

QNP

2024

Barcelona, July 8-12



Investigating finite-temperature dependence of electromagnetic dipole transitions in nuclei

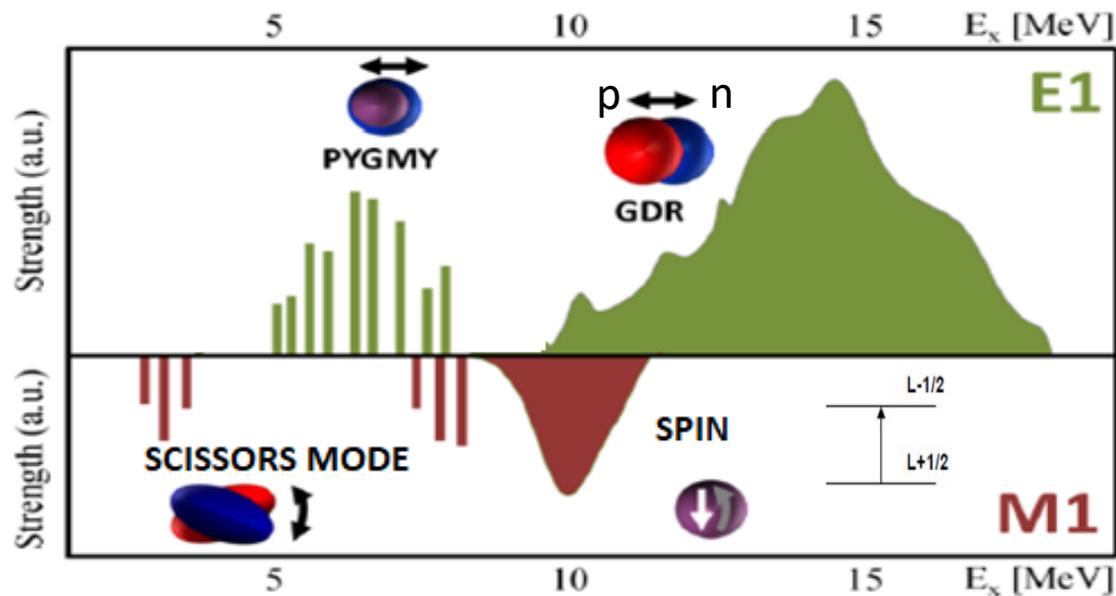
Amandeep Kaur



Department of Physics, University of Zagreb, Croatia

Email: akaur.phy@pmf.hr

Electromagnetic dipole response of a nucleus

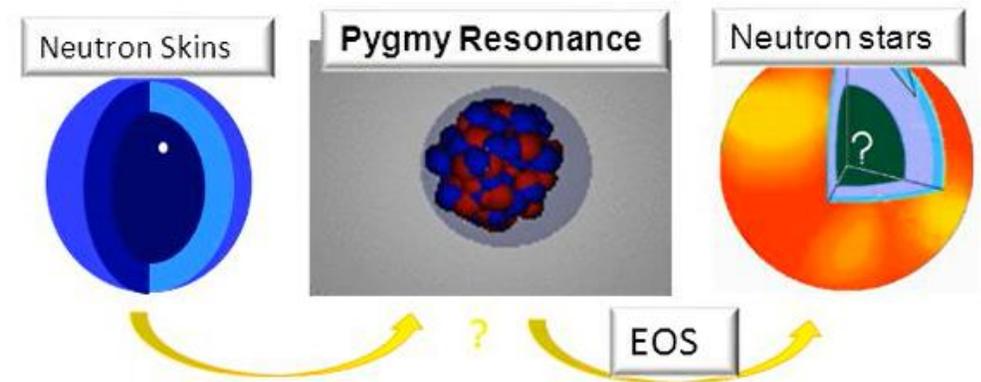


D. Budker et al. <https://onlinelibrary.wiley.com/doi/full/10.1002/andp.202100284>

Astrophysical Interest

- ✓ *Pygmy E1 strengths* → Provides information about neutron skin and symmetry energy in EOS → Relevant for modelling of neutron stars.
- ✓ *Impact the gamma strength functions, reaction rates and r-process nucleosynthesis in the stellar environment.*

- ✓ *Give information on the fundamental properties of nuclei.*
- ✓ *Provide insight into the behaviour of nuclear matter under extreme conditions.*



Electromagnetic dipole response of a nucleus

- ✓ Nuclei exist at high temperatures in stellar environments.
- ✓ **Experimental studies are available on GDR at finite temperature** mainly using fusion-evaporation reaction forming hot and rotating compound nucleus (CN).
- ✓ No experiments so far have searched the PDR mode at finite temperature.

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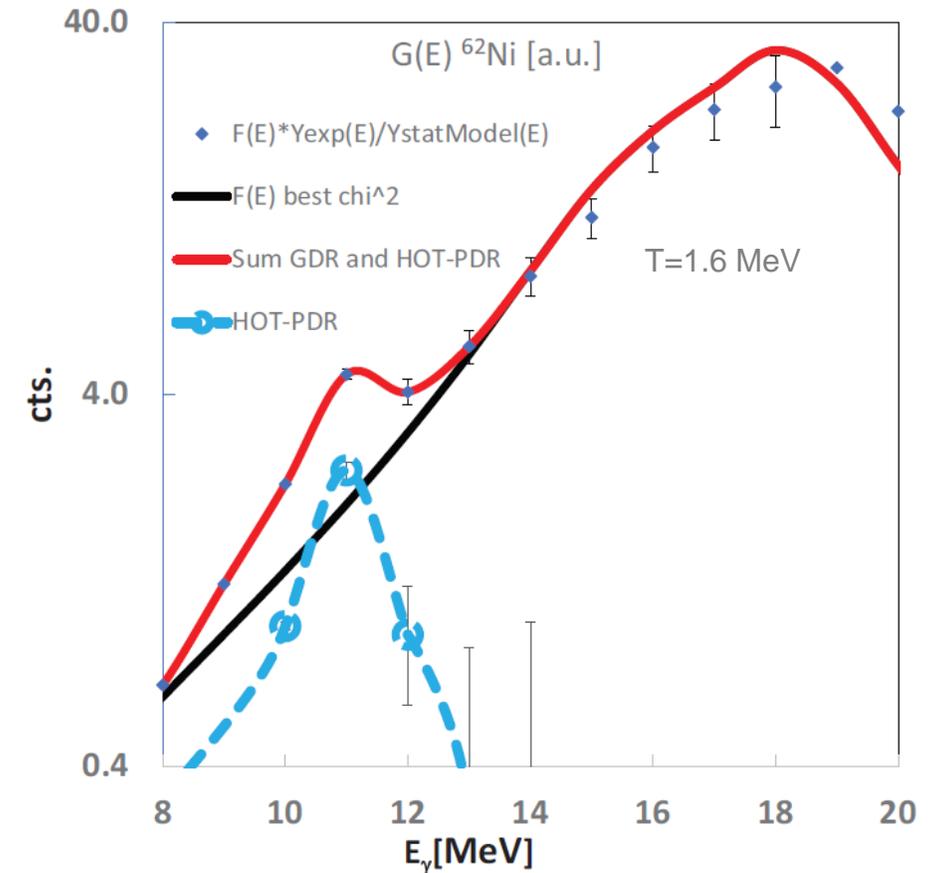
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Recent Experimental Work in Progress in Ni isotopes

O. Wieland, Comex7; (<https://agenda.infn.it/event/21964>)

- ✓ Some evidence of a possible extra strength is observed in neutron-rich nucleus.
- ✓ Appears not in $N=Z$ nucleus but (only) in $N=Z+xn$ nucleus at high excitation energy (CN temperature up to ≈ 2 MeV).
- ✓ Located below GDR and with Strength around 2-4% of total GDR-EWSR.
- ✓ Not from deformation (angular momentum) effects.

