



# Two-neutrino double-beta decay to excited states of heavy nuclei

Beatriz Benavente de Lucas

Collaboration: Javier Ménendez, Dorian Frycz



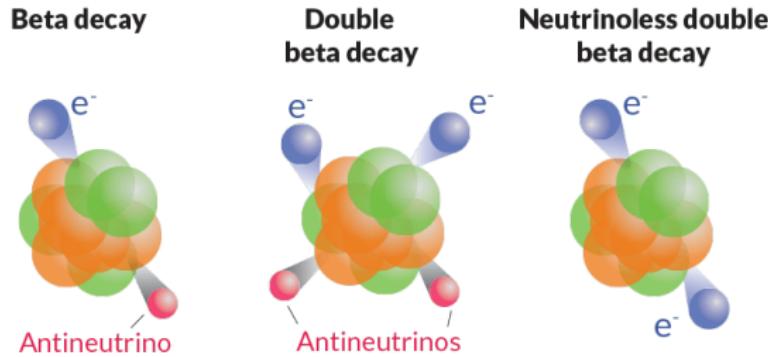
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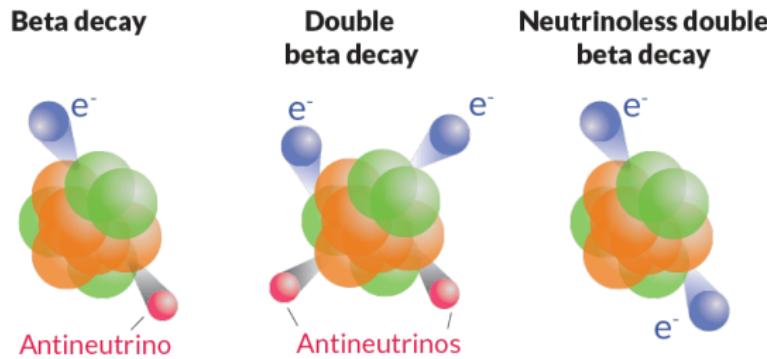
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- Neutrinoless double-beta decay violates the Standard model of particles physics(**D. Castillo's** previous talk)
- Two-neutrino double-beta decay is permitted in the Standard model of particles physics



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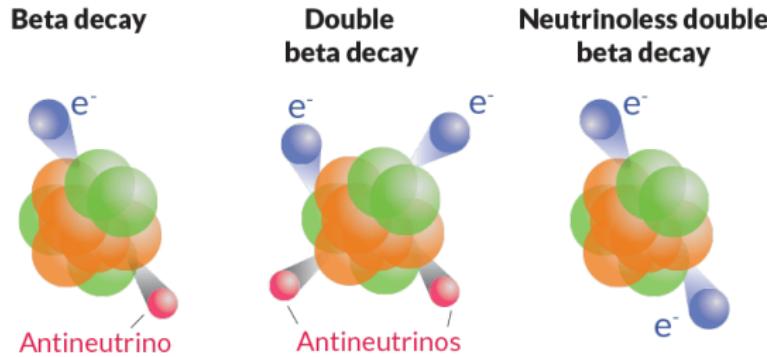
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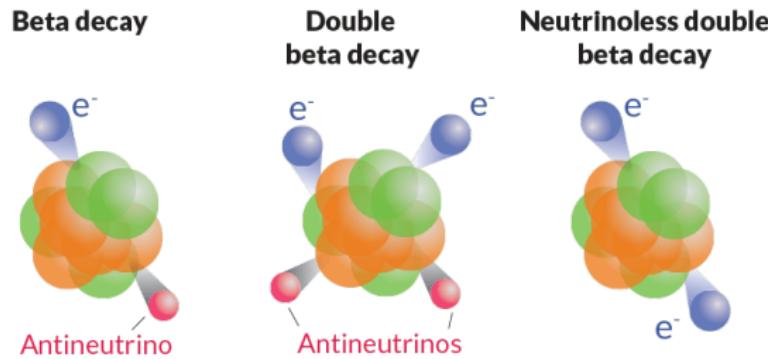
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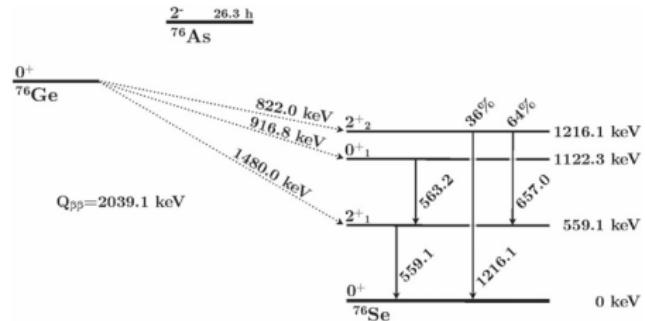
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- Initial and final states are common in both cases
- Many-body methods applicable in both cases

