

# GRAVITATIONAL WAVE IMPRINT OF NON-CONVEX DYNAMICS IN BINARY NEUTRON STAR MERGER

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IN COLLABORATION WITH D.GUERRA, M.RUIZ, J.FONT  
G. Riviaccio et al. (2024) Phys. Rev. D **109**, 064032

*Ayuda CPI-23-478 financiada por CIDEAGENT/2021/046  
and Prometeo CIPROM/2022/49*

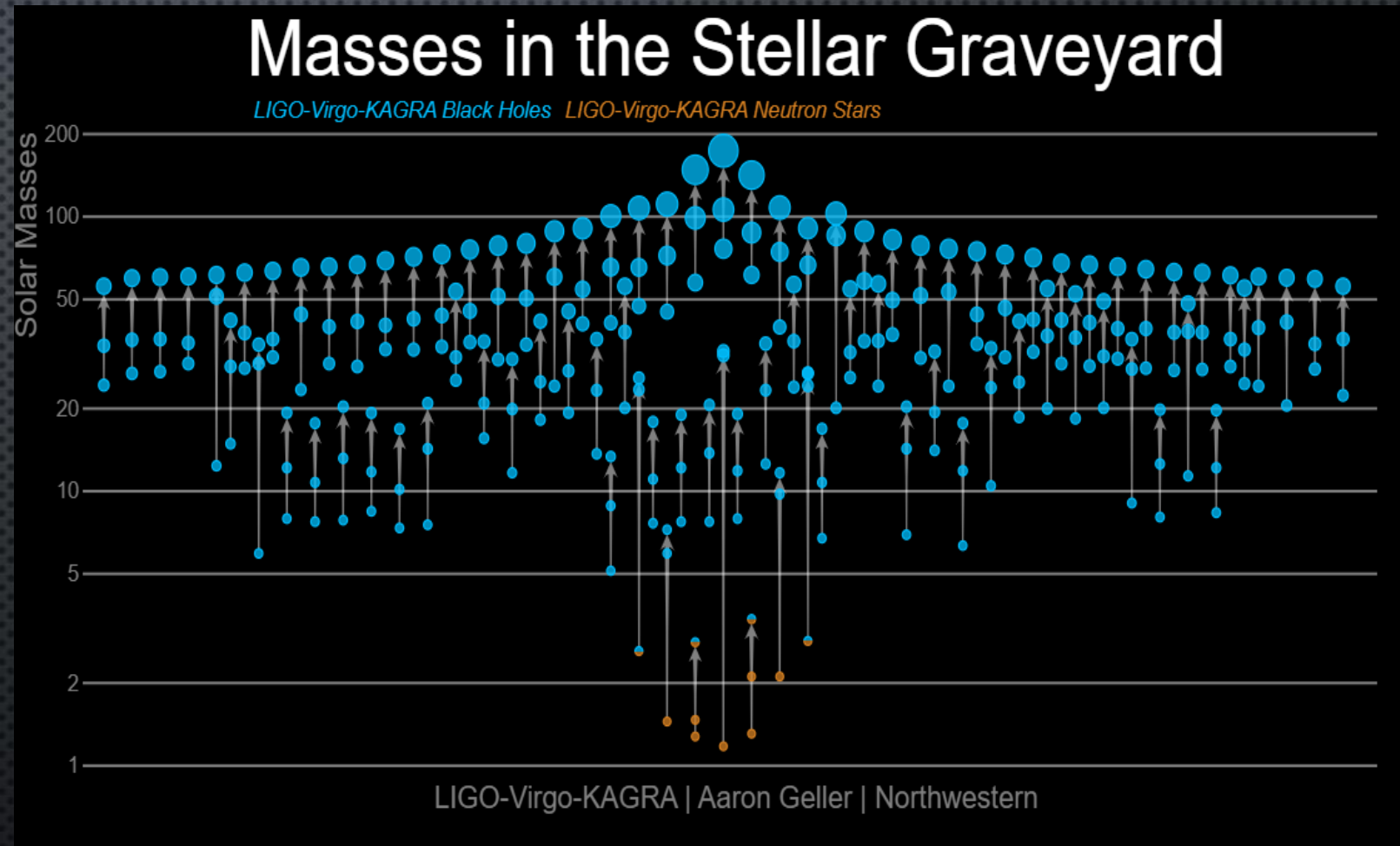
QUARK AND NUCLEAR PHYSICS CONFERENCE

BARCELONA 2024



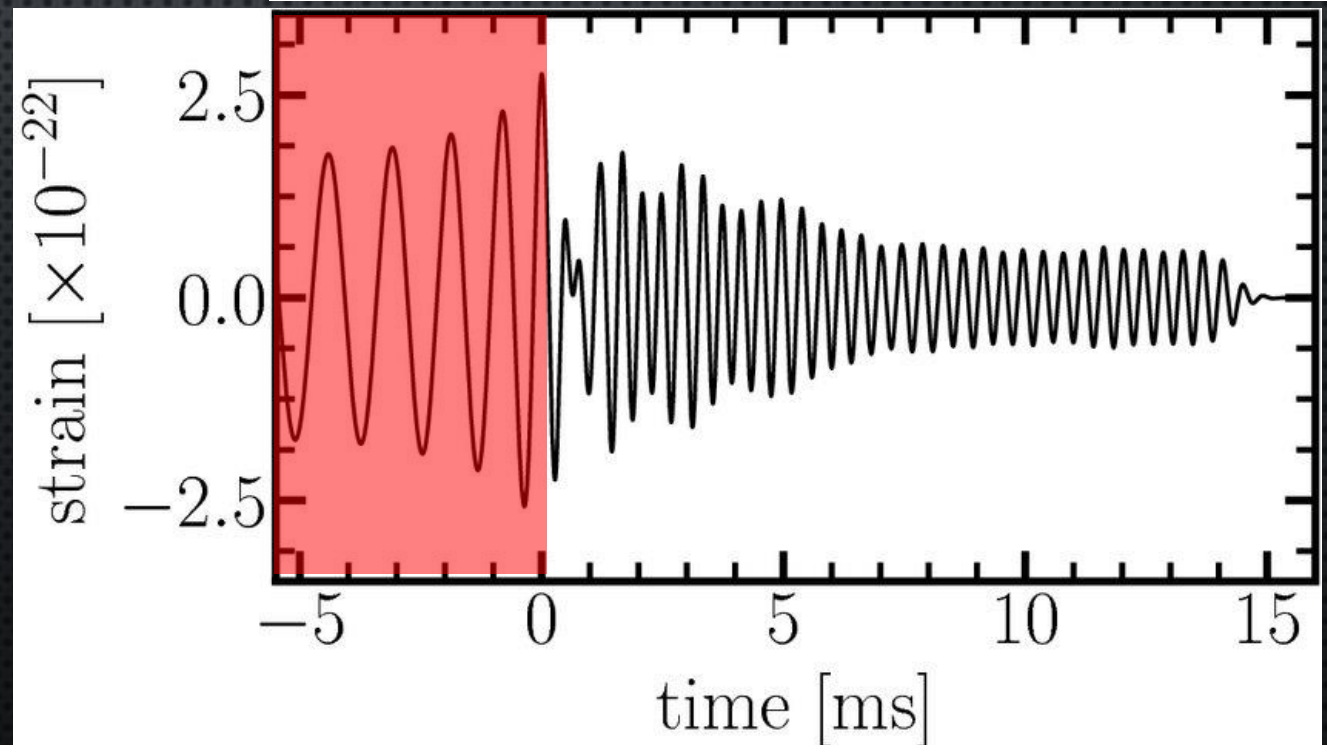
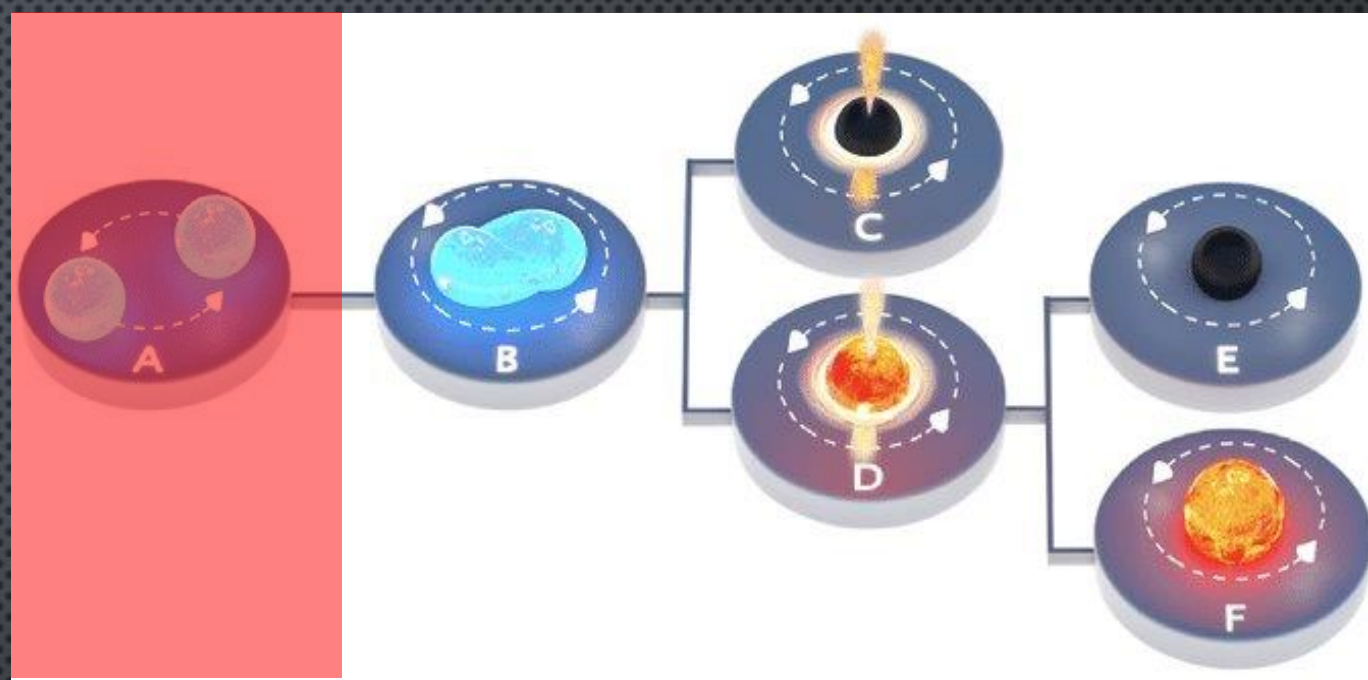
# GRAVITATIONAL WAVES