Result on search of Hot Pygmy in ^{62}Ni

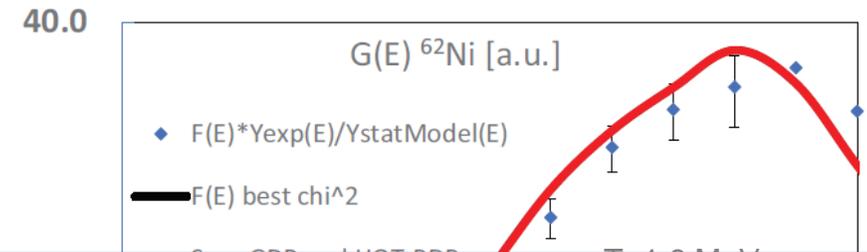


O. Wieland et al., IL NUOVO CIMENTO 47 C (2024) 24

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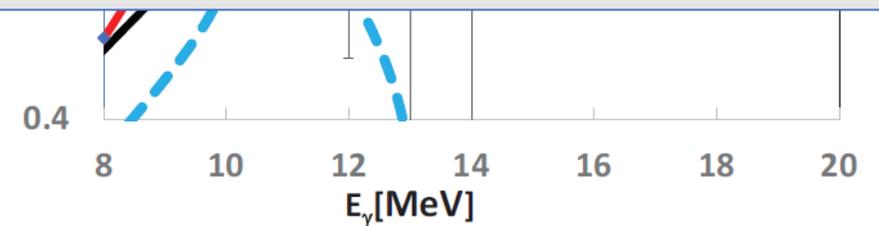
Electromagnetic transitions are sensitive towards the extreme conditions of

- Temperature
- Isospin

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Relativistic nuclear energy density functional (RNEDF)

The point-coupling RNEDF determined from the Lagrangian density

$$\begin{aligned}\mathcal{L}_{PC} = & \bar{\psi}(i\gamma \cdot \partial - m)\psi n \\ & - \frac{1}{2}\alpha_S(\rho)(\bar{\psi}\psi)(\bar{\psi}\psi) - \frac{1}{2}\alpha_V(\rho)(\bar{\psi}\gamma^\mu\psi)(\bar{\psi}\gamma_\mu\psi) \\ & - \frac{1}{2}\alpha_{TV}(\rho)(\bar{\psi}\vec{\tau}\gamma^\mu\psi)(\bar{\psi}\vec{\tau}\gamma_\mu\psi) \\ & - \frac{1}{2}\delta_S(\partial_\nu\bar{\psi}\psi)(\partial^\nu\bar{\psi}\psi) \\ & - e\bar{\psi}\gamma \cdot A\frac{1-\tau_3}{2}\psi\end{aligned}$$

- Free nucleon terms
- Isoscalar-scalar, isoscalar-vector, isovector-vector interaction terms
- Derivative term (effects of finite range interaction)
- Electromagnetic interaction

➤ By integrating the Hamiltonian density over the r-space we obtain the total energy

$$E_{RMF} = \int d^3r \mathcal{H}(r)$$

[T. Nikšić et al., Comput. Phys. Commun. 185, 1808 (2014)]
[DD-PCX: E. Yüksel et al., Phys. Rev. C 99, 034318 (2019)]

➤ **Nuclear state properties** are described within finite temperature Hartree-Bardeen-Cooper-Schrieffer (FT-HBCS) framework supplemented with pairing correlations (Separable Pairing force)

[A. L. Goodman, Nucl. Phys. A 352, 30 (1981)]

➤ **Collective excitations in Nuclei:** Relativistic Quasiparticle Random Phase Approximation (RQRPA)

HBCS+RQRPA are prominent tools for calculations.

Finite temperature calculations needs extra work!

➤ At finite temperature (FT), the occupation probabilities of single particle states are given by

$$n_i = v_i^2(1 - f_i) + u_i^2 f_i$$

➤ The T-dependent Fermi-Dirac distribution function is obtained as

$$f_i = [1 + \exp(E_i/k_B T)]^{-1}$$

Finite temperature RQRPA

- The starting point in the Equation of Motion method is definition of a suitable Excitation operator

$$\Gamma_\nu^\dagger = \sum_{a \geq b} X_{ab}^\nu a_a^\dagger a_b^\dagger - Y_{ab}^\nu a_b a_a + \underbrace{P_{ab}^\nu a_a^\dagger a_b - Q_{ab}^\nu a_b^\dagger a_a}_{\text{Red terms contribute at } T > 0}$$

two-quasiparticle creation/destruction and one-quasiparticle creation/destruction operators.

- With $|BCS\rangle$ as the approximate thermal vacuum the equation of motion can be written as

$$\langle BCS | [\delta\Gamma, H, \Gamma_\nu^\dagger] | BCS \rangle = E_\nu \langle BCS | [\delta\Gamma, \Gamma_\nu^\dagger] | BCS \rangle$$

- The FT-RQRPA equations are derived as

$$f_{a(b)} = [1 + \exp(E_{a(b)}/k_B T)]^{-1}$$

$$\tilde{A}_{abcd} = \sqrt{1 - f_a - f_b} A'_{abcd} \sqrt{1 - f_c - f_d} + (E_a + E_b) \delta_{ac} \delta_{bd}$$

$$\tilde{B}_{abcd} = \sqrt{1 - f_a - f_b} B_{abcd} \sqrt{1 - f_c - f_d}$$

$$\tilde{C}_{abcd} = \sqrt{f_b - f_a} C'_{abcd} \sqrt{f_d - f_c} + (E_a - E_b) \delta_{ac} \delta_{bd}$$

$$\tilde{D}_{abcd} = \sqrt{f_b - f_a} D_{abcd} \sqrt{f_d - f_c}$$

$$A'_{abcd} = (u_a u_b u_c u_d + v_a v_b v_c v_d) V_{abcd}^{pp} + (u_a v_b u_c v_d + v_a u_b v_c u_d) V_{a\bar{d}\bar{b}c}^{ph} - (-1)^{j_c + j_d + J} (u_a v_b v_c u_d + v_a u_b u_c v_d) V_{a\bar{c}\bar{b}\bar{d}}^{ph}$$

$$C'_{abcd} = (u_a v_b u_c v_d + v_a u_b v_c u_d) V_{a\bar{b}c\bar{d}}^{pp} + (u_a u_b u_c u_d + v_a v_b v_c v_d) V_{a\bar{d}b\bar{c}}^{ph} + (-1)^{j_c + j_d + J} (u_a u_b v_c v_d + v_a v_b u_c u_d) V_{a\bar{c}\bar{b}\bar{d}}^{ph}$$