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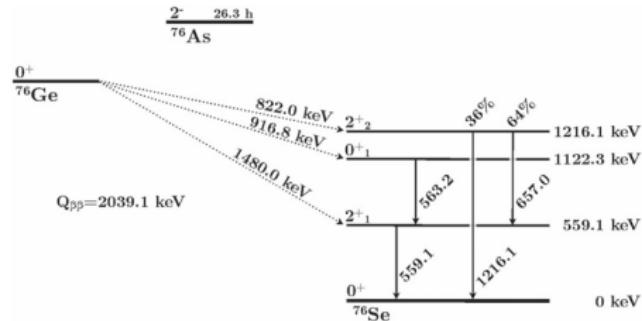
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GERDA Collaboration et al J. Phys. G: Nucl. Part. Phys. 42 (2015)

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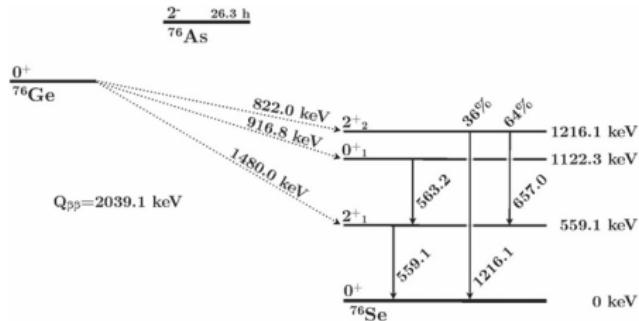
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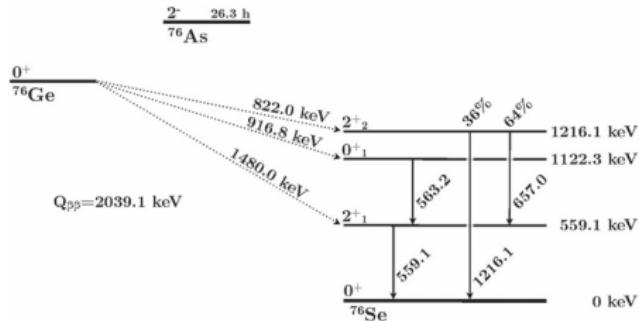


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- Similar study on  $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$

L. Jokiniemi, B. Romeo, C. Bräse, J. Kotila, P. Soriano, A. Schwenk, J. Menéndez. Phys. Lett. B 838 (2023)



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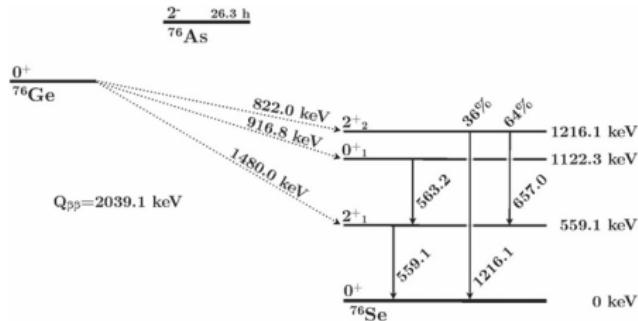
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- $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$ ,  $E(^{76}\text{Se}, 0_2^+) = 1.122 \text{ MeV.}$
  - $^{82}\text{Se} \rightarrow ^{82}\text{Kr}$ ,  $E(^{82}\text{Kr}, 0_2^+) = 1.488 \text{ MeV.}$
  - $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$ ,  $E(^{130}\text{Xe}, 0_2^+) = 1.793 \text{ MeV.}$

Brookhaven National Laboratory. National Nuclear Data Center. <https://www.nndc.bnl.gov> (2023)



GERDA Collaboration et al J. Phys. G: Nucl. Part. Phys. 42 (2015)

# Nuclear shell model

Schrödinger equation:

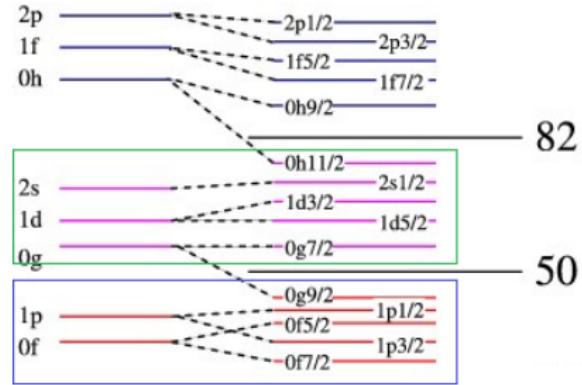
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Restriction to the valence space:



$^{76}\text{Ge}, {}^{82}\text{Se}$ :  $(1p_{3/2}, 0f_{5/2}, 1p_{1/2}, 0g_{9/2})$   
 ${}^{130}\text{Te}$ :  $(0g_{7/2}, 1d_{5/2}, 1d_{3/2}, 2s_{1/2}, 0h_{11/2})$

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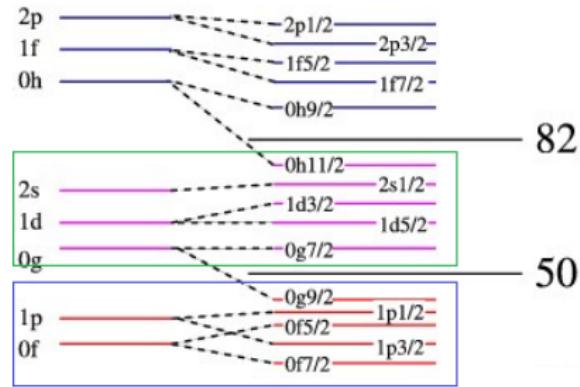
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**ANTOINE** shell-model code:  
Lanczos method

E. Caurier, F. Nowacki. Acta Phys. Pol. B 30: 705 (1999)

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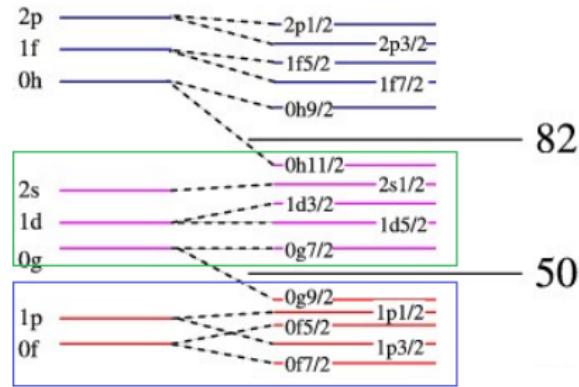


Linear combinations of the Slater determinants:

$$|\psi\rangle = \sum_{\alpha} C_{\alpha} |\phi_{\alpha}\rangle$$

$$|\phi_{\alpha}\rangle = \sum_{i=nljm} a_i^{\dagger} |0\rangle$$

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$$M^{2\nu} = \sum_n \frac{\langle 0_f^+ | \sum_a \sigma_a \tau_a^- | 1_n^+ \rangle \langle 1_n^+ | \sum_b \sigma_b \tau_b^- | 0_i^+ \rangle}{E_n - (E_i - E_f)/2}$$

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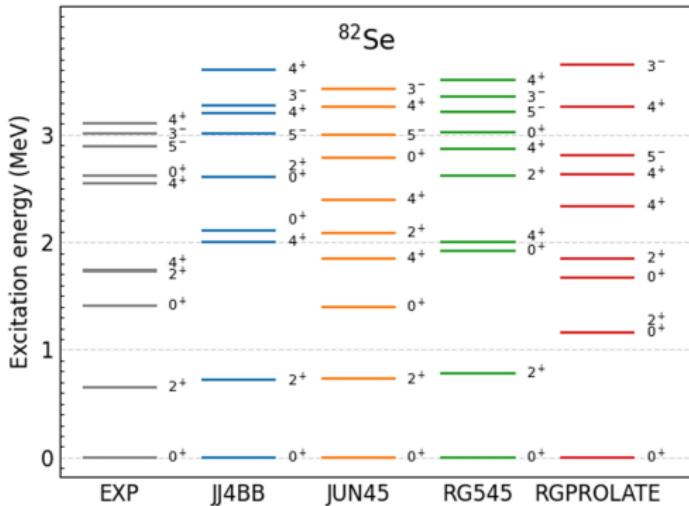
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- Correction by quenching factor,  $q$ , on the matrix elements
- Half-life:

$$\left( T_{1/2}^{2\nu} \right)^{-1} = G^{2\nu} g_A^4 \left( M^{2\nu} m_e c^2 \right)^2$$

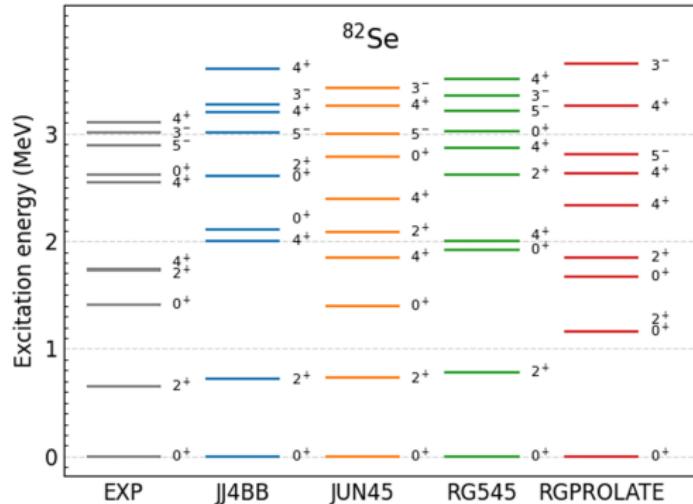
$G^{2\nu}$  : phase-space factor  
 $g_A$  : axial coupling  
 $m_e$  : electron mass

