

# Impact of nuclear masses on the r-process nucleosynthesis

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In collaboration with G. Martínez Pinedo (GSI, Darmstadt, DE)







10th International Conference on Quarks and Nuclear Physics

July 8 – 12, 2024

Barcelona, Spain



# The Origin of the Solar System Elements

|          |   |   |          |          |          |          |          |          |          |          |  |   |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |  |  |
|----------|---|---|----------|----------|----------|----------|----------|----------|----------|----------|--|---|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|--|--|
| 1<br>H   | big bang fusion  |   |          |          |          |          |          |          |          |          | cosmic ray fission  |   |          |          |          |          |          |          |          |          | 2<br>He  |          |          |          |          |          |          |          |          |          |          |          |  |  |
| 3<br>Li  | 4<br>Be   | merging neutron stars  |          |          |          |          |          |          |          |          |  | exploding massive stars  |          |          |          |          |          |          |          |          |          | 5<br>B   | 6<br>C   | 7<br>N   | 8<br>O   | 9<br>F   | 10<br>Ne |          |          |          |          |          |  |  |
| 11<br>Na | 12<br>Mg  | dying low mass stars   |          |          |          |          |          |          |          |          |  | exploding white dwarfs   |          |          |          |          |          |          |          |          |          | 13<br>Al | 14<br>Si | 15<br>P  | 16<br>S  | 17<br>Cl | 18<br>Ar |          |          |          |          |          |  |  |
| 19<br>K  | 20<br>Ca  | 21<br>Sc  | 22<br>Ti | 23<br>V  | 24<br>Cr | 25<br>Mn | 26<br>Fe | 27<br>Co | 28<br>Ni | 29<br>Cu | 30<br>Zn   | 31<br>Ga  | 32<br>Ge | 33<br>As | 34<br>Se | 35<br>Br | 36<br>Kr |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |  |  |
| 37<br>Rb | 38<br>Sr  | 39<br>Y   | 40<br>Zr | 41<br>Nb | 42<br>Mo | 43<br>Tc | 44<br>Ru | 45<br>Rh | 46<br>Pd | 47<br>Ag | 48<br>Cd   | 49<br>In  | 50<br>Sn | 51<br>Sb | 52<br>Te | 53<br>I  | 54<br>Xe |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |  |  |
| 55<br>Cs | 56<br>Ba  | 72<br>Hf  | 73<br>Ta | 74<br>W  | 75<br>Re | 76<br>Os | 77<br>Ir | 78<br>Pt | 79<br>Au | 80<br>Hg | 81<br>Tl   | 82<br>Pb  | 83<br>Bi | 84<br>Po | 85<br>At | 86<br>Rn |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |  |  |
| 87<br>Fr | 88<br>Ra  |   |          |          |          |          |          |          |          |          |  |   |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |  |  |
|          |   |   |          |          |          |          |          |          |          |          |  |   |          |          |          |          |          | 57<br>La | 58<br>Ce | 59<br>Pr | 60<br>Nd | 61<br>Pm | 62<br>Sm | 63<br>Eu | 64<br>Gd | 65<br>Tb | 66<br>Dy | 67<br>Ho | 68<br>Er | 69<br>Tm | 70<br>Yb | 71<br>Lu |  |  |
|          |   |   |          |          |          |          |          |          |          |          |  |   |          |          |          |          |          | 89<br>Ac | 90<br>Th | 91<br>Pa | 92<br>U  |          |          |          |          |          |          |          |          |          |          |          |  |  |

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# The Origin of the Solar System Elements