- H. Sommermann, Ann. of Phys. 151, 163 (1983)
- E. Yüksel et al., Phys. Rev. C 96, 024303 (2017)
- A. Kaur, E. Yüksel, N. Paar, Phys. Rev. C 109, 014314 (2024)

Finite temperature RQRPA

- The FT-RQRPA equations can be combined into a single matrix

$$\begin{pmatrix} \tilde{C} & \tilde{a} & \tilde{b} & \tilde{D} \\ \tilde{a}^+ & \tilde{A} & \tilde{B} & \tilde{b}^T \\ -\tilde{b}^+ & -\tilde{B}^* & -\tilde{A}^* & -\tilde{a}^T \\ -\tilde{D}^* & -\tilde{b}^* & -\tilde{a}^* & -\tilde{C}^* \end{pmatrix} \begin{pmatrix} \tilde{P} \\ \tilde{X} \\ \tilde{Y} \\ \tilde{Q} \end{pmatrix} = \hbar\omega \begin{pmatrix} \tilde{P} \\ \tilde{X} \\ \tilde{Y} \\ \tilde{Q} \end{pmatrix}$$

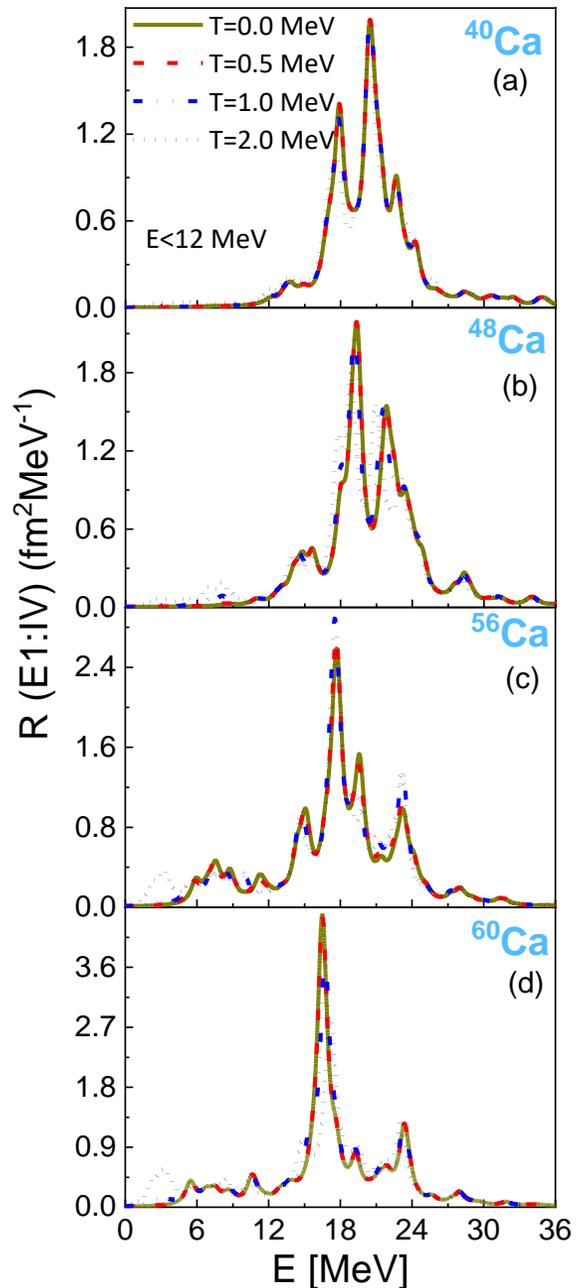
Red terms contribute at $T > 0$

*In the limit $T \rightarrow 0$
FT-RQRPA \rightarrow RQRPA*

- The reduced transition probability is

$$\begin{aligned} B(TJ) &= |\langle \omega || \hat{F}_J || \tilde{0} \rangle|^2 \\ &= \left| \sum_{c \geq d} \left\{ \begin{aligned} &(\tilde{X}_{cd}^\omega + (-1)^{j_c - j_d + J} \tilde{Y}_{cd}^\omega)(u_c v_d + (-1)^J v_c u_d) \sqrt{1 - f_c - f_d} \\ &+ (\tilde{P}_{cd}^\omega + (-1)^{j_c - j_d + J} \tilde{Q}_{cd}^\omega)(u_c u_d - (-1)^J v_c v_d) \sqrt{f_d - f_c} \end{aligned} \right\} \langle c || \hat{F}_J || d \rangle \right|^2 \end{aligned}$$