# Spectrum



- 4 different interactions
- No interaction significantly better than the others
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Occupation study:  $|n_{g_{9/2}} n_{p_{1/2}} n_{f_{5/2}} n_{p_{3/2}} p_{g_{9/2}} p_{p_{1/2}} p_{f_{5/2}} p_{p_{3/2}}\rangle$

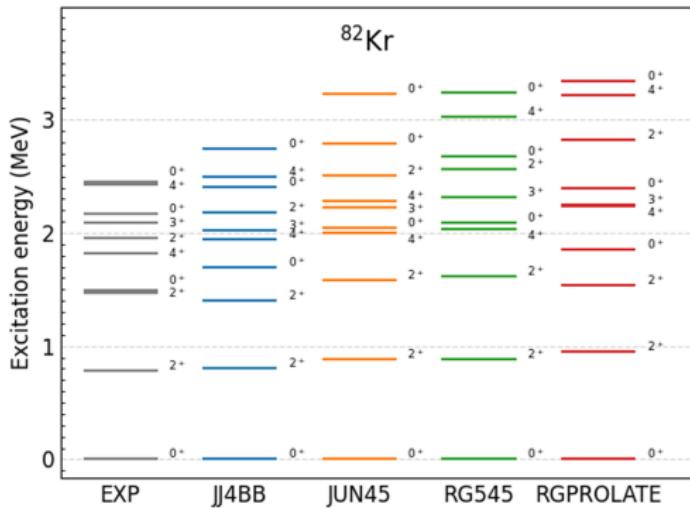
$$\text{JJ4BB: } |0_{gs}^+\rangle = 0.60|8\ 2\ 6\ 4\ 0\ 0\ 4\ 2\rangle + \dots$$

$$\text{JUN45: } |0_{qs}^+\rangle = 0.62|82640042\rangle + \dots$$

$$\text{RG545: } |0_{qs}^+\rangle = 0.61|82640042\rangle + \dots$$

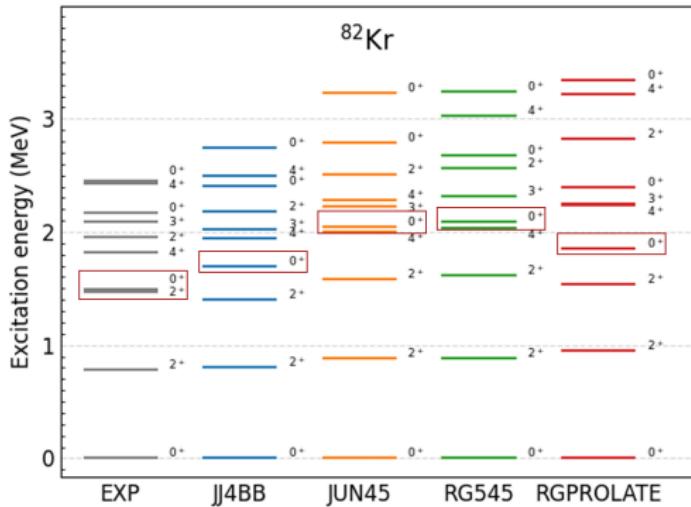
$$\text{RGPROLATE: } |0_{gs}^+\rangle = 0.44|100640060\rangle + 0.32|100640042\rangle + \dots$$

# Spectrum



- JJ4BB, RGPROLATE: best description of  $0^+_2$  energy
- JUN45, RG545: higher  $0^+_2$  energy prediction
- Wf describing  $0^+_2$  state fragmented across all interactions