merging neutron stars 

|          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
|          |          |          | 41<br>Nb | 42<br>Mo | 43<br>Tc | 44<br>Ru | 45<br>Rh | 46<br>Pd | 47<br>Ag | 48<br>Cd | 49<br>In | 50<br>Sn | 51<br>Sb | 52<br>Te | 53<br>I  | 54<br>Xe |
| 55<br>Cs | 56<br>Ba | 72<br>Hf | 73<br>Ta | 74<br>W  | 75<br>Re | 76<br>Os | 77<br>Ir | 78<br>Pt | 79<br>Au | 80<br>Hg | 81<br>Tl | 82<br>Pb | 83<br>Bi | 84<br>Po | 85<br>At | 86<br>Rn |
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|          |          | 57<br>La | 58<br>Ce | 59<br>Pr | 60<br>Nd | 61<br>Pm | 62<br>Sm | 63<br>Eu | 64<br>Gd | 65<br>Tb | 66<br>Dy | 67<br>Ho | 68<br>Er | 69<br>Tm | 70<br>Yb | 71<br>Lu |
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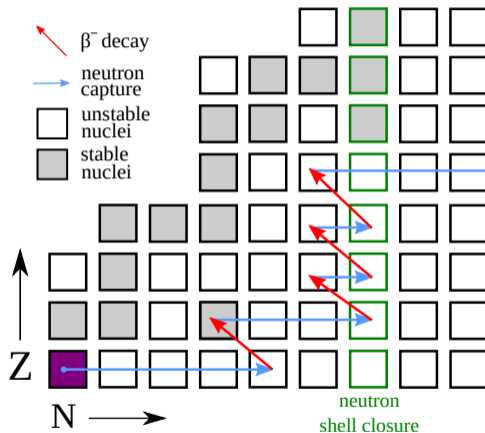
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# The $r$ process

B<sup>2</sup>FH, Rev. Mod. Phys. 29, 547 (1957) ; A. Cameron, Report CRL-41 (1957)

$$\tau_{(n,\gamma)} \ll \tau_{\beta^-}$$



$$A_{\text{final}} \approx A_{\text{initial}} + \frac{\text{neutrons}}{\text{seed}}$$

$$Y_e = \frac{n_e}{n_b}$$

- The path to heavier nuclei goes through **neutron-rich nuclei**.
- Astrophysical site with **high neutron fluxes**  $\rightarrow$  transient object (e.g., **neutron star mergers**).

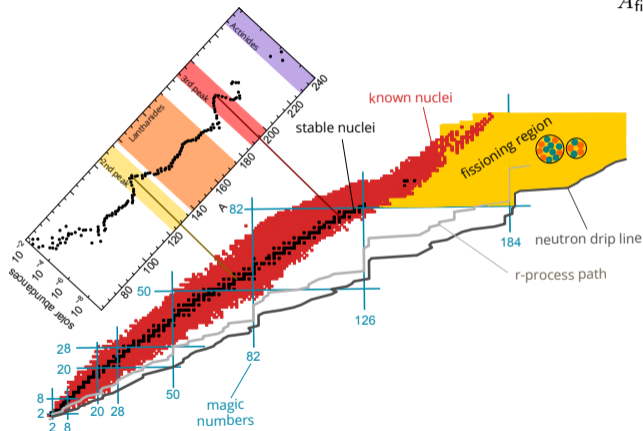
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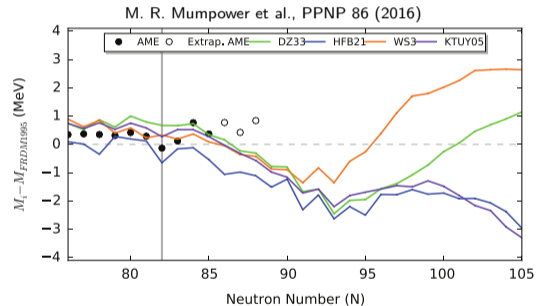
- Nuclear masses are an **essential ingredient**:
  - i) **energy budget** of  $n$  captures,  $\beta$  decays and fission;
  - ii) location of the  **$r$ -process path**;
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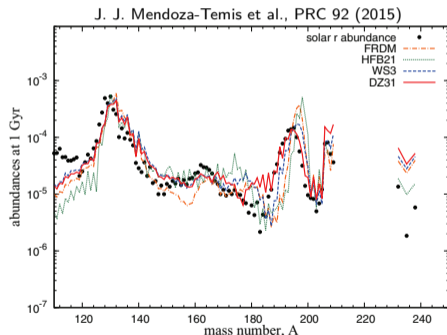
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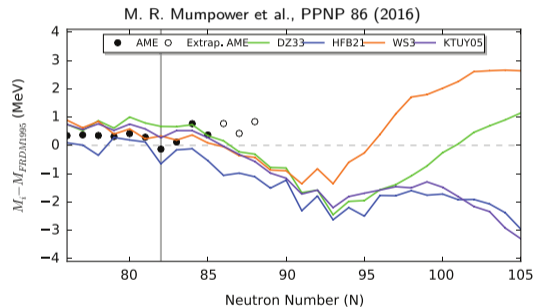
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What are the most relevant nuclear mass differences for the  $r$ -process abundances?