Isvector E1 response at finite temperature



Calculations are performed using DD-PCX interaction

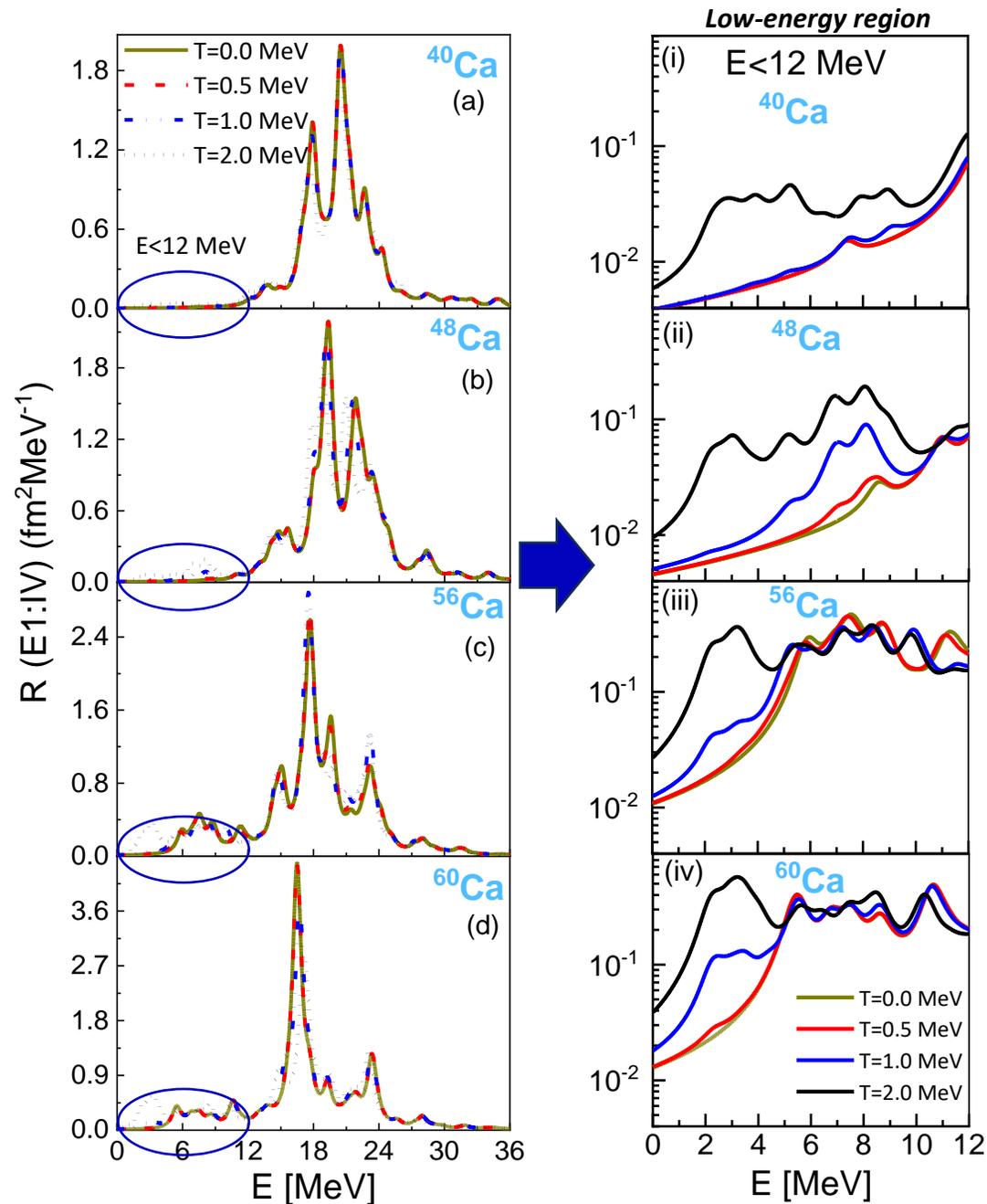
At $T=0$ MeV

- Low-energy excited states begin to emerge, as neutron number of Ca isotopes increases.

At finite temperature

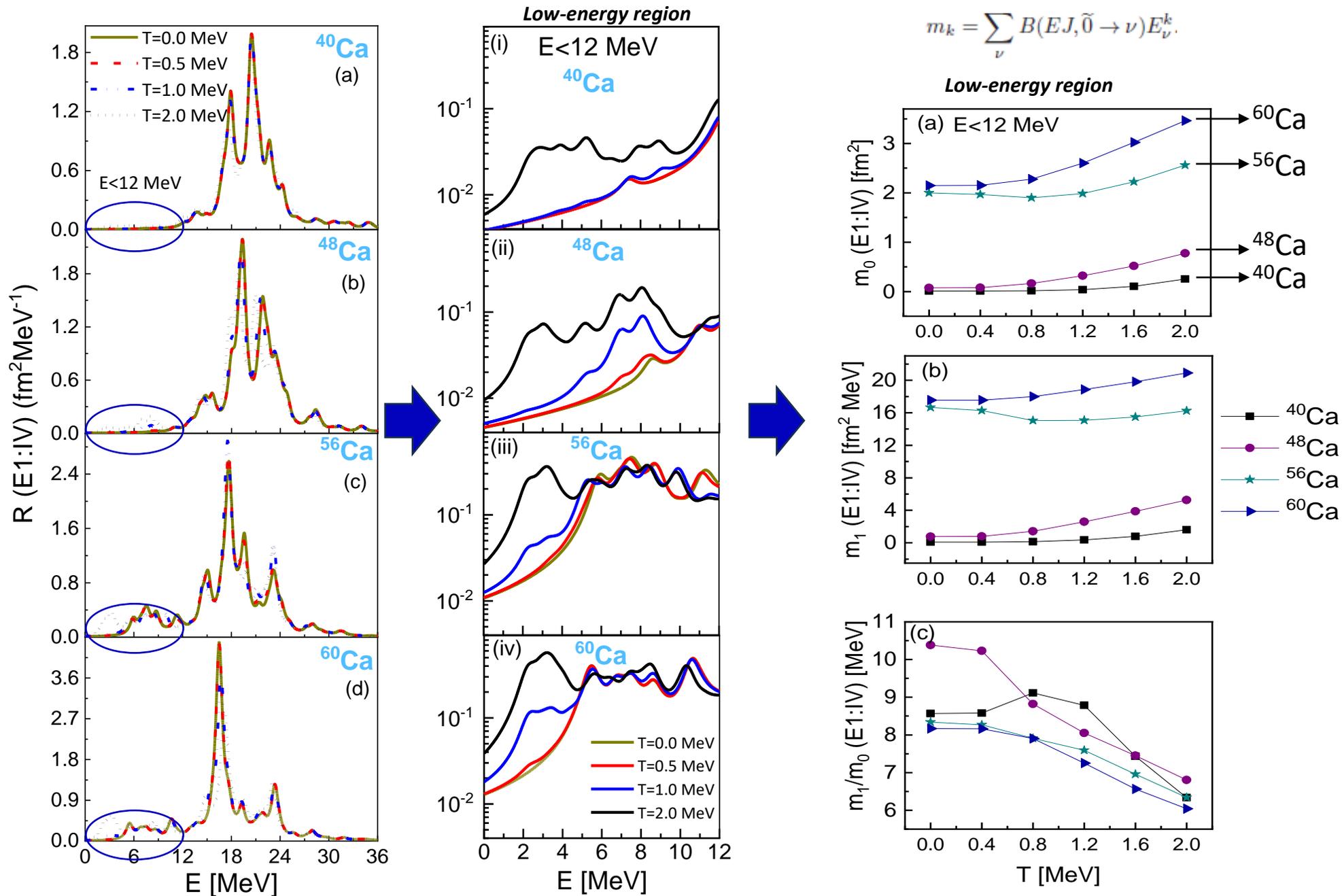
- Giant dipole resonance (GDR) region exhibits only minor changes up to $T=2$ MeV.