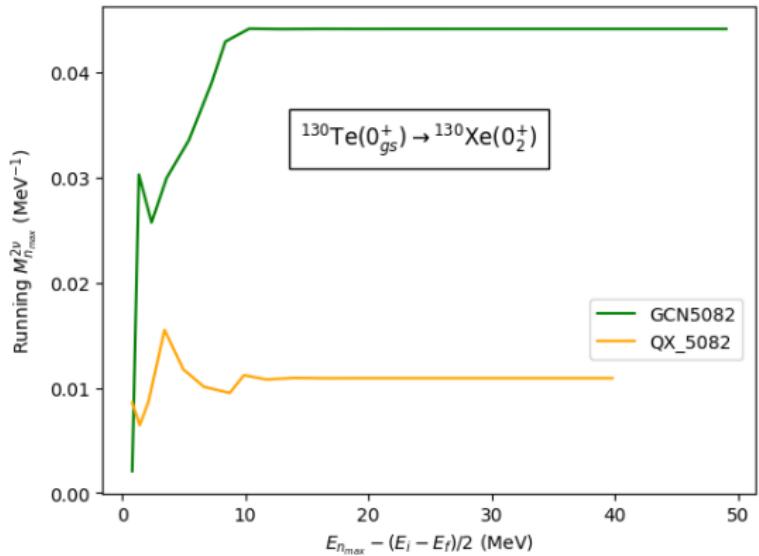
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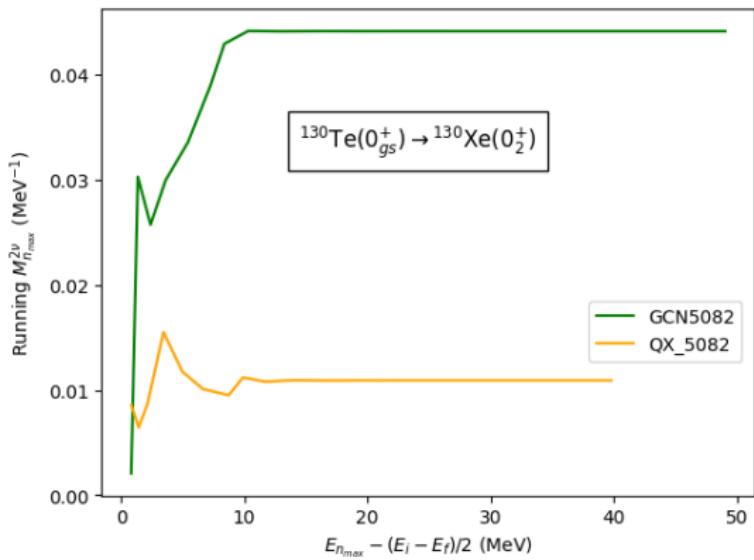
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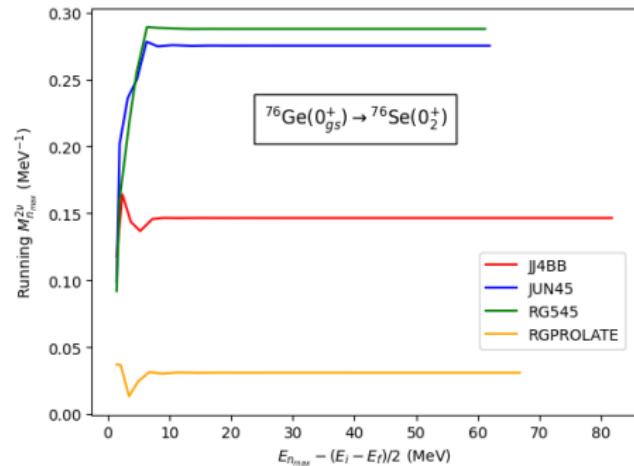
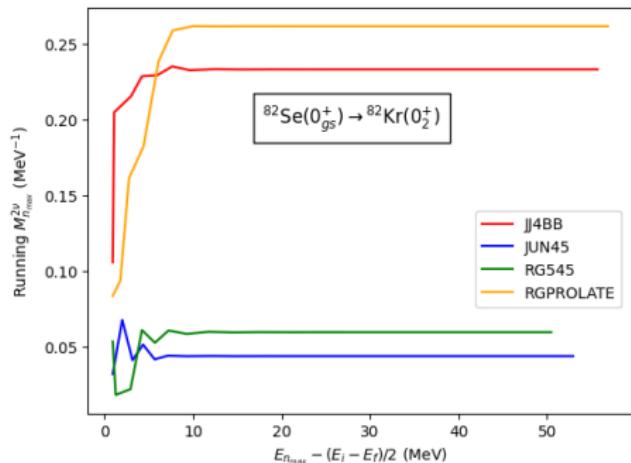
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$$M_{n_{max}}^{2\nu} = \sum_n^{n_{max}} \frac{\langle 0_f^+ || \sum_a \sigma_a \tau_a^- || 1_n^+ \rangle \langle 1_n^+ || \sum_b \sigma_b \tau_b^- || 0_i^+ \rangle}{E_n - (E_i - E_f)/2}$$



- Convergence of matrix elements
- Running matrix element: truncation of matrix elements for  $n$  intermediate states
- Calculated using Lanczos strength function