## Nuclear masses - Global and local contributions

Binding energies can be decomposed into **two contributions**:

$$E = E_{\text{bulk}} + E_{\text{shell}}$$

$E_{\text{bulk}}$ : **homogeneous, bulk part**. Determines the global properties, depends smoothly on  $A$ . It can be described using the liquid drop model (LDM):

$$\begin{aligned} \frac{E^{\text{LDM}}}{A} &= a_{\text{vol}} + a_{\text{sur}} A^{-1/3} + a_{\text{cur}} A^{-2/3} \\ &+ a_{\text{sym}} I^2 + a_{\text{ssym}} A^{-1/3} I^2 + a_{\text{sym}}^{(2)} I^4 \\ &+ a_{\text{Coul}} Z^2 A^{-4/3} + a_{\text{pai}} \delta \end{aligned}$$

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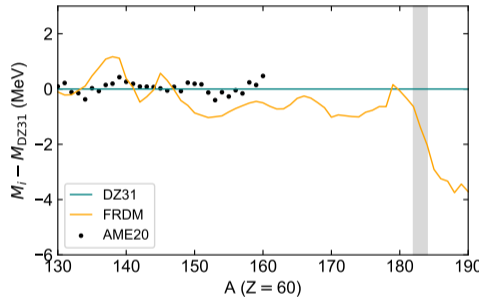
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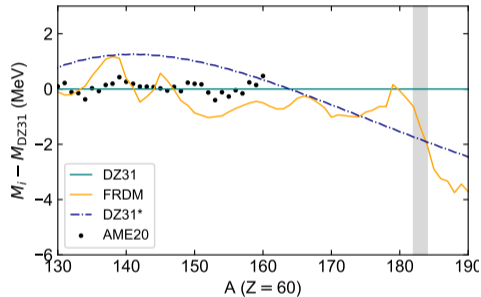
**This talk:**  $r$ -process abundances are insensitive to global changes in masses.

## Nuclear masses - Global and local changes



Starting from the DZ31 and FRDM models, we construct two new mass tables by mixing their bulk and the quantum shell parts:

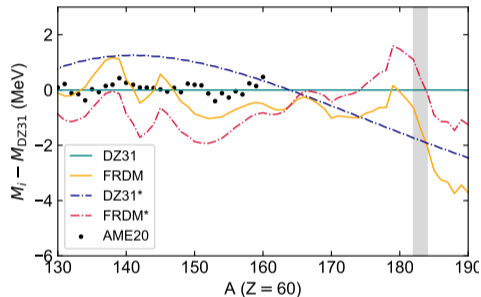
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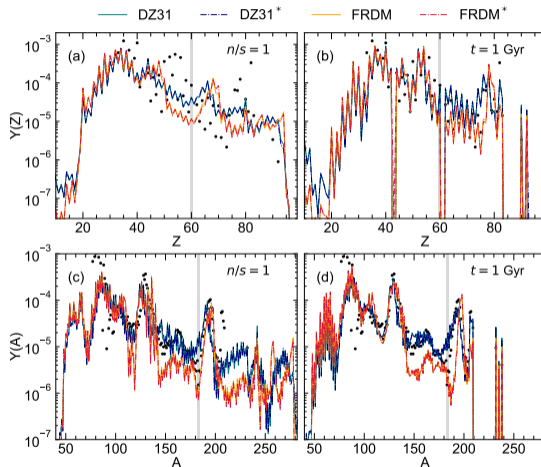
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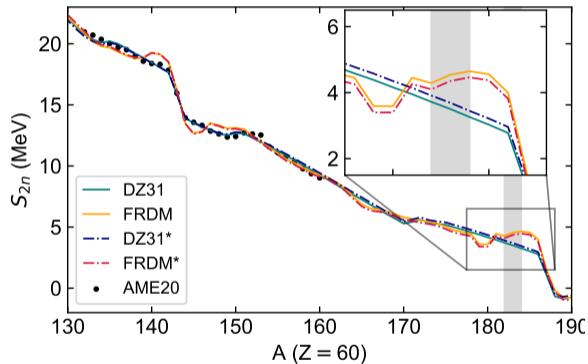
# Masses and $r$ process