Isvector E1 response at finite temperature

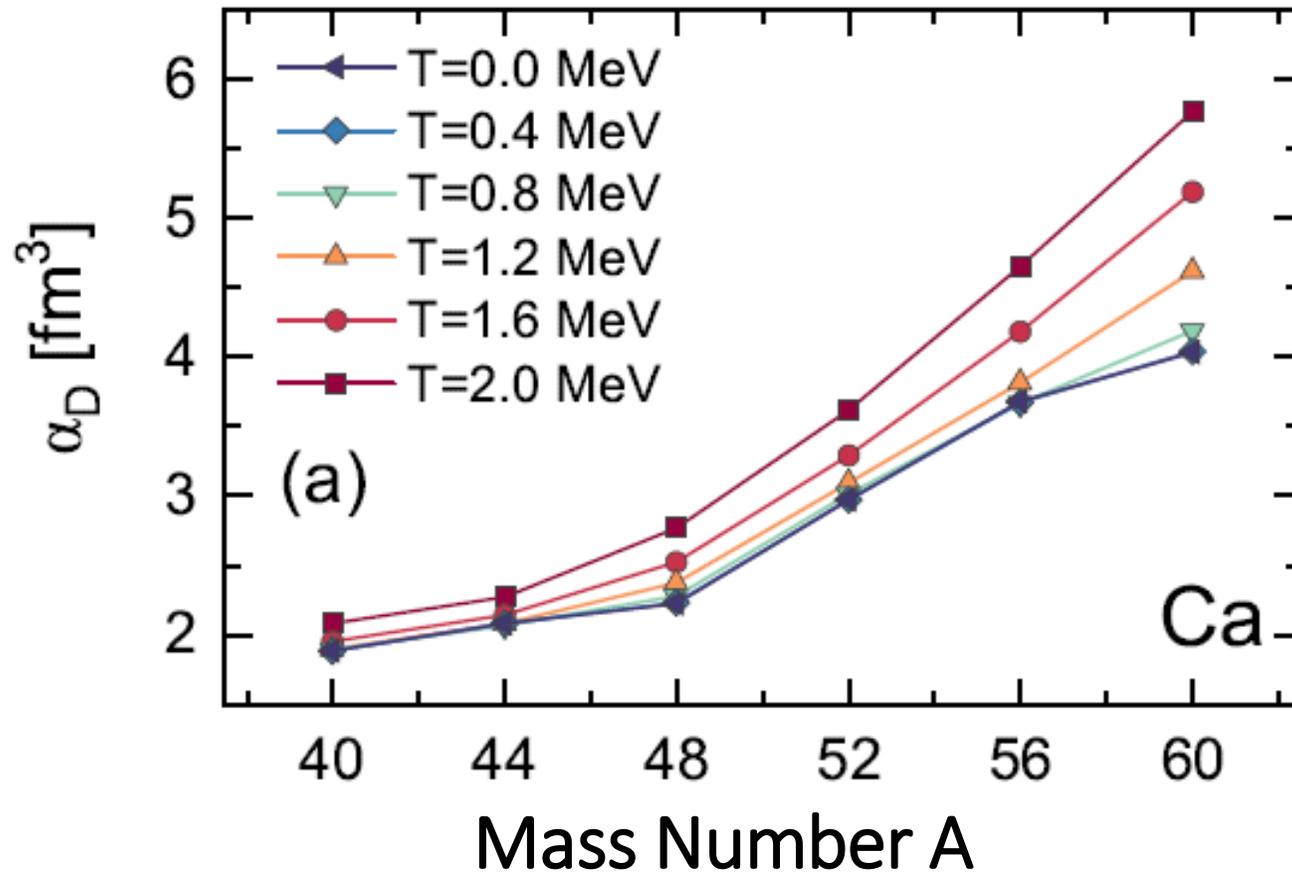


- *New low-energy excited states start to emerge below $E < 5$ MeV.*
- *At $T = 2$ MeV, its influence become more pronounced in the low-energy region of neutron-rich nuclei.*
- *Thermal unblocking effects → open new excitation channels*
- *These newly formed states at low energies are created through single quasiparticle transitions and do not exhibit collectively.*

Isvector E1 response at finite temperature



Dipole Polarizability α_D at finite temperature



- α_D is highly sensitive to the density dependence of the symmetry energy and is directly proportional to the inverse energy-weighted E1 sum rule m_{-1} .

$$\alpha_D = \frac{8\pi e^2}{9} m_{-1}(E1)$$

- In addition to the increase with the neutron excess, for all isotopes, the dipole polarizability systematically increases with temperature.

M1 response at finite temperature

- ✓ M1 excitation at the leading one-body operator would take place between the spin-orbit partner orbits.

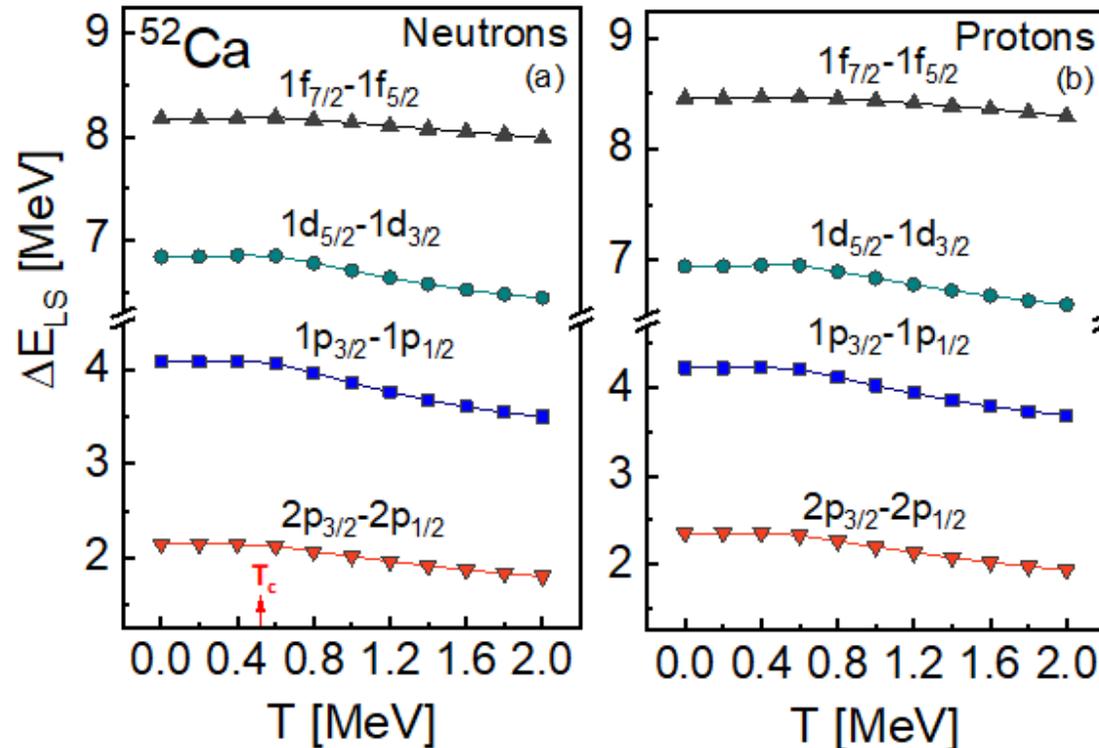
$$\hat{\mu}_v^{M1,IV} = \sqrt{\frac{3}{4\pi}} \mu_N \sum_{k \in A} [g_s^{IV} \hat{s}_v(k) + g_l^{IV} \hat{l}_v(k)] \hat{t}_0(k)$$

Nuclear spin and orbital g factors for the IV-M1 mode are
 $g_s = 4.706$ and $g_l = 0.5$

