

# Can femtosopic correlation function shed light on the nature of the lightest, charm, axial mesons?

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arXiv:2312.11811 [hep-ph])

QNP2024  
Barcelona, Spain



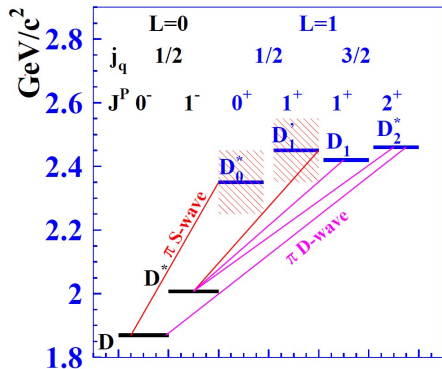
Financial support:

- A brief overview on the two lightest axial mesons with charm:  $D_1(2430)$  and  $D_1(2420)$
- Description based on the dynamics at the quark level as well as among hadrons
- Use of two approaches resulting in different scattering lengths: one in agreement with lattice QCD and the other with data of ALICE
- Investigation if the correlation function for channels dominated by strong interactions are sensitive to two scenarios



# Motivation

- $D$ -meson excitations:



[Belle, PRD 69, 112002 (2004)]

- PDG:

$D_1(2420)$  :

$$M = 2422.1 \pm 0.6 \text{ MeV},$$

$$\Gamma = 31.3 \pm 1.9 \text{ MeV}.$$

$D_1(2430)$  :

$$M = 2412 \pm 9 \text{ MeV},$$

$$\Gamma = 314 \pm 29 \text{ MeV}.$$

- Belle (2004) and LHCb (2020):  
fit from the  $D^*\pi$  invariant mass  
distribution of  $B^- \rightarrow D^{*+}\pi^-\pi^-$   
decay



## Explanation of the masses and widths ( $R = \Gamma_{D_1(2430)}/\Gamma_{D_1(2420)} \sim 10$ ) from the same dynamics: controversies

- Models based purely on hadron dynamics: existence of two low-lying  $D_1$ 's, but predictions do not coincide with experiments
- Heavy quark symmetry: decay rates lead  $R \sim 10$  once the states are assumed with  $1^1P_1$  and  $1^3P_1$  (Manohar-Wise book)
- Quark model states with mixing:  $R$  far from data (e.g. Ferretti and Santopinto, PRD 97, 114020 (2018))
- Mixing of the two states through the consideration of hadron loops can describe  $R$  (Zhou and Xiao, PRD 84, 034023 (2011))
- Different types of mixing of the  $1^1P_1$  and  $1^3P_1$  states lead to similar masses but different values of the  $R$
- Hadron loops or meson clouds are useful in better describing the properties of  $D_1(2420)$  and  $D_1(2430)$



## Scattering length $a_{D^{(*)}\pi}$ ( $D^*\pi$ : main decay of the $D_1$ states):

Femtoscopia (ALICE, arXiv:2401.13541)

Lattice QCD (Mohler et al. PRD 87, 034501 (2013))

→ **DISAGREEMENT**

EFT predictions (Torres-Rincon et al. PRD 108, 096008 (2023))

## Purposes of this work

- **Obtention of a model that can describe the mass and width of the two lowest-lying  $D_1$  states**

Our attempt shows that an interplay of quark-hadron degrees of freedom can be useful

- **Investigation if femtoscopic correlation functions can be useful in resolving the situation**

Focus on channels  $D^{*+ (0)}\pi^{0 (+)}$ , dominated by strong interactions, not needing Coulomb interactions

(different of those in PRD 108, 096008 (2023) [unitarized ChPT with heavy quark symmetry] );

They can be used to settle the value of the  $D^*\pi$  scattering length

## Our approach

### Meson-meson coupled channel + Bare quark-model pole

- Interactions between vector and pseudoscalar mesons based on  $SU(4)$  symmetry: Gamermann and Oset, EPJA 33, 119 (2007); Malabarba et al., PRD 107, 036016 (2023)

Lowest-order amplitude ( $I = 1/2$ ):

$$V_{ij} = \frac{C_{ij}}{4f^2} (s - u) \vec{\epsilon} \cdot \vec{\epsilon}',$$

|                | $\pi D^*$ | $D\rho$    | $\bar{K}D_s^*$        | $D_s\bar{K}^*$       |
|----------------|-----------|------------|-----------------------|----------------------|
| $\pi D^*$      | -2        | $\gamma/2$ | $-\sqrt{\frac{3}{2}}$ | 0                    |
| $D\rho$        |           | -2         | 0                     | $\sqrt{\frac{3}{2}}$ |
| $\bar{K}D_s^*$ |           |            | -1                    | 0                    |
| $D_s\bar{K}^*$ |           |            |                       | -1                   |