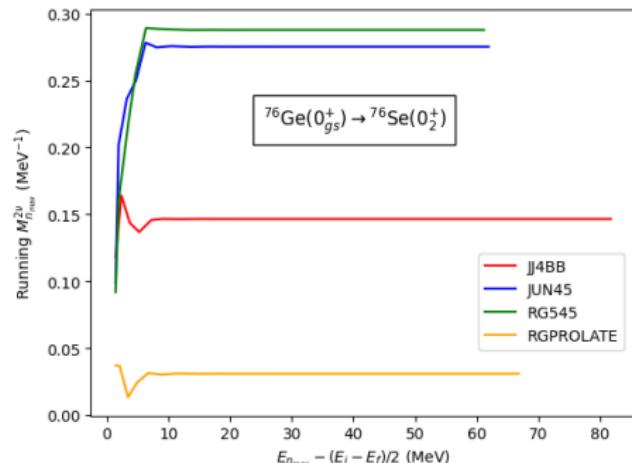
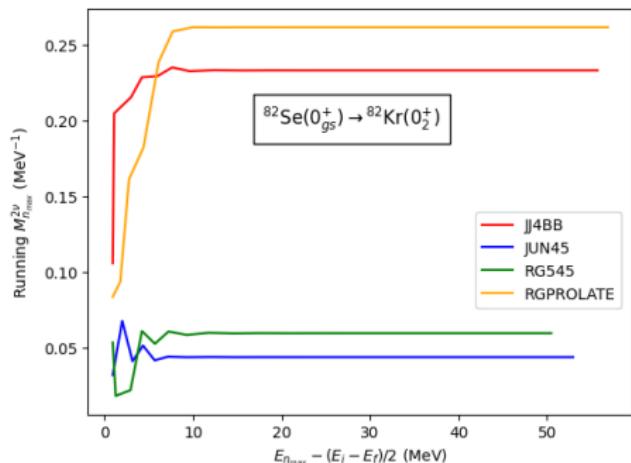
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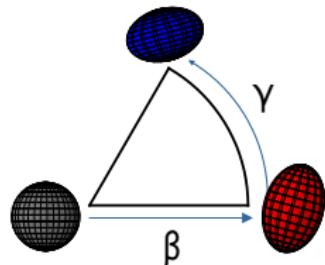
# Projected generator coordinate method (PGCM)

Variational approach:

- Configuration mixing of Hartree-Fock-Bogoliubov (HFB) states:  
 $|\Psi_{\text{GCM}}\rangle = \sum_q f_q |\phi_{\text{HFB}}(q)\rangle$

B. Bally, et al. Eur. Phys. J. A **60**, 62 (2024)

- Similar deformations for all interactions



D. Frycz: 11/07, 17:30h, M1

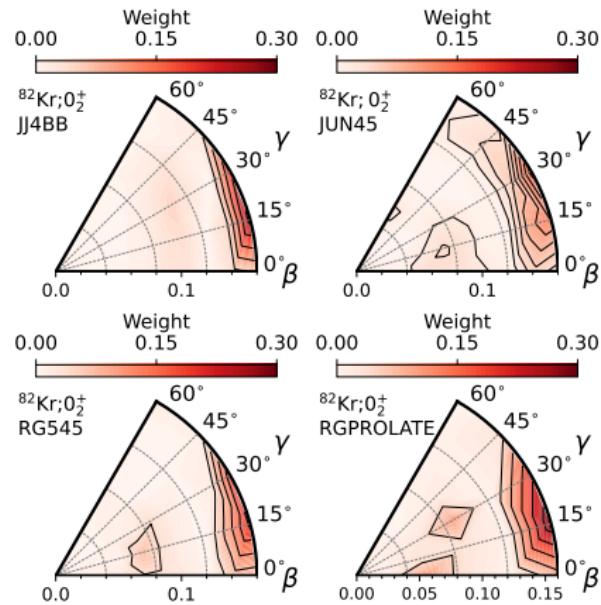


Figure: Contribution of each HFB wavefunction to fully mixed state for  $^{82}\text{Kr}(0_2^+)$  with all interactions

## Quenching

Quenching factor to correct the overestimation of matrix elements

- $q_\beta = 0.6$ , from previous  $\beta$  decay studies from literature  
E. Caurier et al. Phys. Lett. B 711: 1, 62-64 (2012)

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Predicted half-life g.s. to g.s.  $\xrightarrow{q_{2\nu}}$  Experimental half-life g.s. to g.s.