G. Kružić, T. Oishi, D. Vale, and N. Paar, Phys. Rev. C 102, 044315 (2020).

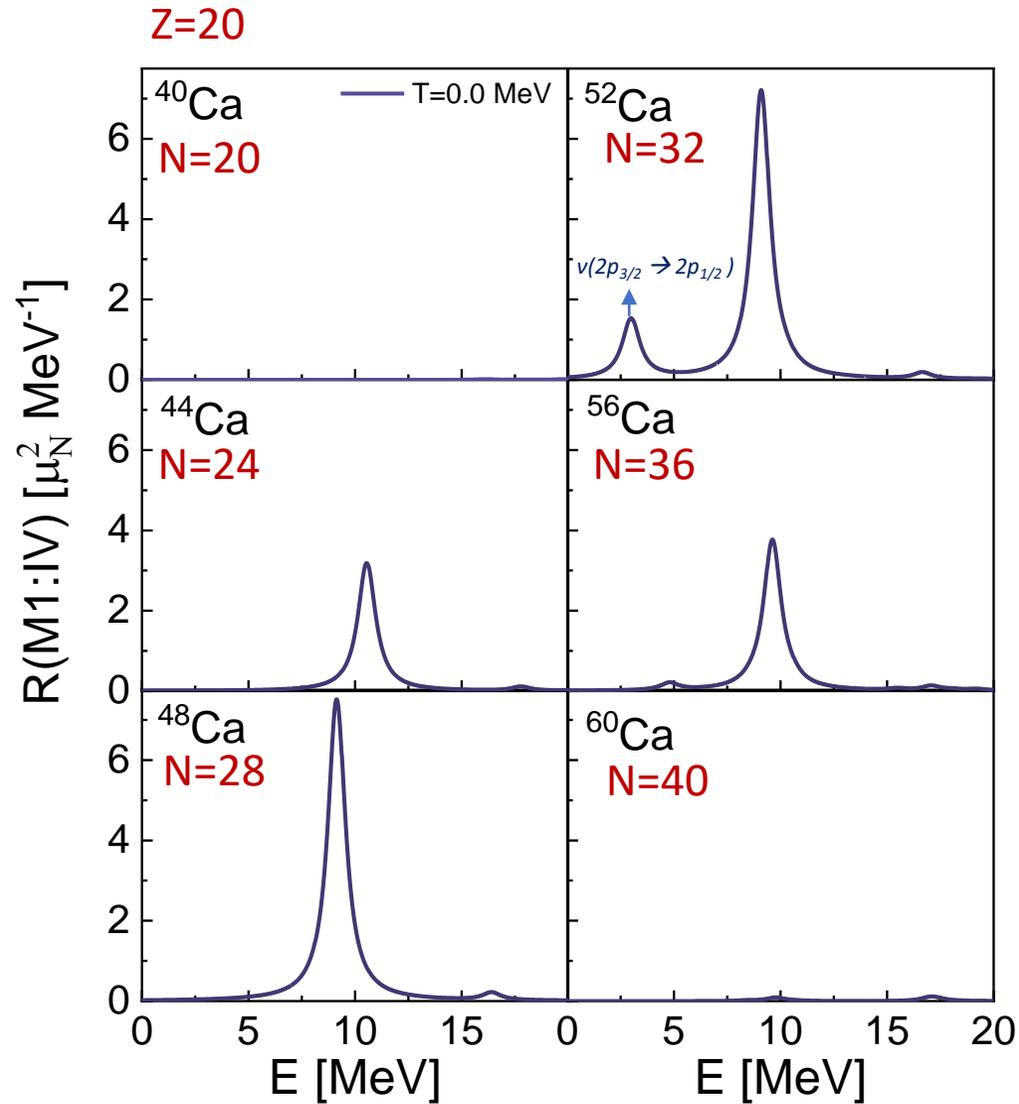
- ✓ Thus, it can provide important information on the underlying SO splittings.

Spin-orbit (SO) gap energies (ΔE_{LS})

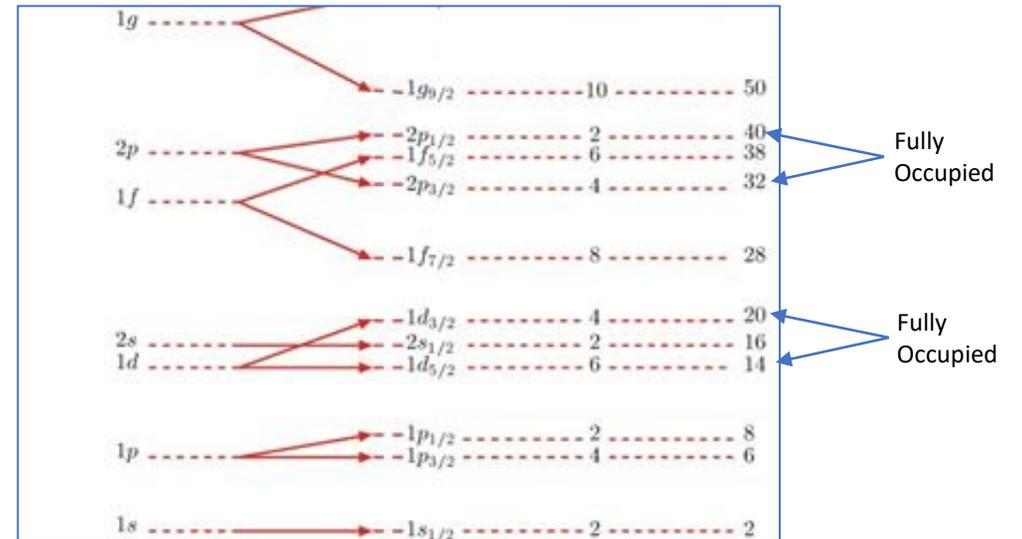


- ✓ Gap between SO partners decreases with an enhancement in T especially above T_c .
- ✓ Because the pairing force reduces rapidly with increase in temperature and collapses above T_c .
- ✓ This reduction in SO gap energies above T_c will significantly modify the M1 response.