$C_{ij}$  for the most relevant channels to study the  $D_1$  states

$$\gamma = \left(\frac{m_L}{m_H}\right)^2; \quad m_L = 800 \text{ MeV and } m_H = 2050 \text{ MeV}$$

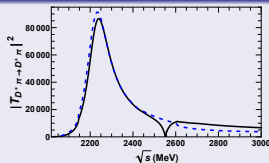
- Additional contribution: Box diagrams for the  $D\rho \rightarrow D^*\pi \rightarrow D\rho$  with pseudoscalar exchange ( $PPV$  and  $PVV$  vertices)
- Solution of the Bethe-Salpeter equation ( $G$ : loop function):

$$T = V + VGT$$



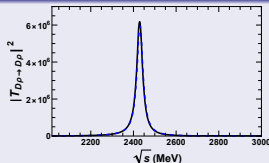
## First state

- $M \sim 2428$  MeV,  $\Gamma \sim 33$  MeV
- Strong (weak) coupling to  $D\rho$  ( $D^*\pi$ )
- Good agreement with  $D_1(2420)$



## Second state

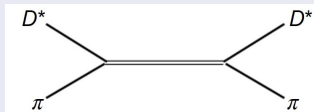
- $M \sim 2220$  MeV,  $\Gamma \sim 131$  MeV
- Strong coupling to  $D^*\pi$
- Discrepancy with  $D_1(2430)$



Better description: addition of a bare quark-model pole for  $D^*\pi$

$$V_{QM} = \pm \frac{g_{QM}^2}{s - M_{QM}^2};$$

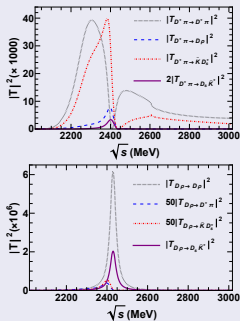
$M_{QM}$ ,  $g_{QM}$ : adjusted to describe the  $D_1(2430)$  as well as the  $D^*\pi$  scattering lengths



# Model A

$$V_{QM} = -\frac{6000^2}{s - 2440^2}$$

(Godfrey and Isgur, PRD 32, 189 (1985))



- $D^* \pi$ :  $M \sim 2304$  MeV,  $\Gamma \sim 160$  MeV

(Lower limit for  $D_1(2430)$  from Babar (2006))

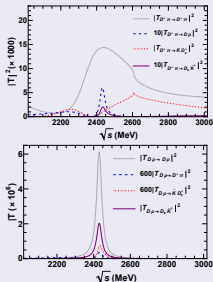
- $a_{D^* \pi}^{(1/2)} = -0.20$  fm

(In accordance with lattice results for  $a_{D\pi}^{(1/2)}$  (Liu et al. PRD 87, 014508 (2013)))

# Model B

$$V_{QM} = \frac{10000^2}{s - 2370^2}$$

( $g_{QM}, M_{QM}$  considered as free parameters)



- $D^* \pi$ :  $M \sim 2436$  MeV,  $\Gamma \sim 311$  MeV

(Agreement with LHCb and Belle data)

- $a_{D^* \pi}^{(1/2)} = 0.1$  fm

(In accordance with recent Alice results for  $a_{D^* \pi}^{(1/2)}$  (e-Print: 2401.13541 [nucl-ex]))



# Correlation Functions

Generalized coupled-channel CF for a specific channel  $i$

$$\begin{aligned} C_i(k) &\simeq \int d^3\vec{r} S_{12}(\vec{r}) |\Psi(\vec{r}, \vec{k})|^2 \\ &= 1 + 4\pi\theta(\Lambda - k) \int_0^\infty dr r^2 S_{12}(\vec{r}) \left( \sum_j |j_0(kr)\delta_{ji} + T_{ji}(\sqrt{s})\tilde{G}_j(r; s)|^2 - j_0^2(kr) \right) \end{aligned}$$

$\vec{k}$ : relative momentum;

$E = \sqrt{s}$ : the CM energy;

$T_{ji}$ : elements of the scattering matrix encoding the meson-meson interactions;

$$\tilde{G}_j(r; s) = \int_{|\vec{q}| < \Lambda} \frac{d^3q}{(2\pi)^3} \frac{\omega_1^{(j)} + \omega_2^{(j)}}{2\omega_1^{(j)}\omega_2^{(j)}} \frac{j_0(qr)}{s - (\omega_1^{(j)} + \omega_2^{(j)})^2 + i\epsilon},$$

( $\omega_a^{(j)} \equiv \omega_a^{(j)}(k) = \sqrt{k^2 + m_a^2}$ ;  $\Lambda = 700$  MeV);

