including thermal gluon mass:**

$$\Delta\varphi = \frac{m_g^2 + k_T^2}{\omega} \Delta t$$



# The Role of the Phase Accumulation

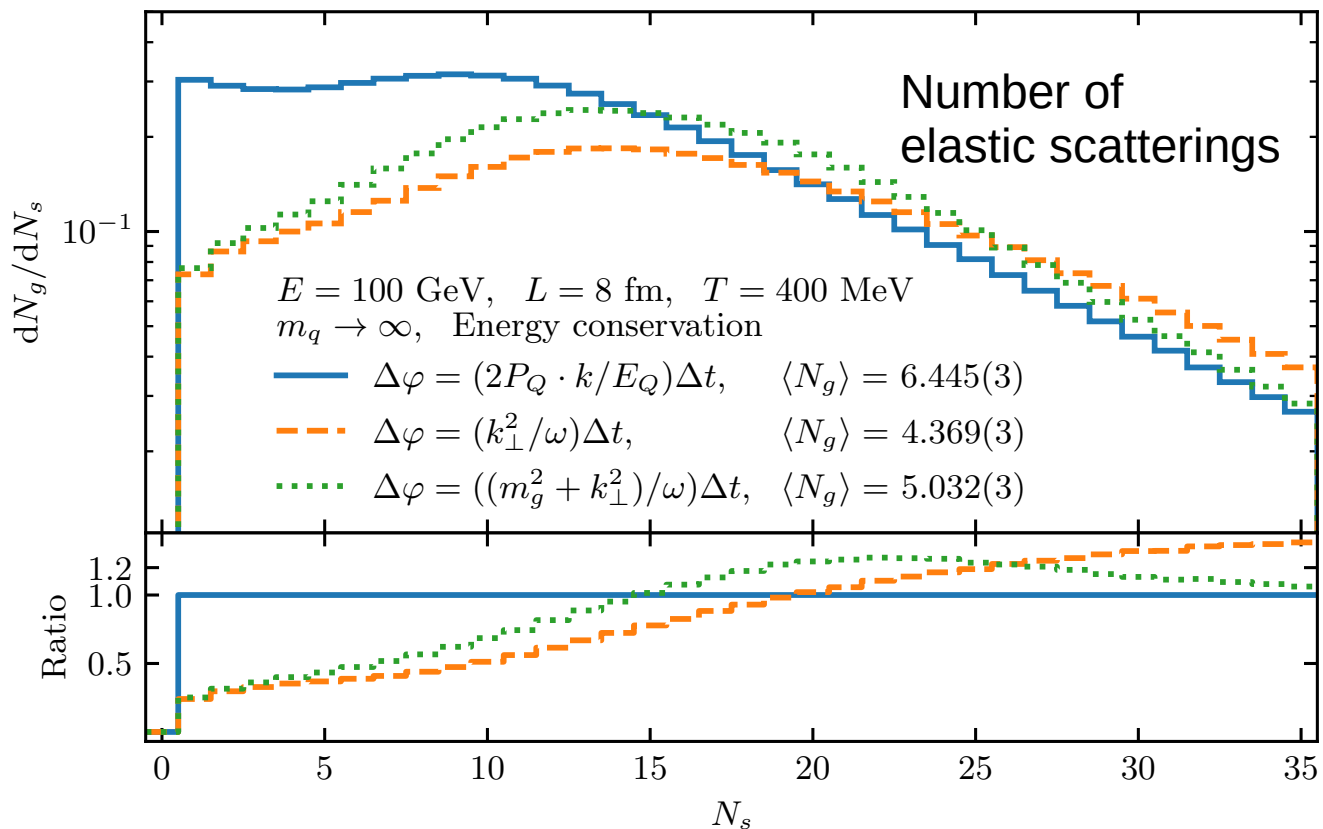
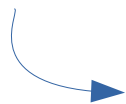
Effects at low energy & low  $k_T$



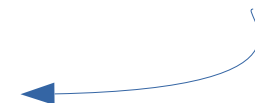
Number of radiated gluons per jet  $\sim 5 - 6$

# The Role of the Phase Accumulation

Effects at low  $N_s$

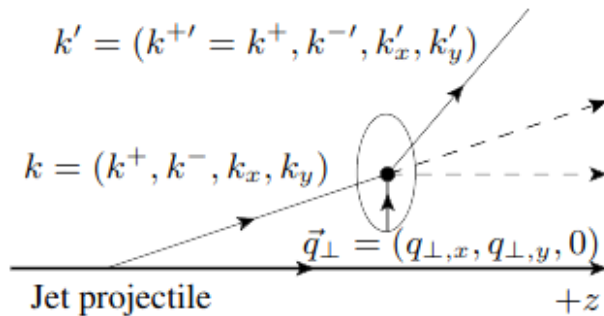


When neglecting the gluon mass in the phase accumulation, a larger path length is required to have a comparable overall number of radiations