- BINARY BLACK HOLE (BBH)
- BINARY NEUTRON STAR (BNS)
  - KILONOVAE E.G. AT2017GFO
  - SHORT GAMMA RAY BURST (sGRB) 170817A
- SUPERNOVAE, PRIMORDIAL BH, ...



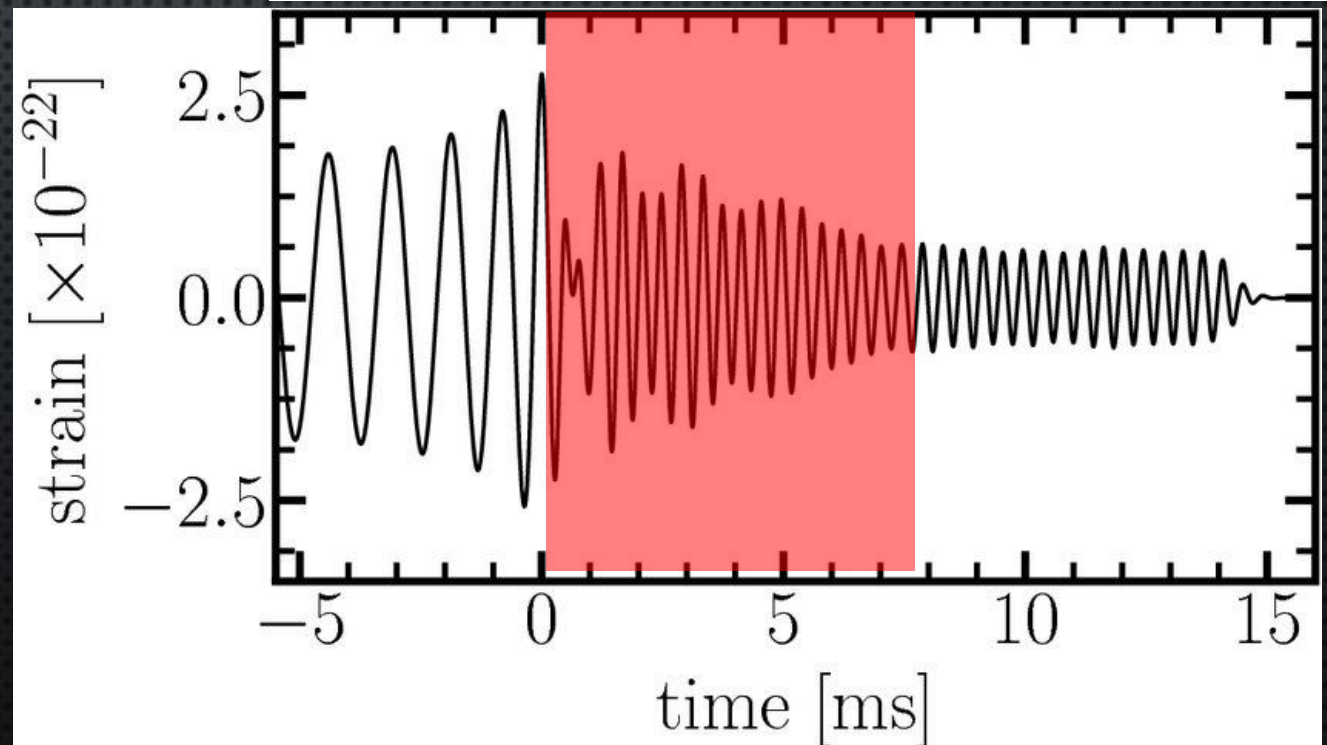
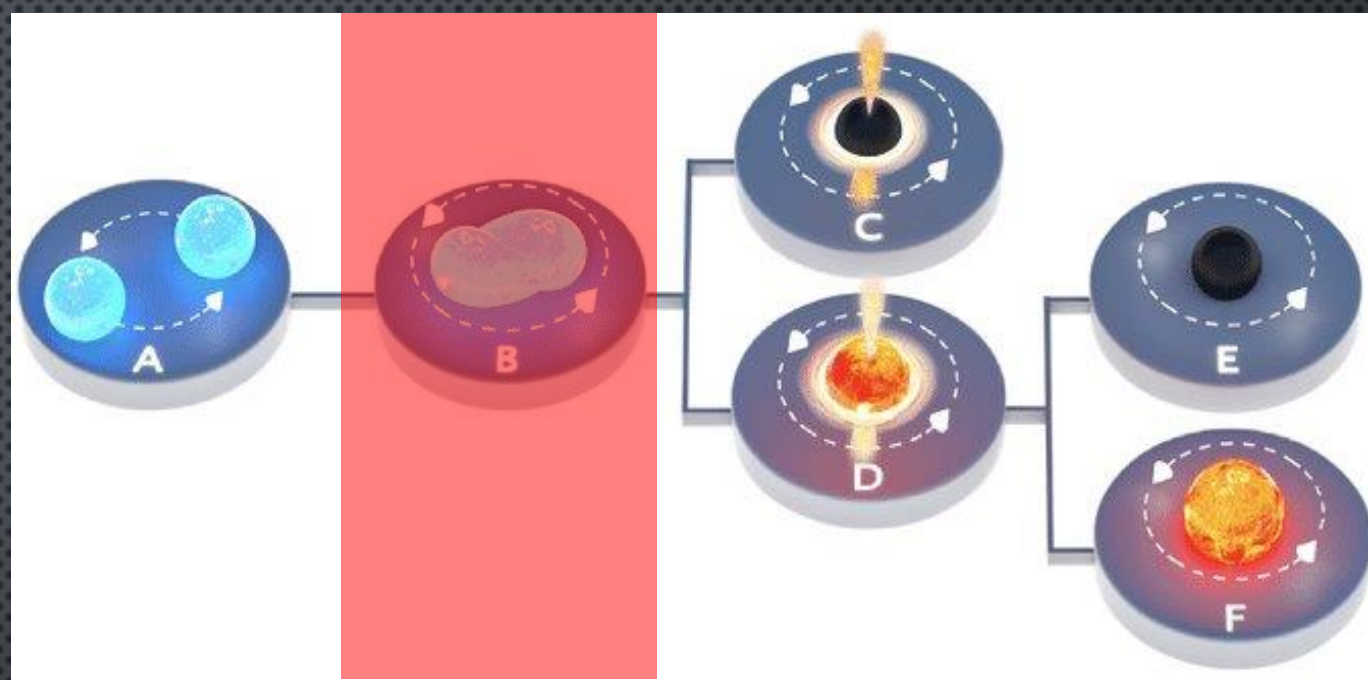
# GRAVITATIONAL WAVES