A. Barabash. Universe. 6(10): 159 (2020)

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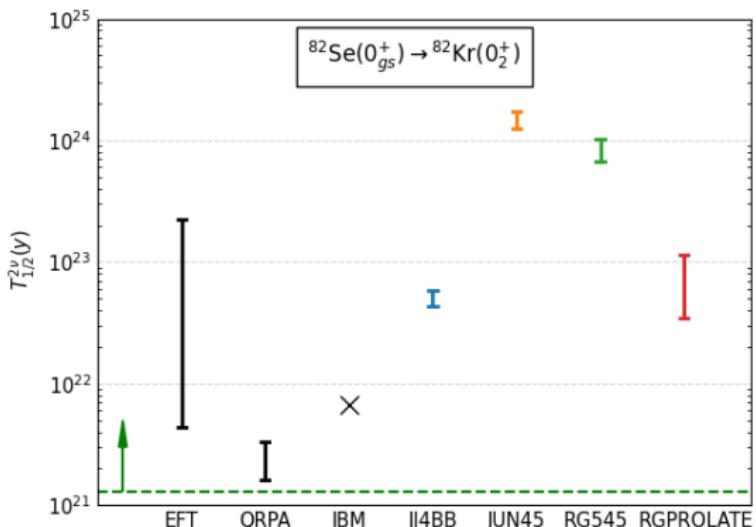
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	$q_{2\nu}$	INT
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	0.56	JJ4BB
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	0.55	JUN45
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	0.54	RG545
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	0.44	RGPROLATE
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.64	JJ4BB
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.61	JUN45
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$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.54	RGPROLATE
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	0.47	GCN5082
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	0.75	QX_5082

# Half-life predictions



NEMO-3 collaboration. Nuc. Phys. A 996: 121701 (2020)

E. A. Coello Pérez, J. Menéndez, A. Schwenk. Phys. Rev. C 98: 045501 (2018)

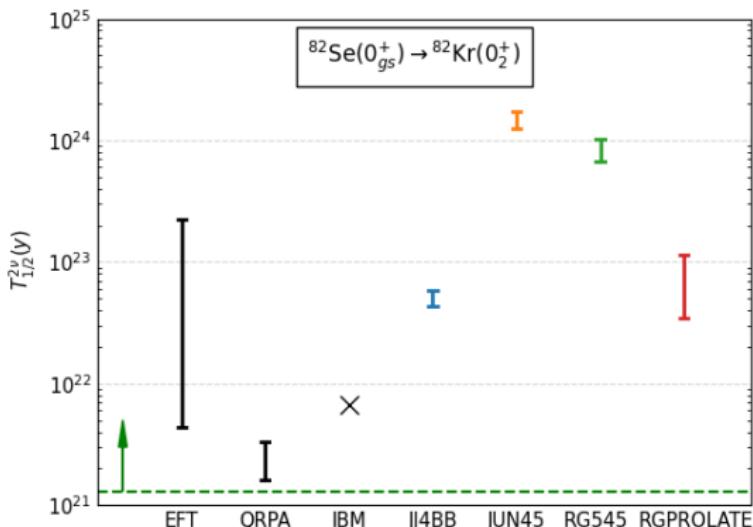
J. Toivanen, J. Suhonen. Phys. Rev. C 55: 2314 (1997)

J. Barea, J. Kotila, F. Iachello. Phys. Rev. C 91: 034304 (2015)

Experimental limit:  $T_{1/2}^{2\nu}({}^{82}\text{Se}, 0^+_gs \rightarrow {}^{82}\text{Kr}, 0^+_2) > 1.3 \cdot 10^{21}$  yr

Range of predictions:  $T_{1/2}^{2\nu}({}^{82}\text{Se}, 0^+_gs \rightarrow {}^{82}\text{Kr}, 0^+_2) = (3.5 - 170) \cdot 10^{21}$  yr

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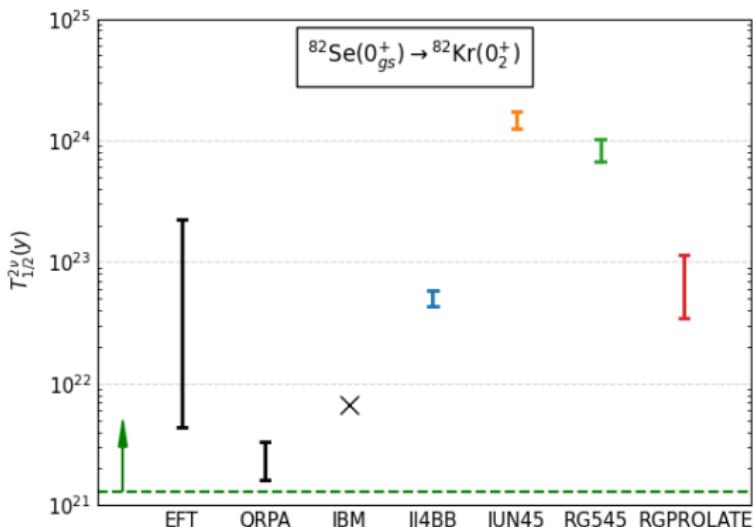
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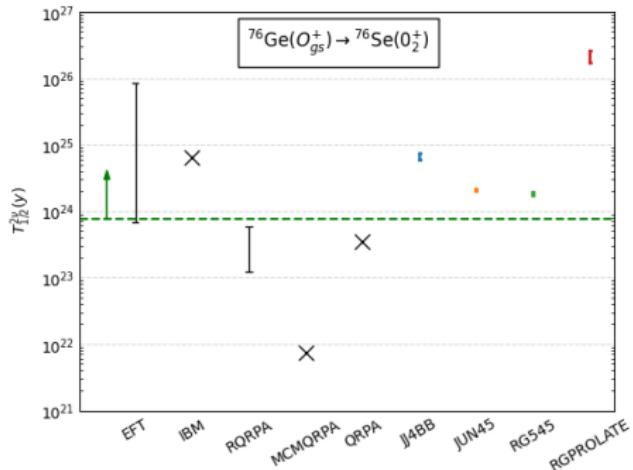
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S. Stoica, I. Mihut. Nucl. Phys. A 602: 197 (1996)