Isovector M1 response at T=0 MeV

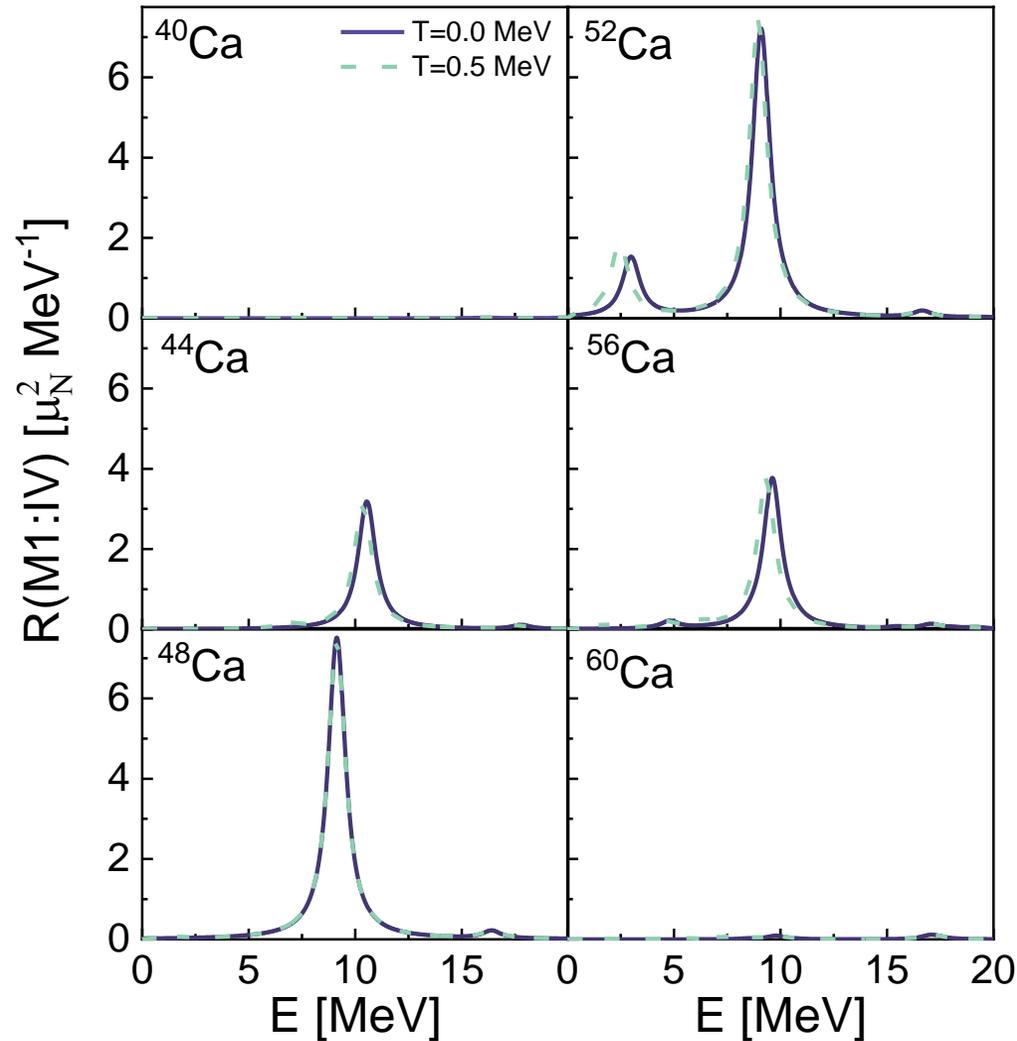


- The M1 response does not appear when the SO-partner orbits are both occupied or empty.
- M1 transitions are not present for protons due to shell closure for $Z=20$.
- For ^{40}Ca and ^{60}Ca , the nucleon numbers 20 and 40 are the “M1-silence” points.



- For $^{44-56}\text{Ca}$ nuclei, there is a strong peak in each isotope that attributes to the M1 excitation of valence neutron transitions $v(1f_{7/2} \rightarrow 1f_{5/2})$.

M1 response at finite temperature



✓ At $T=0.5$ MeV, the M1 strength does not change much.

At $T=1$ & 2 MeV

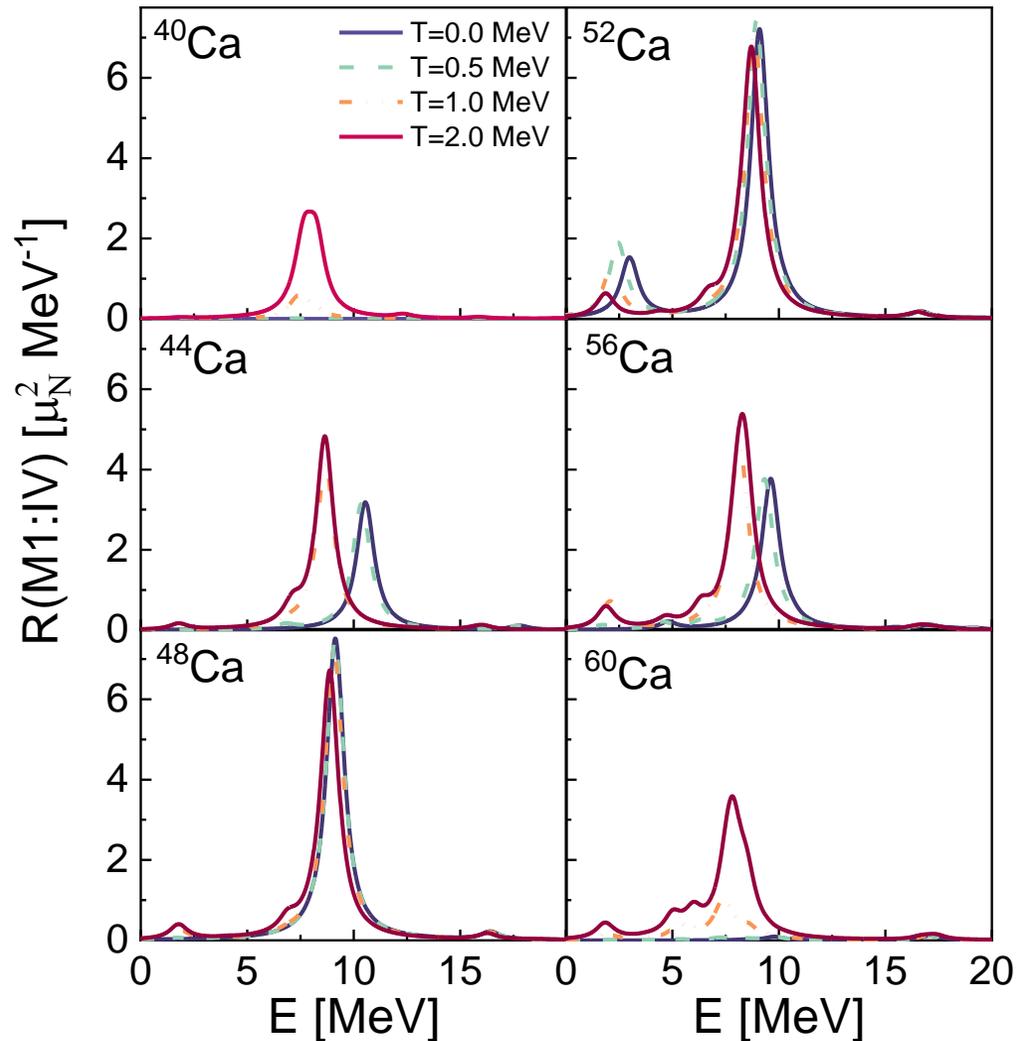
✓ Due to thermal unblocking of forbidden transitions between $(1d_{5/2} \rightarrow 1d_{3/2})$ and $(1f_{7/2} \rightarrow 1f_{5/2})$, M1 strength appears for ^{40}Ca and ^{60}Ca nuclei.

✓ Low-energy region $E < 5$ MeV:

New smaller peak arises for neutron-rich nuclei as a result of major $\nu(2p_{3/2} \rightarrow 2p_{1/2})$ transition.