- **INSPIRAL**
- POST MERGER
- HYPERMASSIVE NS
- BLACK HOLE / SUPRAMASSIVE NS



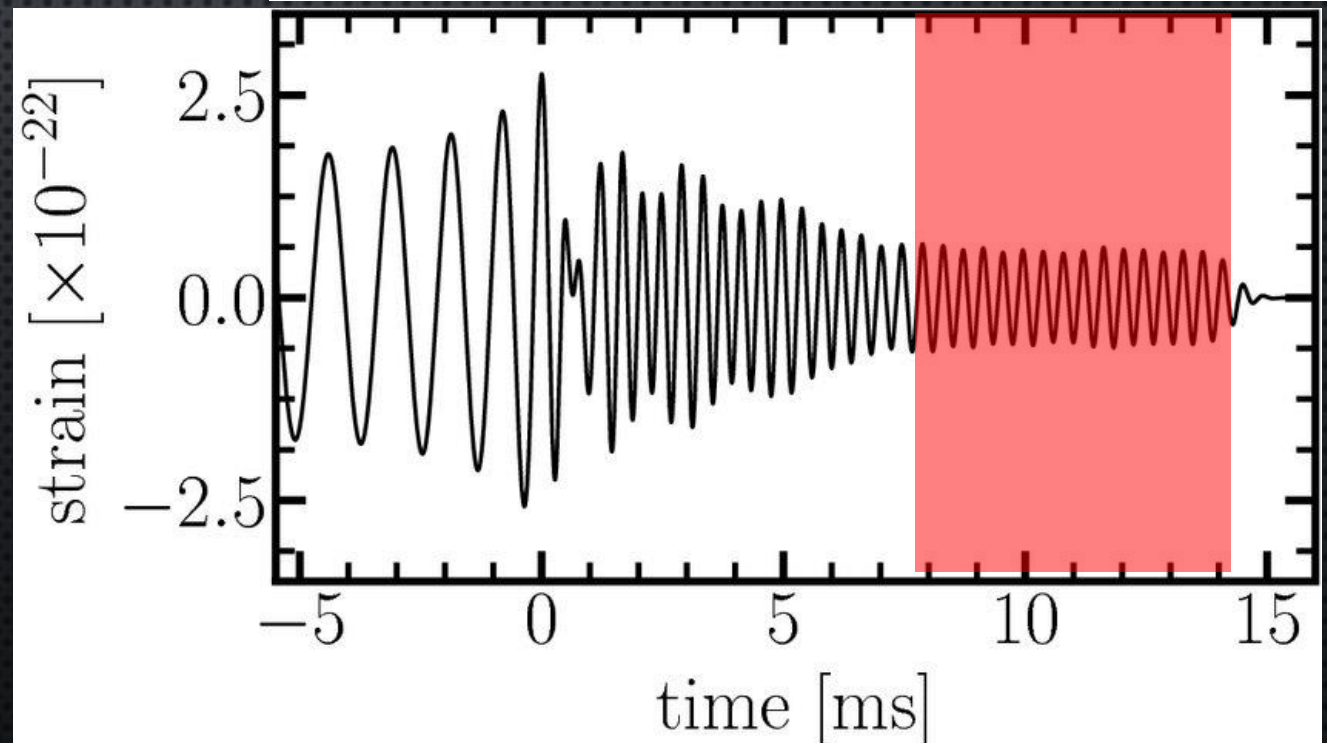
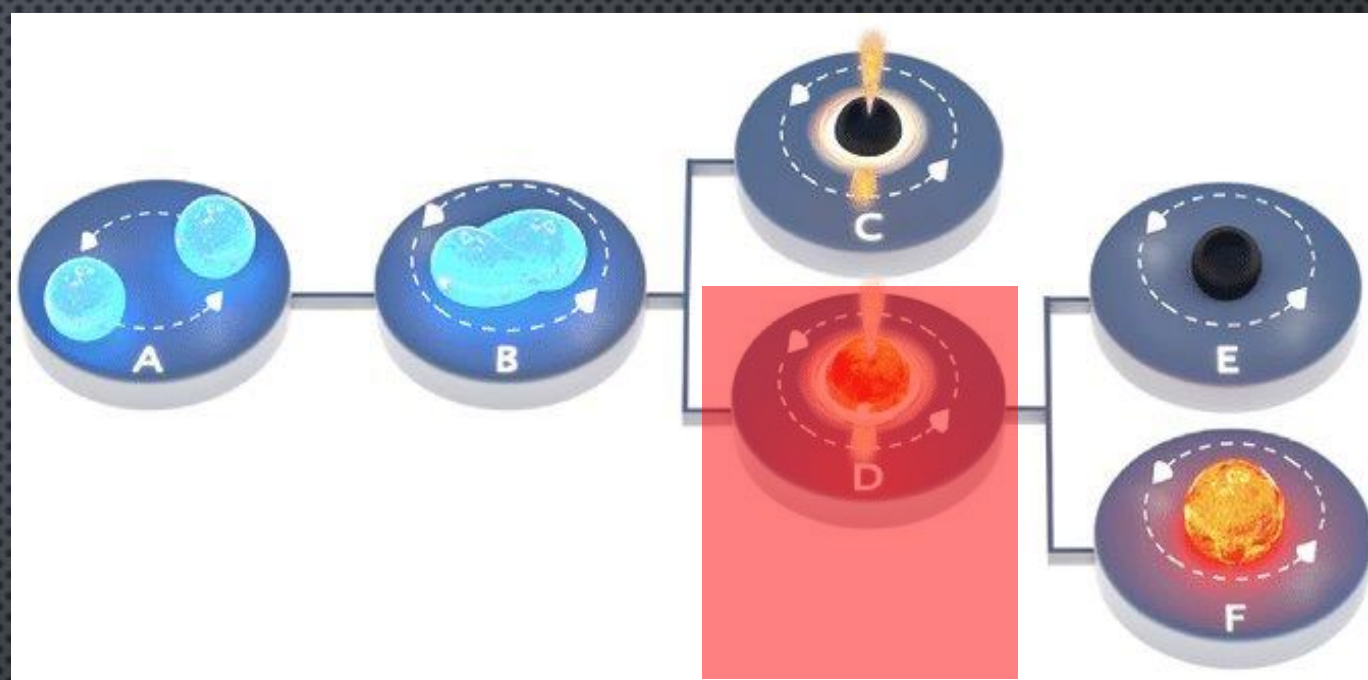
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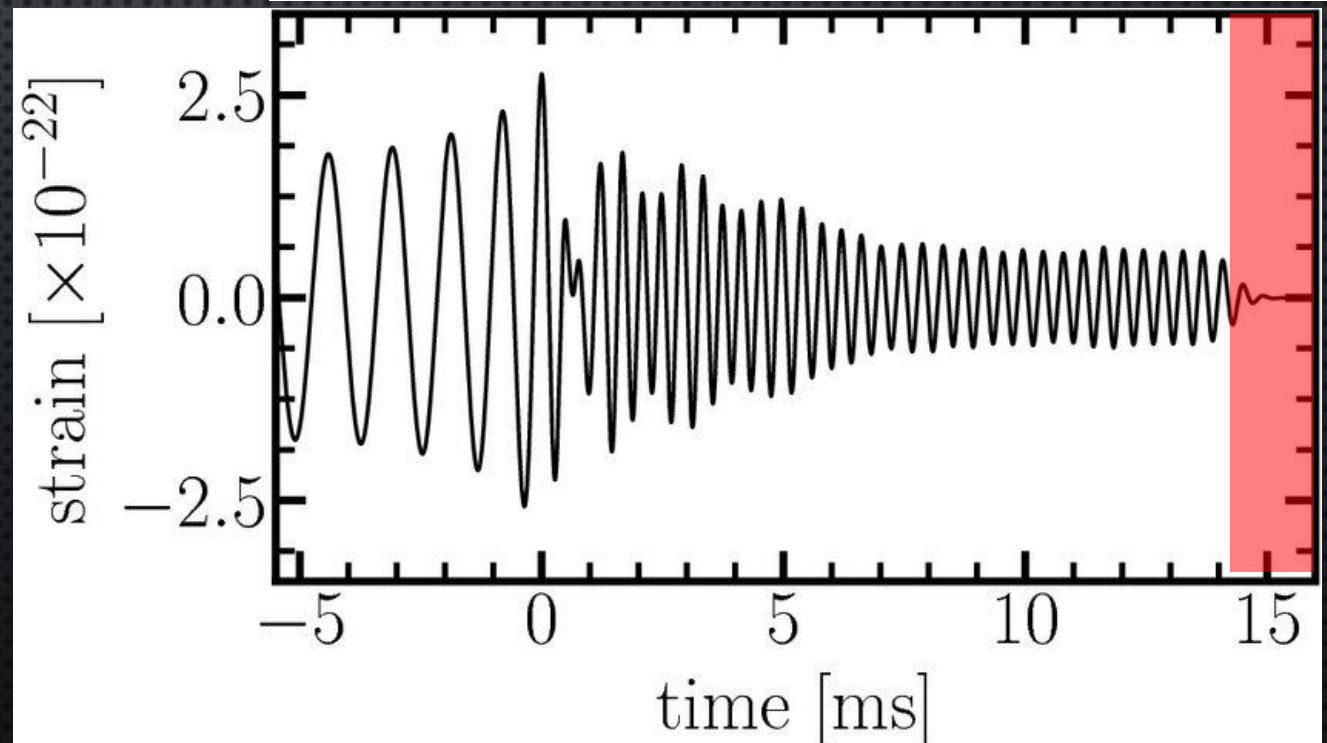
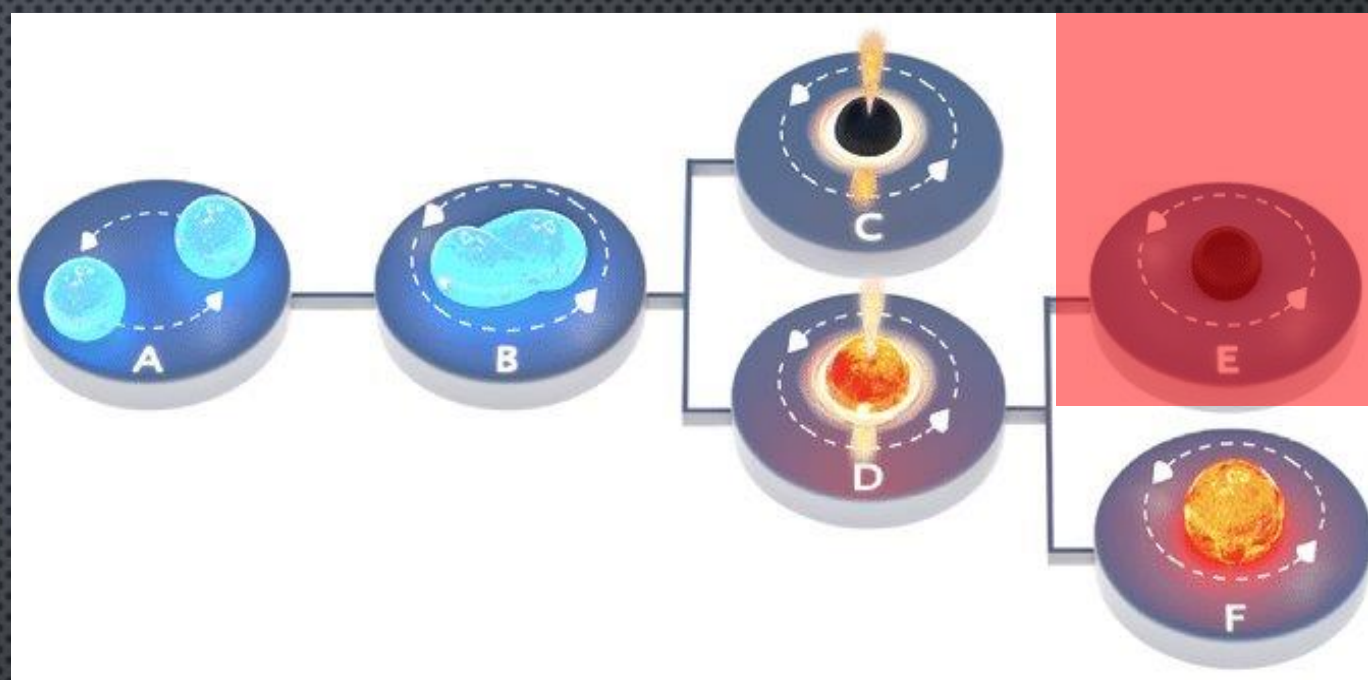
# GRAVITATIONAL WAVES

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# GRAVITATIONAL WAVES

- INSPIRAL
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# NUMERICAL SIMULATION OF BNS MERGER

CODE FOR GENERAL RELATIVISTIC  
HYDRODYNAMIC SIMULATION:

EINSTEIN TOOLKIT



[WWW.EINSTEINTOOLKIT.ORG](http://WWW.EINSTEINTOOLKIT.ORG)

Equation of State (EoS):

- Tabulated
- Piecewise Polytrope (Approximation)