M. Aunola, J. Suhonen. Nucl. Phys. A 602: 133 (1996)

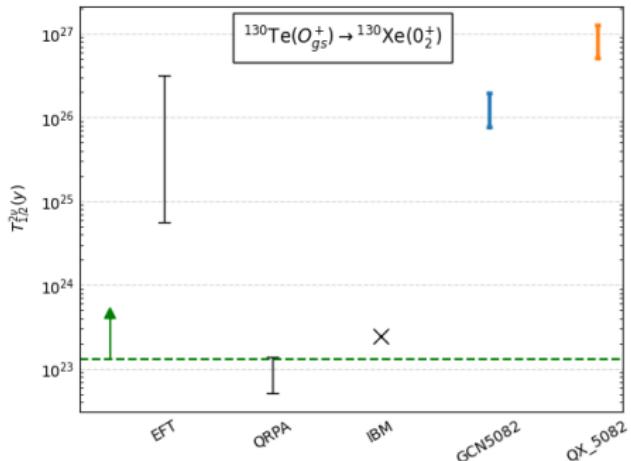
MAJORANA Collaboration. Phys. Rev. C 103: 1, 015501 (2021)

J. Barea, J. Kotila, F. Iachello. Phys. Rev. C 91: 034304 (2015)

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Range of predictions:

$$T_{1/2}^{2\nu}(^{76}\text{Ge}, 0_{gs}^+ \rightarrow ^{76}\text{Se}, 0_2^+) = (2 - 260) \cdot 10^{24} \text{ yr}$$



J. Barea, J. Kotila, F. Iachello. Phys. Rev. C 91: 034304 (2015)

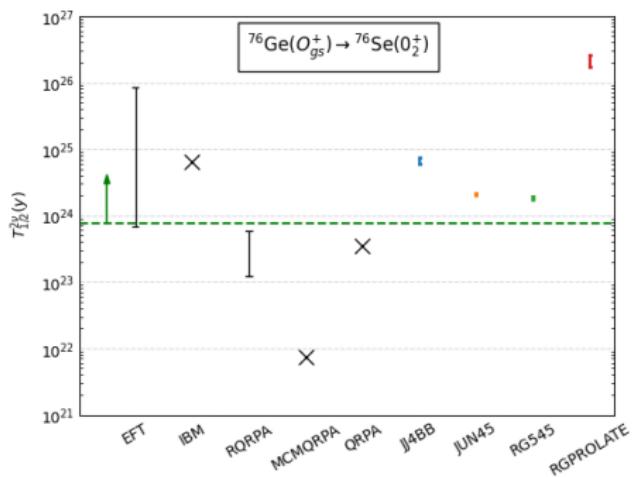
E. Andreotti et al. Phys. Rev. C 85: 045503 (2012)

E. A. Coello Pérez, J. Menéndez, A. Schwenk. Phys. Rev. C 98: 045501 (2018)

Range of predictions:

$$T_{1/2}^{2\nu}(^{130}\text{Te}, 0_{gs}^+ \rightarrow ^{130}\text{Xe}, 0_2^+) = (7.7 - 130) \cdot 10^{25} \text{ yr}$$

# Summary



- Study of 3 different  $2\nu\beta\beta$  decays with different interactions in the context of the NSM
- Many-body methods applicable in the study of the neutrinoless double-beta decay
- Different running matrix elements, but are yet to find a plausible explanation for it
- Predicted half-lives consistent with experimental limits, close to it in some cases

The discrepancies between the prediction of half-lives makes the testing of these values a good way of validating the many-body methods used in the study. We really look forward to these results being tested!



# Thank you!



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