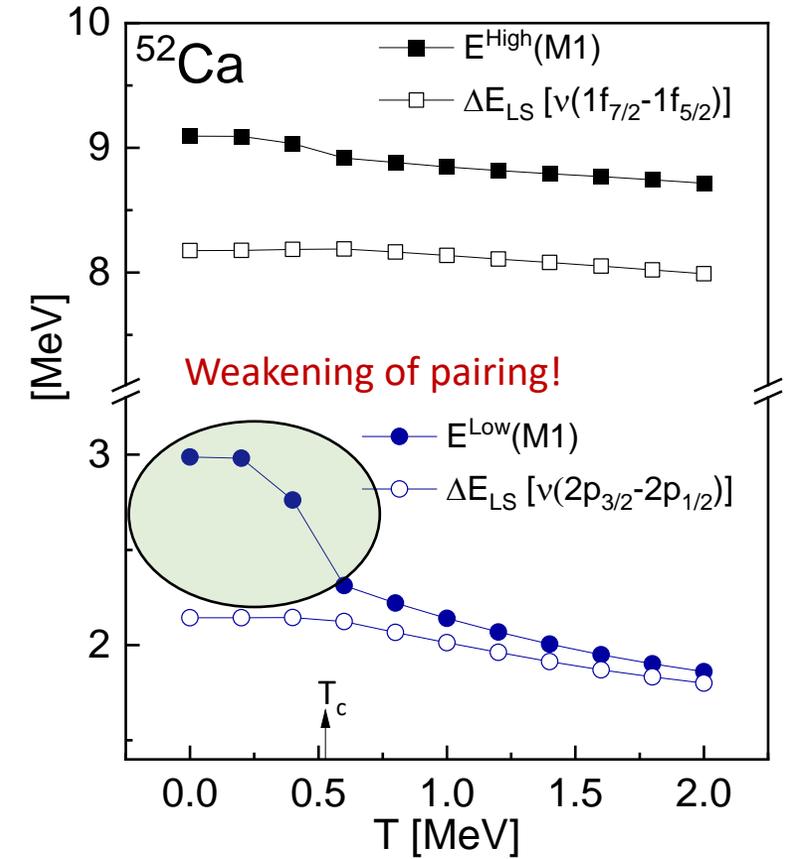
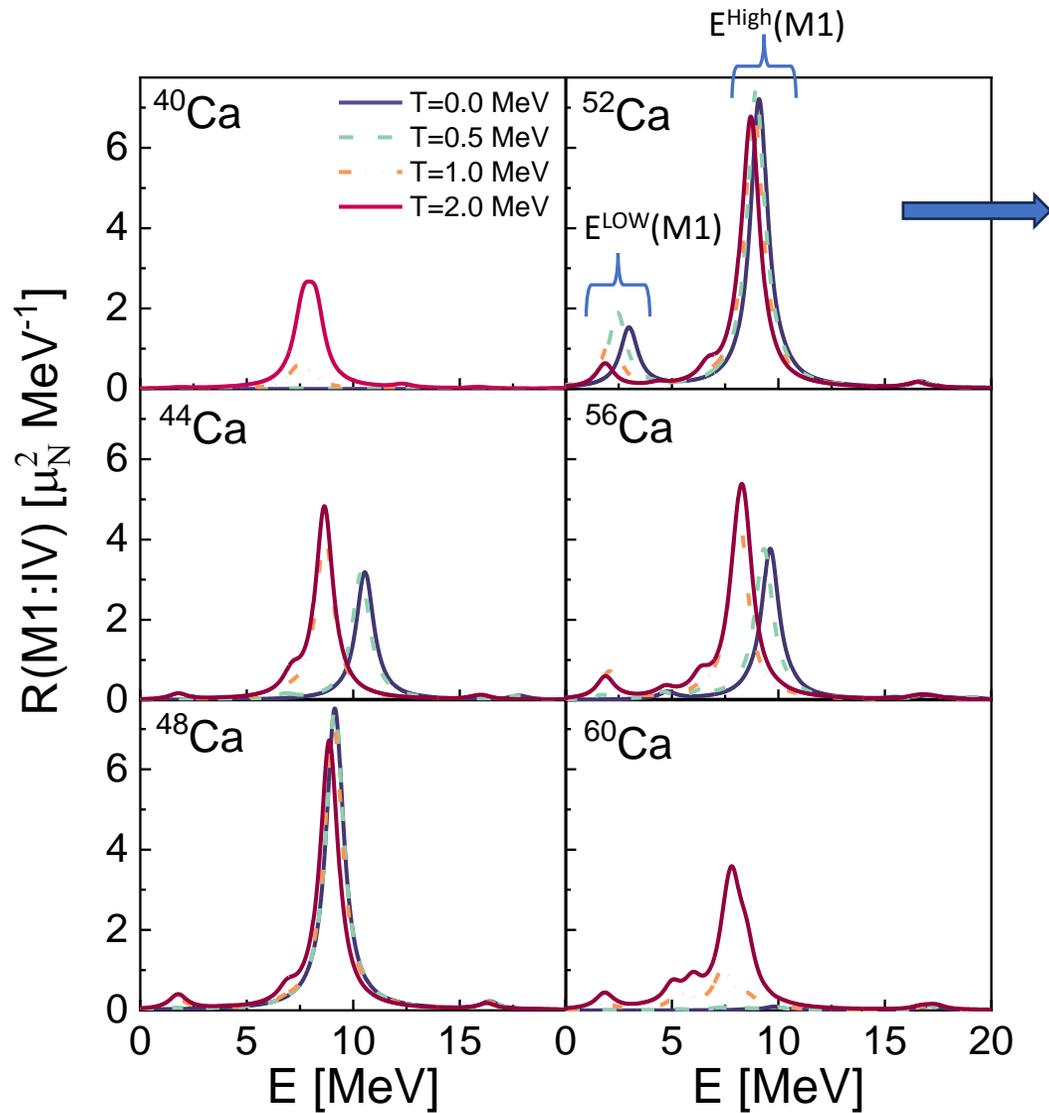
✓ M1 transitions are considerably sensitive to changes in temperature.

M1 response at finite temperature



- ✓ At $T=0.5$ MeV, the M1 strength does not change much.
- ✓ At $T=1$ & 2 MeV
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M1 response at finite temperature



- *M1 response shifts to lower energies for $^{44,48,52,56}\text{Ca}$ nuclei with increasing temperature.*

- ✓ Weakening and disappearance of pairing correlations
- ✓ Weakening of the residual interaction
- ✓ Decrement in SO splitting

Summary

A self-consistent finite temperature relativistic QRPA (FT-RQRPA) framework is developed to study the finite temperature effects on E1 and M1 transitions.

- **New excitation channels open due to thermal unblocking effects** in the low and high energy region; especially in neutron-rich nuclei.
- The GDR region of E1 response is slightly modified for the considered range of temperature; however, the M1 response exhibits a considerable dependence on temperature.
- Temperature and pairing effects play a significant role below critical temperature T_c .

Future perspectives: Possible contributions of E1 and M1 transitions at finite temperature in γ strength functions.

Acknowledgments

Collaborators:



Nils Paar

University of Zagreb, Croatia



Esra Yüksel

University of Surrey, UK



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