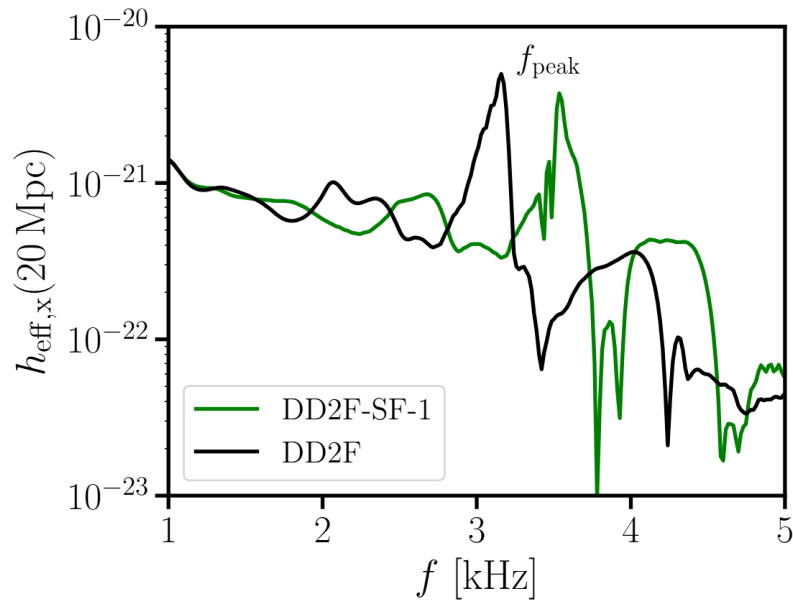
G.Riviuccio et al. 2024

**Equation of State (?)**

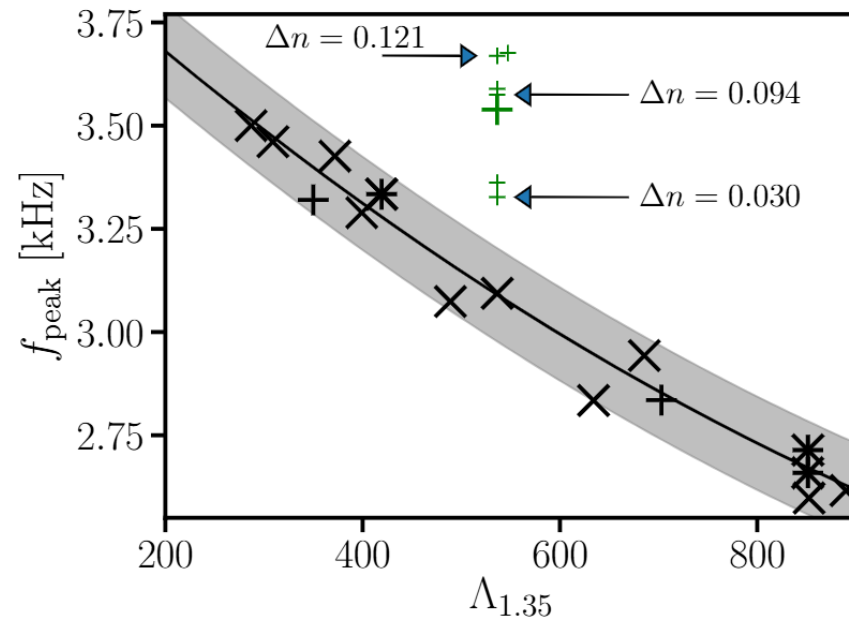
# EOS: PHASE TRANSITIONS (PT)

- FIRST ORDER PT                      OR                      CROSS-OVER
- HYPERONS                              OR                      DECONFINED QUARK MATTER (DQM)

Fourier Transformation of Gravitational Wave



Universal Relation: Tidal deformability vs Freq. peak



First order PT to DQM

Nucleonic EoS



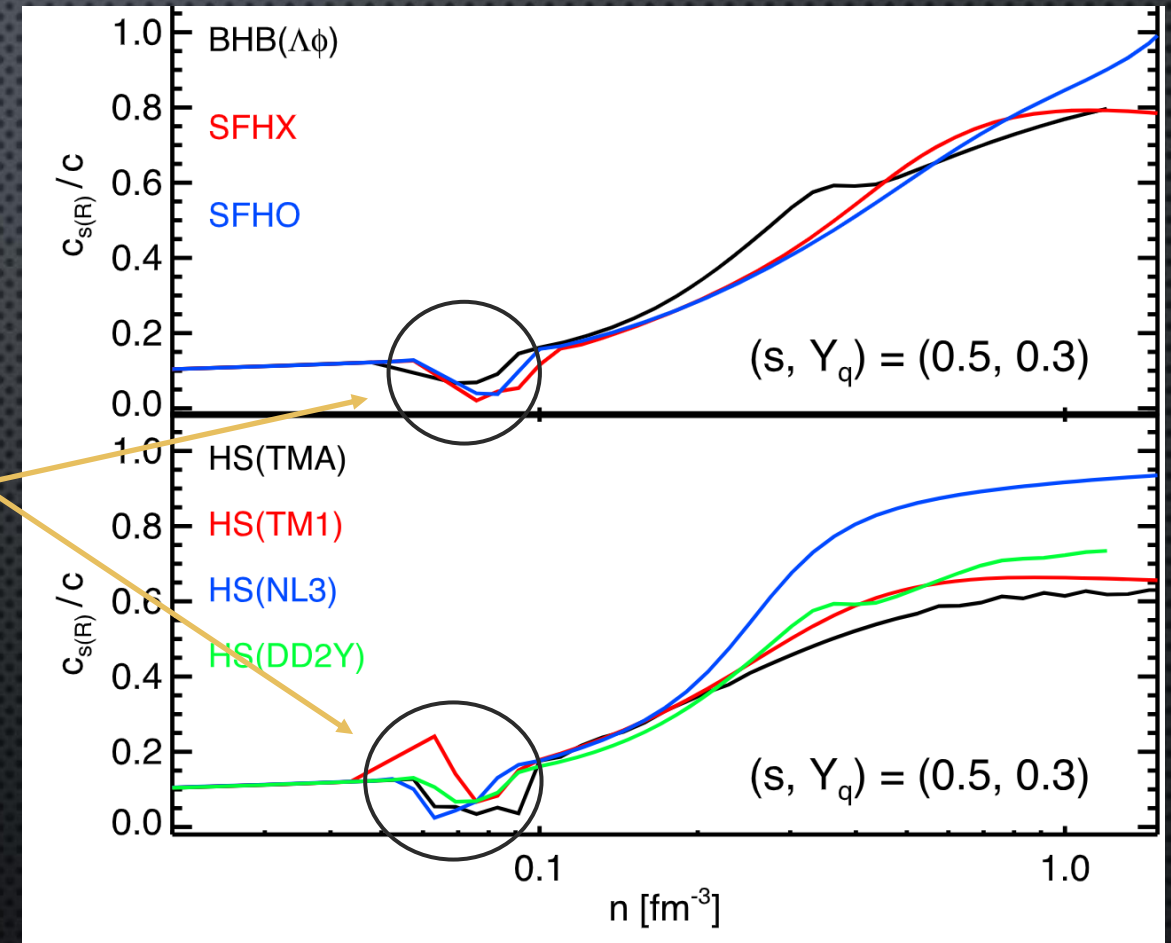
# EOS: ANOMALOUS DYNAMICS IN PHASE TRANSITION

- SOUND SPEED  $c_s^2 = \left. \frac{\partial P}{\partial \rho} \right|_S$

Non-Monotonic

- Phase Transition are in general **Non-Convex**

R Menikoff and B. Plohr Rev. Mod. Phys. 61, 75



# EOS: CONVEXITY

FUNDAMENTAL DERIVATIVE  $G = 1 + \left. \frac{\partial \ln c_s^2}{\partial \ln \rho} \right|_S$

• MATERIAL IN EQUILIBRIUM  $\Rightarrow$  METASTABLE STATE

• SHOCKS  $\Rightarrow$  LOSS OF CONVEXITY  $\Rightarrow$  PHASE TRANSITION

$$G < 0 \Rightarrow \text{Non-convex}$$



**What is the contribution of Non-Convexity?**

# EOS: GGL MODEL

- PIECEWISE POLYTROPE:

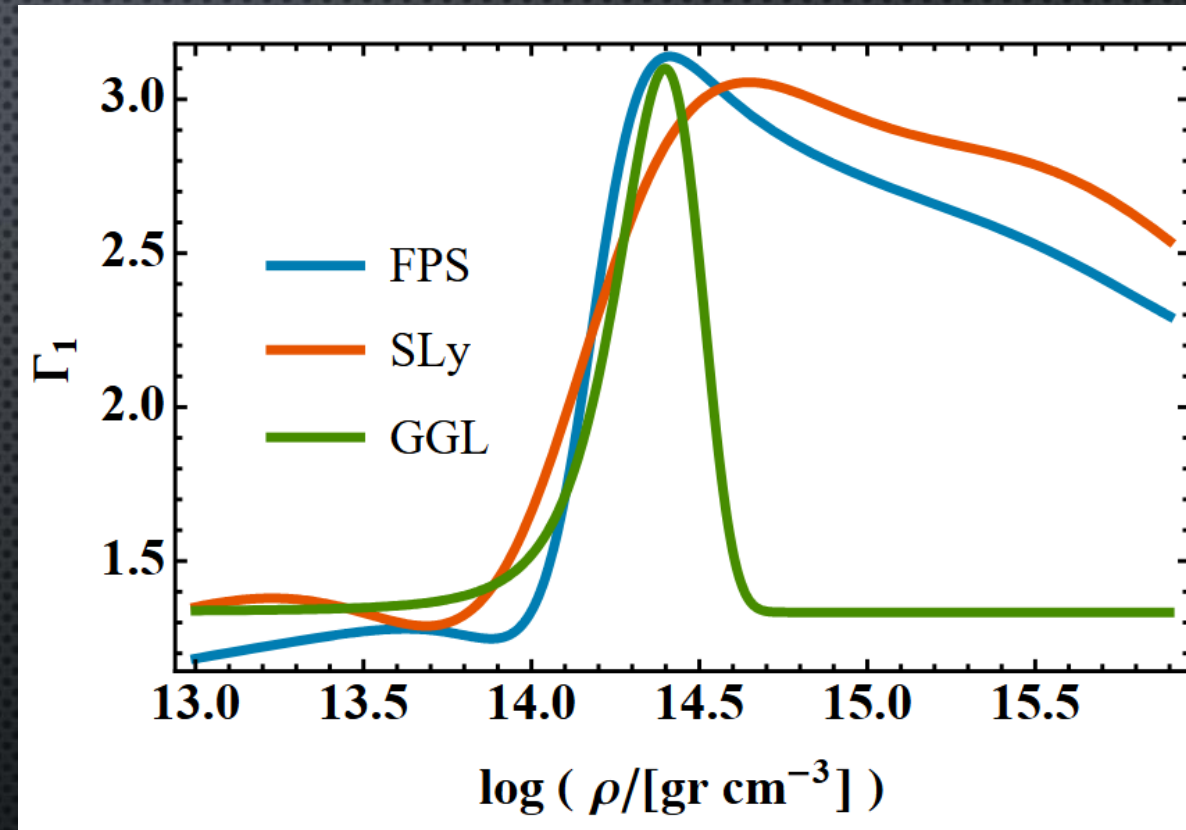
$$P_{th} = (\Gamma - 1)\epsilon_{th}n$$

- TYPICALLY  $\Gamma = 1.8$  **CONSTANT!**

- Gaussian Gamma Law EoS:

- $\Gamma(\rho) = \Gamma_0 + (\Gamma_1 - \Gamma_0)e^{-\frac{(\rho - \rho_1)^2}{\Sigma^2}}$

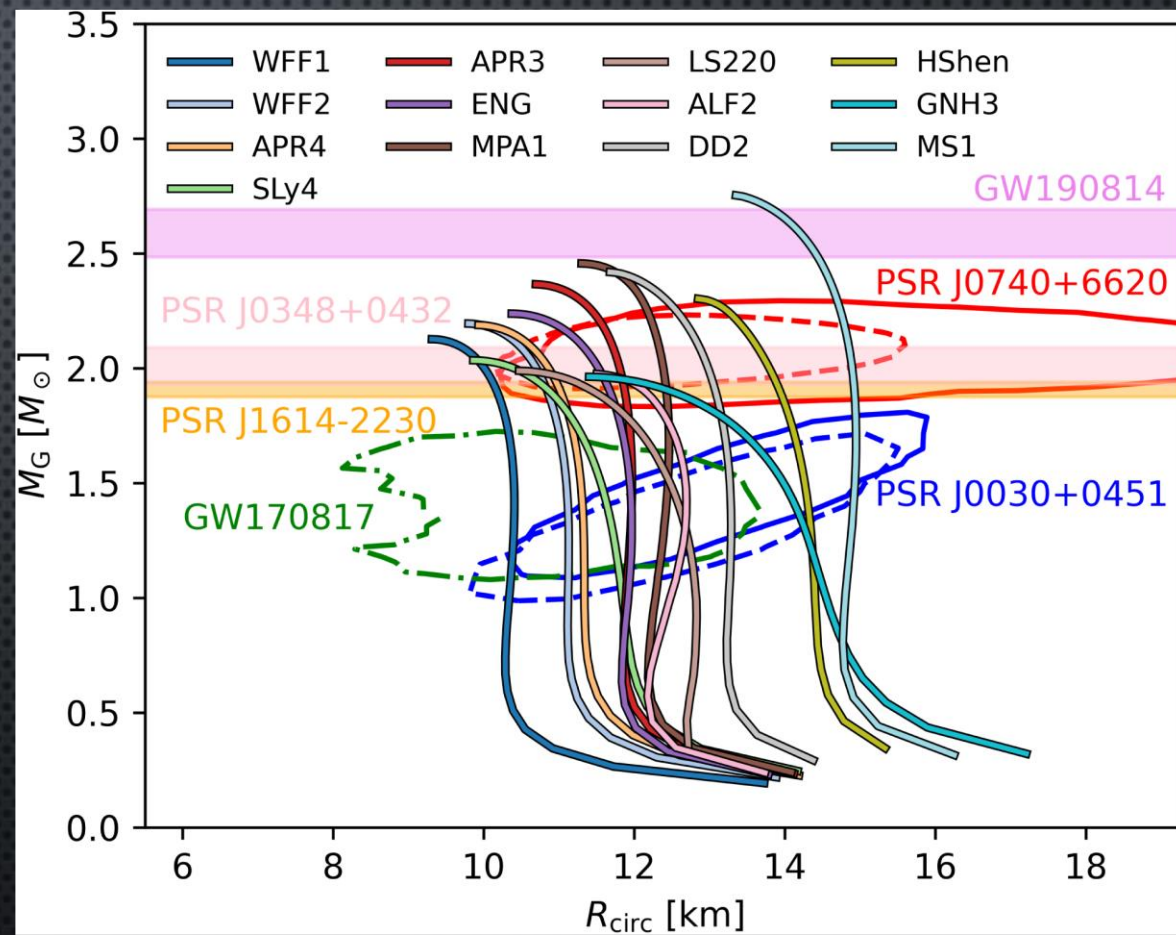
- $\Gamma_0 = 1.8$



M. A. Aloy et al. (2018)

# EOS: INITIAL DATA

EOS	$M$	$\mathcal{C}$	$\Lambda$	$M_{\text{ADM}}$	$J_{\text{ADM}}$	$\Omega$	$\rho_{0,\text{max}}$
WFF1	1.26	0.18	406.07	2.50	6.45	1.76	$10^{15.01}$
WFF2	1.27	0.17	1115.06	2.52	6.54	1.76	$10^{14.90}$
APR4	1.28	0.17	440.75	2.52	6.56	1.77	$10^{14.93}$
SLy4	1.28	0.16	511.70	2.54	6.62	1.77	$10^{14.93}$
APR3	1.28	0.16	620.00	2.53	6.61	1.77	$10^{14.86}$
ENG	1.28	0.16	636.35	2.53	6.60	1.77	$10^{14.87}$
MPA1	1.28	0.15	784.52	2.54	6.64	1.77	$10^{14.81}$
LS220	1.29	0.15	899.05	2.55	6.69	1.77	$10^{14.84}$
ALF2	1.29	0.15	941.42	2.54	6.66	1.77	$10^{14.79}$
DD2	1.29	0.13	1113.92	2.56	6.73	1.78	$10^{14.76}$
HShen	1.30	0.14	1633.24	2.58	6.82	1.78	$10^{14.69}$
GNH3	1.30	0.13	1371.15	2.58	6.81	1.78	$10^{14.77}$
MS1	1.30	0.13	2020.75	2.58	6.83	1.79	$10^{14.63}$