~2000 NSM trajectories from Collins *et al.*, MNRAS 101093 (2023)



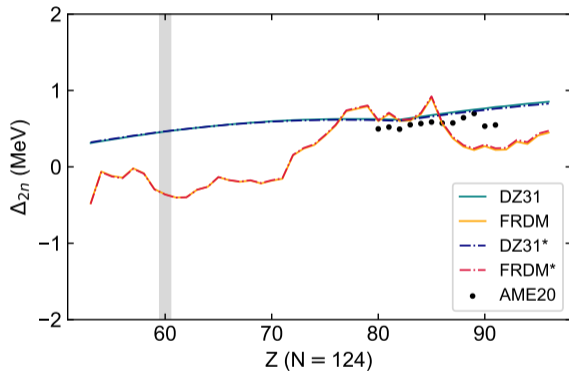
Abundances **insensitive to global changes in masses** (e.g., symmetry energy).

## Nuclear masses - Global and local changes



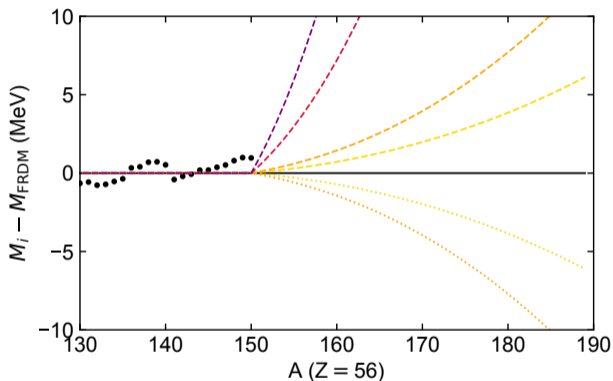
Abundance mostly related to **local changes** on  $S_{2n}$  (rather than bulk properties of masses)  $\rightarrow$   
 $\Delta_{2n}(N, Z) = S_{2n}(N, Z) - S_{2n}(N + 2, Z)$ .

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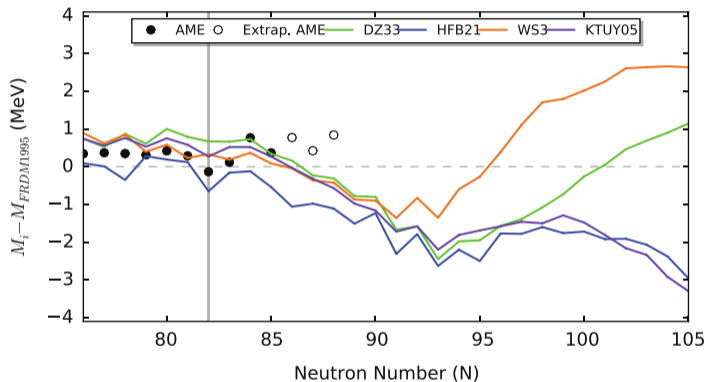
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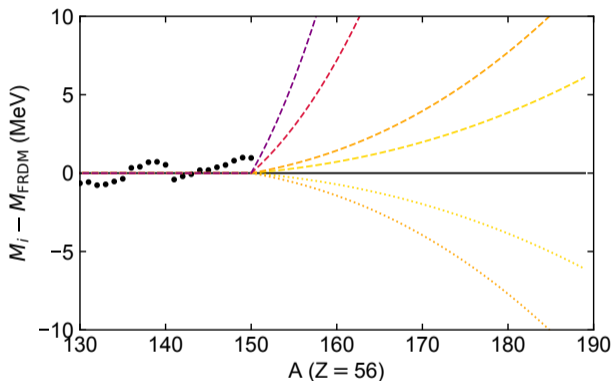
$$\frac{E^{\text{LDM}}}{A} + a_{\text{Nsym}} H(N_{\text{max}}^{\text{exp}}(Z)) I^2 \quad \text{with} \quad I = \frac{N - Z}{N + Z}$$