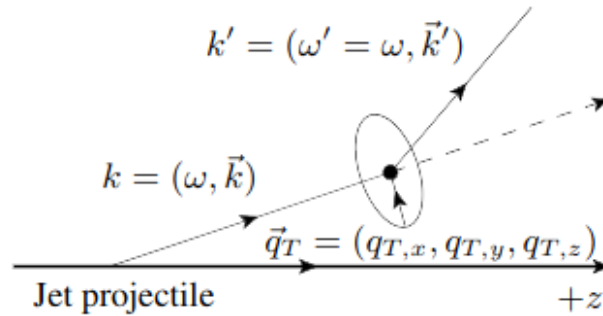


# The Role of the Elastic Scatterings

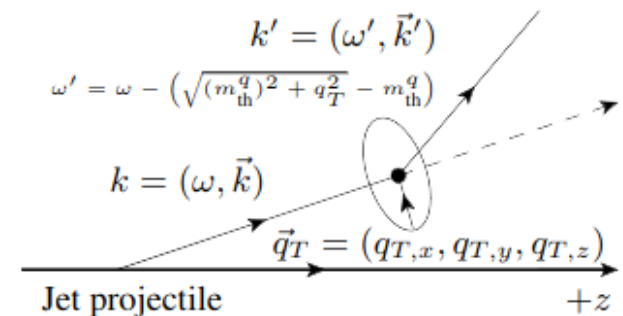
Choice of prescription in elastic scatterings:



$k^+$  conservation

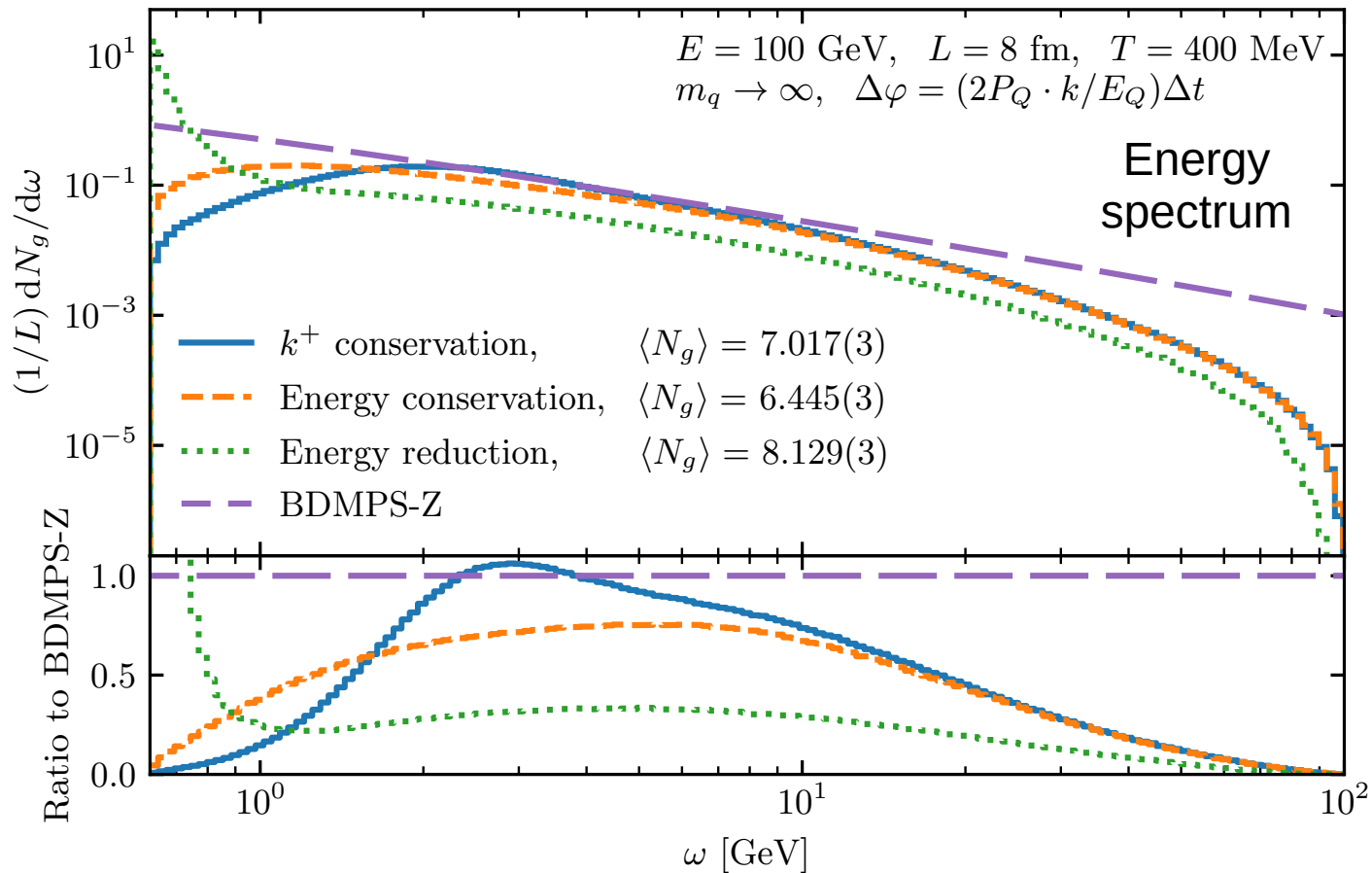


Energy conservation



Energy reduction

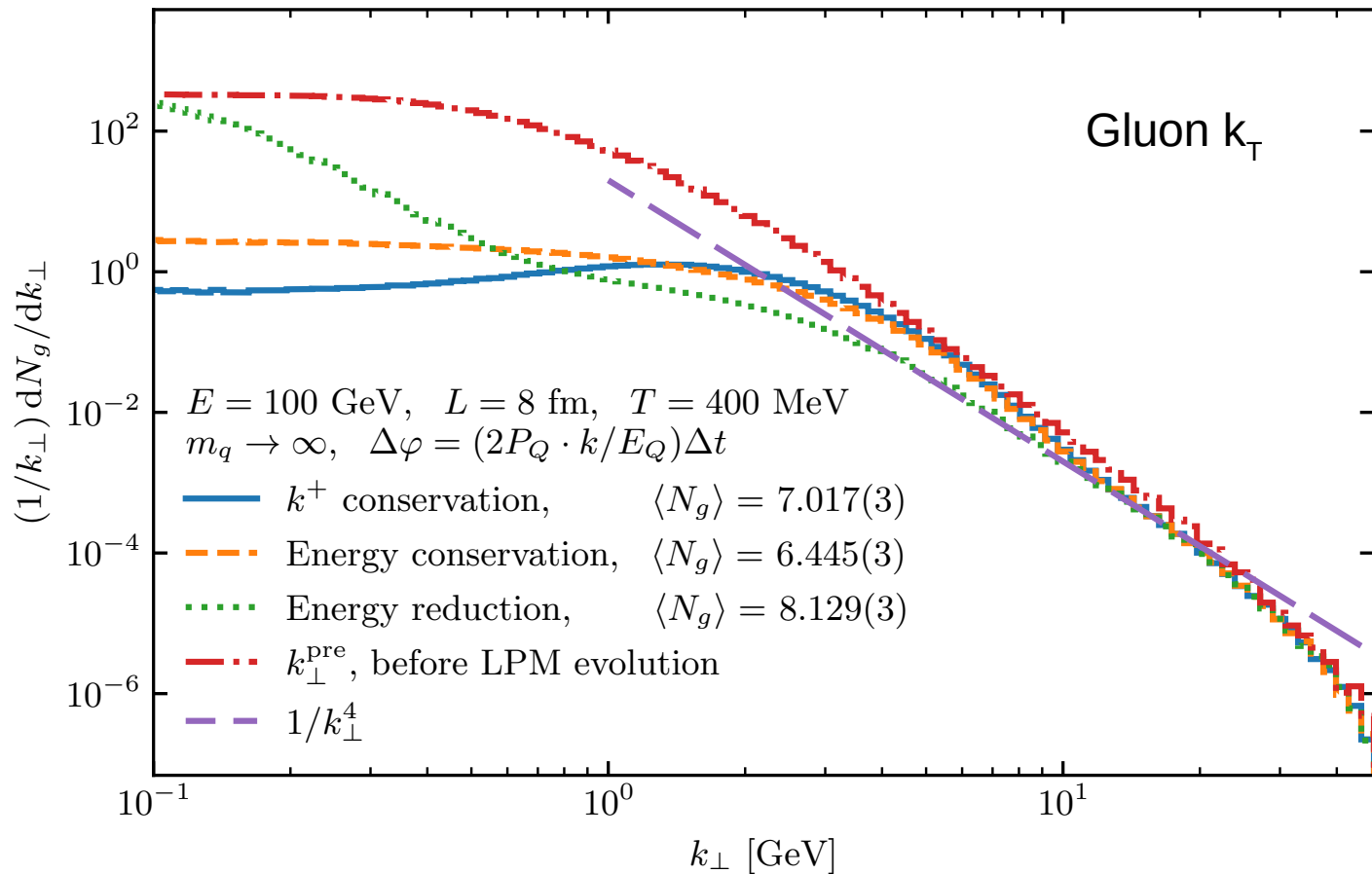
# The Role of the Elastic Scatterings



Same BDMS behaviour at intermediate energies

Difference at small energies

# The Role of the Elastic Scatterings



Large difference at small  $k_{\perp}$