# EVOLUTION

CODE FOR GENERAL RELATIVISTIC  
HYDRODYNAMIC SIMULATION:

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[WWW.EINSTEINTOOLKIT.ORG](http://WWW.EINSTEINTOOLKIT.ORG)



COLD PIECEWISE POLITROPE

+

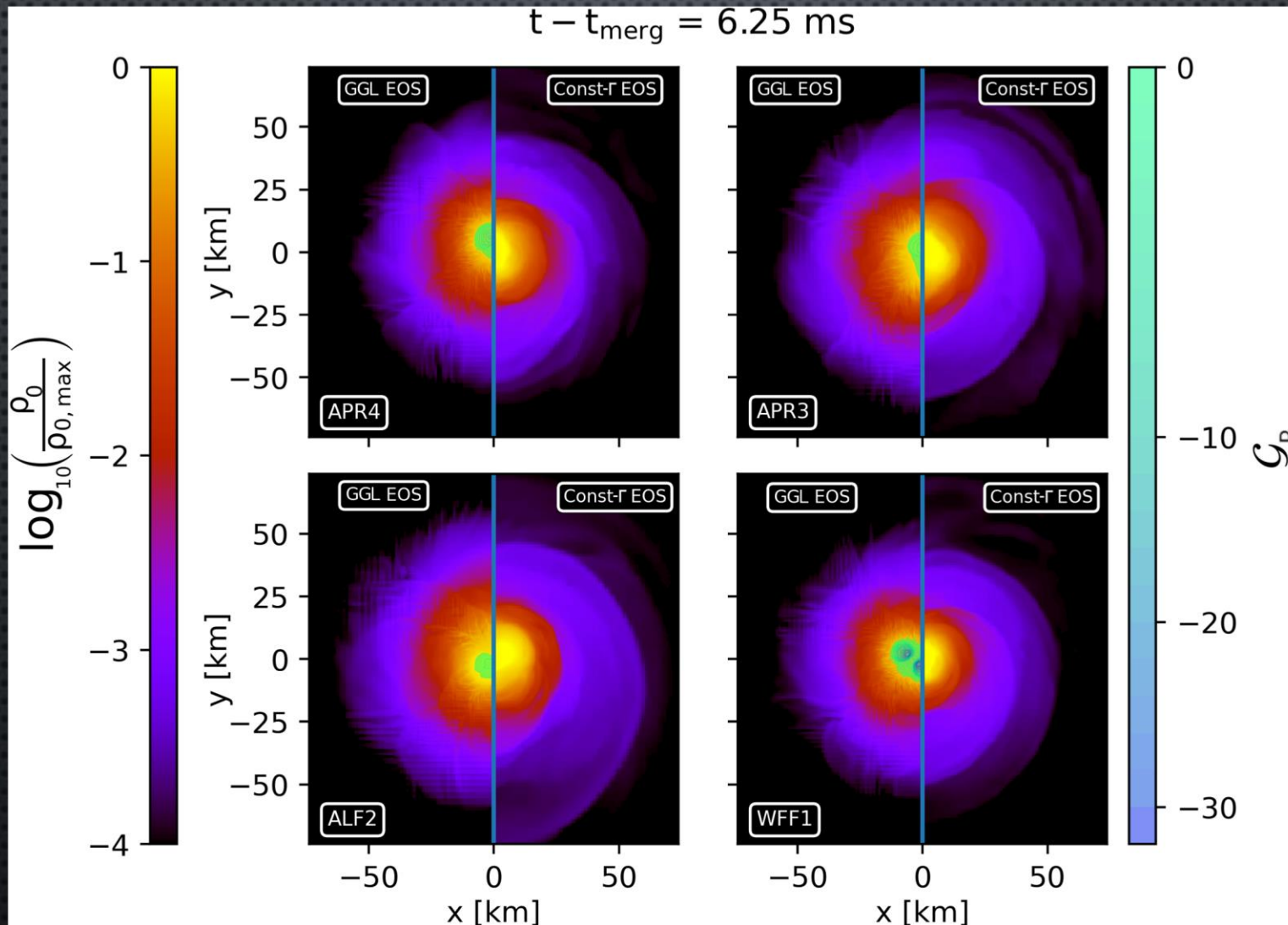
$$P_{th} = (\Gamma - 1)\epsilon_{th}n$$



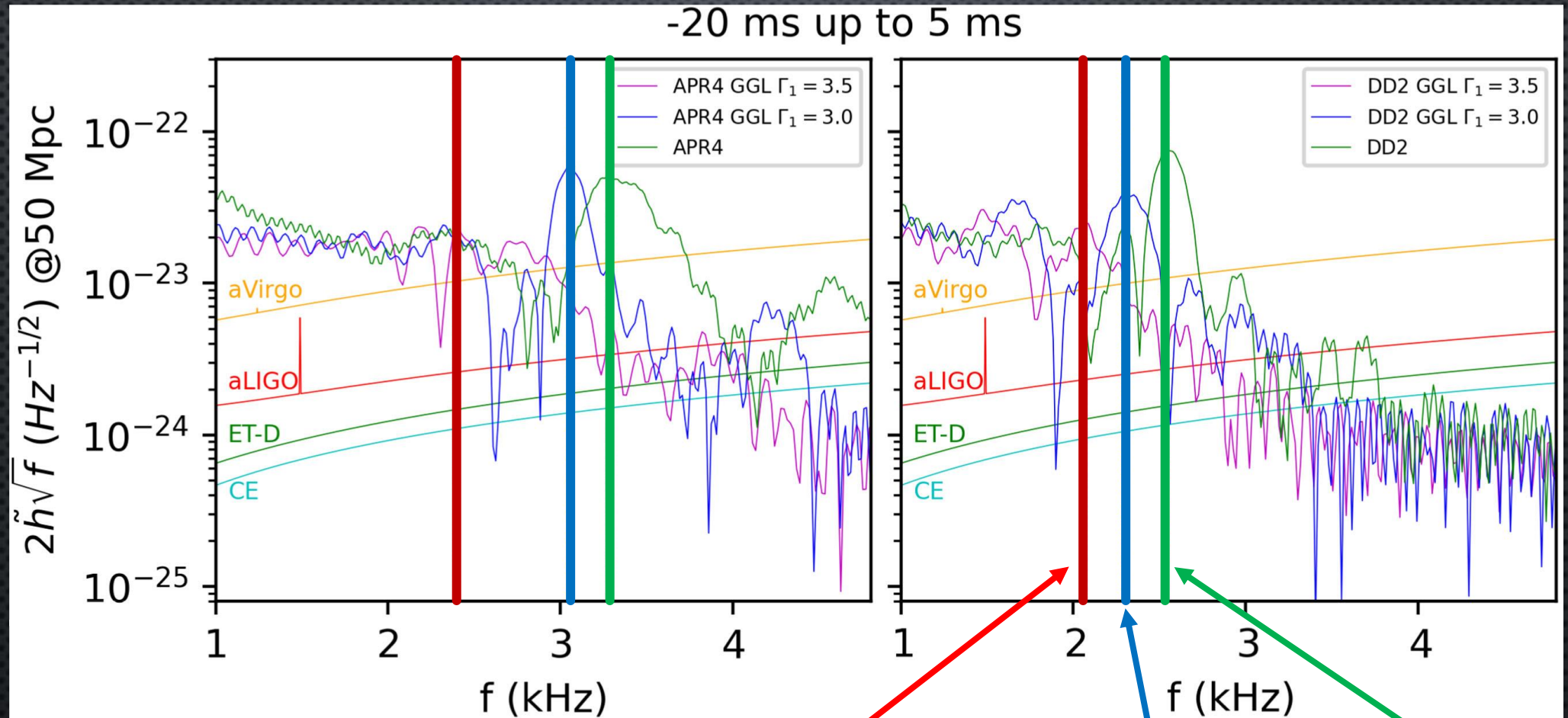
$\Gamma = \text{CONST}$

GGL EOS

# RESULTS: NON-CONVEX CORE AND NO SPIRAL ARM



# RESULTS: GENERAL SHIFT ON THE LEFT OF THE MAIN POST-MERGER PEAK IN FREQUENCY



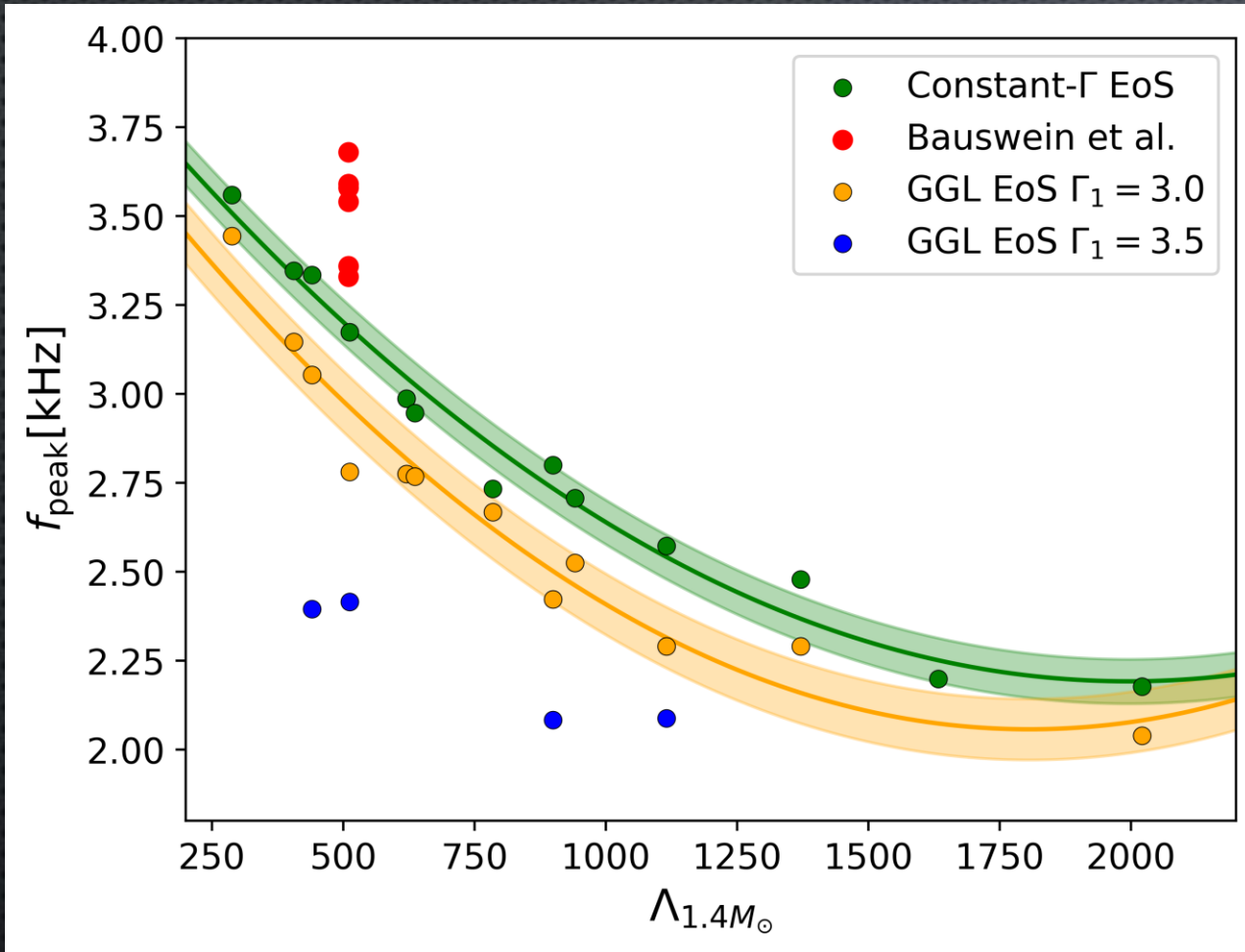