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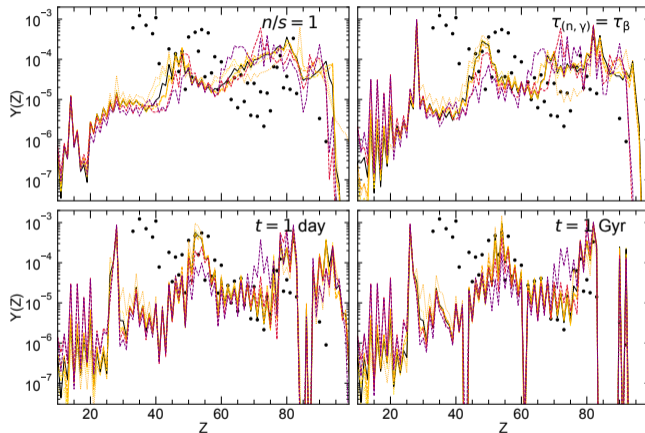
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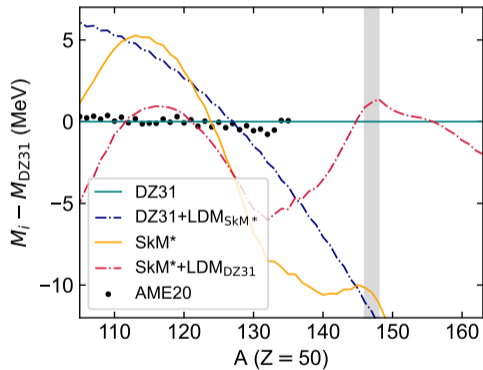
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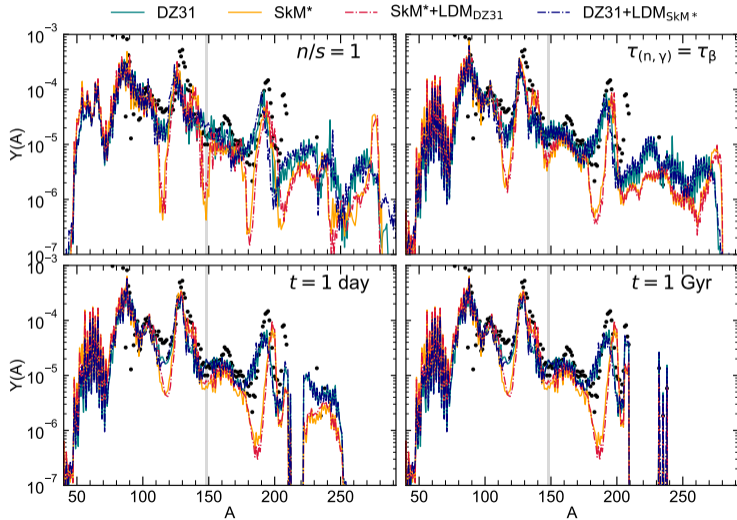
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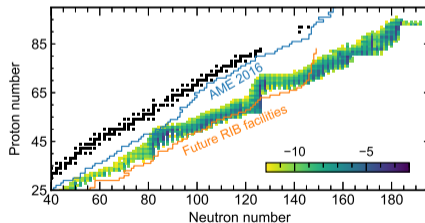


# Nuclear masses - Global and local changes



## Conclusions

- Understanding the cosmic origin of heavy elements produced by the  $r$ -process requires a detailed knowledge of nuclear properties of **neutron rich nuclei**, being nuclear masses an **essential ingredient**.
- By separating the bulk behaviour from the quantum shell-correction contribution in different mass tables, we studied the impact of **local and global changes** in mass surfaces on the  $r$ -process.
- We find that global changes on masses have little effect on final  **$r$ -process abundances**, which are mostly **determined by shell effects producing local changes in  $S_n$** . **All discrepancies are equal, but some are more equal than others.**



- This result allows to better quantify the more impactful changes on nuclear masses, providing further guidance to **future experiments**.