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GGL  $\Gamma_1 = 3.5$

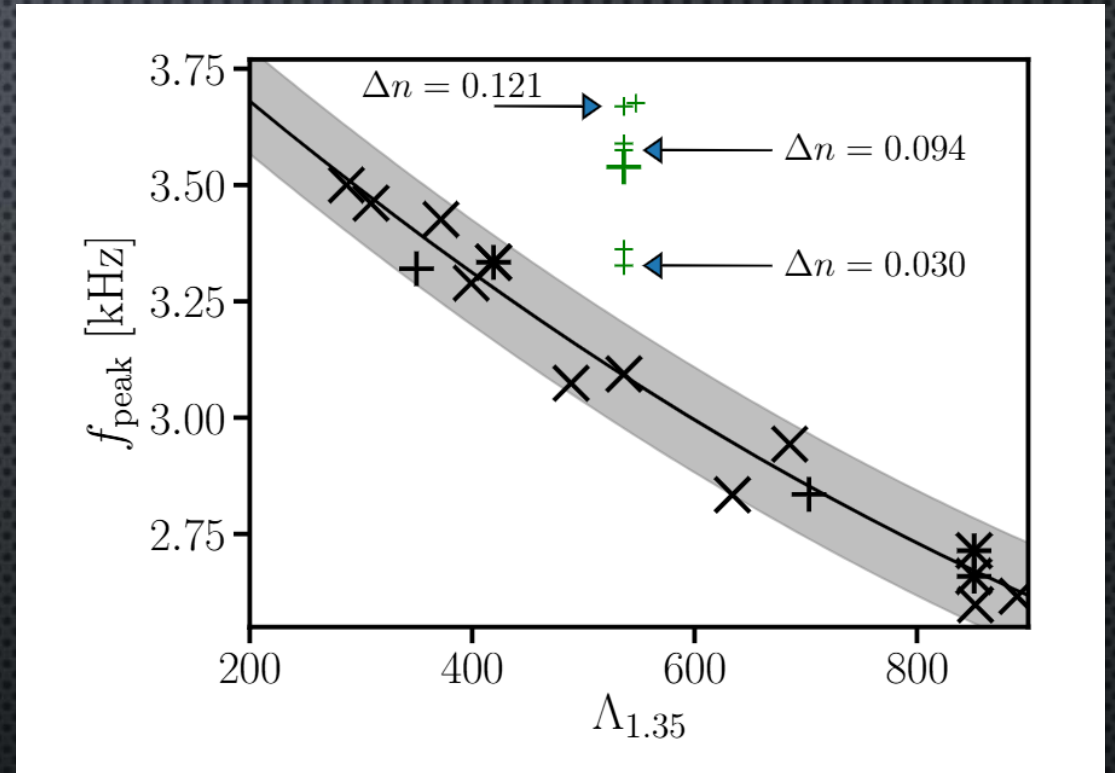
GGL  $\Gamma_1 = 3.0$

STANDARD  $\Gamma = 1.8$

# QUASI-UNIVERSAL RELATION



G. Riviello et al. (2024) Phys. Rev. D **109**, 064032



Bauswein et al. 2019 Phys. Rev. Lett. **122**, 061102



# TAKE-HOME MESSAGES

- NUMERICAL SIMULATION TO CONSTRAIN EOS
- NON-CONVEXITY ENHANCES THE EFFECT OF TRANSITION
- **EVALUATE THE FUNDAMENTAL DERIVATIVE TO BETTER UNDERSTAND THE EOS PROPERTIES AND OBSERVABLES**



THANKS!

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