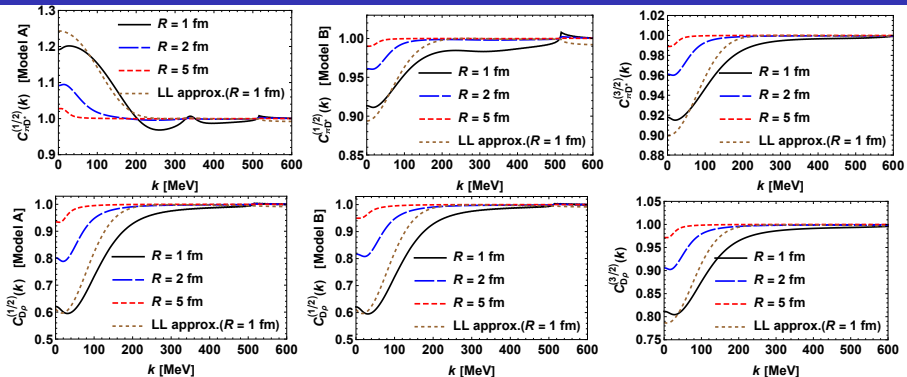
$S_{12}(\vec{r})$ : source function,

$$S_{12}(\vec{r}) = \frac{1}{(4\pi)^{\frac{3}{2}} R^3} \exp\left(-\frac{r^2}{4R^2}\right),$$

( $R$ : source size parameter)



# Results: Correlation Functions in isospin basis



Lednický-Lyuboshits:  $C_{LL} = 1 + \frac{1}{(kR)^2 + (\frac{R}{a})^2} \left[ \frac{1}{2} - \frac{2R}{a\sqrt{\pi}} F_2(2kR) - kRF_3(2kR) \right]$ ;  $F_2 = \int dt \frac{e^{t^2 - z^2}}{z}$ ,  $F_3 = \frac{1 - e^{-z^2}}{z}$

- Model A:  $C_{D^{*\pi}}^{(1/2)}(k=0)|_{R=1\text{fm}} > 1$ , because of the attractive character and  $a_{D^{*\pi}}^{(1/2)} < 0$
- Model B:  $C_{D^{*\pi}}^{(1/2)}(k=0)|_{R=1\text{fm}} < 1$ , because of  $a_{D^{*\pi}}^{(1/2)} = 0.1 \text{ fm} < 2.3R$  (same in  $C_{D^{*\pi}}^{(3/2)}$ )
- Both models:  $C_{D^{*\pi}}^{(1/2)}(k > 0)$  reflects the behavior of  $T_{D^{*\pi}, D^{*\pi}}^{(1/2)}$  (same in  $C_{D^{*\pi}}^{(3/2)}$ )
- Dip in  $C_{D\rho}^{(1/2)}(k=0)$ : influence of the narrow state in  $T_{D\rho, D\rho}^{(1/2)}$  below the  $D\rho$  threshold

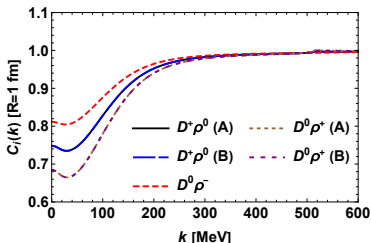
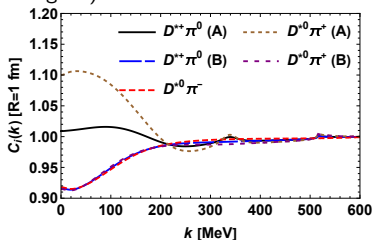


# Results: Correlation Functions in physical basis

$$C_{D^*0\pi^+} \equiv C_{D^*0\pi^+ \rightarrow D^*0\pi^+} + C_{D^{*+}\pi^0 \rightarrow D^*0\pi^+} = \frac{2}{3} C_{D^*\pi}^{(1/2)} + \frac{1}{3} C_{D^*\pi}^{(3/2)};$$

$$C_{D^{*+}\pi^0} \equiv C_{D^*0\pi^+ \rightarrow D^{*+}\pi^0} + C_{D^{*+}\pi^0 \rightarrow D^{*+}\pi^0} = \frac{1}{3} C_{D^*\pi}^{(1/2)} + \frac{2}{3} C_{D^*\pi}^{(3/2)}; \quad C_{D^*0\pi^-} \equiv C_{D^*\pi}^{(3/2)};$$

( $D\rho$ : analogous)



- Model A: features of  $T_{D^*\pi, D^*\pi}^{(1/2)}$  are more notable in the channel  $D^*0\pi^+$ , because of the bigger weight of the  $I = 1/2$
- Model B: there is no sizable difference between  $D^*0\pi^+$ ,  $D^{*+}\pi^0$  and  $D^*0\pi^-$  (similarity between  $C_{D^*\pi}^{(1/2)}(k)$  and  $C_{D^*\pi}^{(3/2)}(k)$ )
- $C_{D^+\rho^0}(k)$  closer to one at threshold than  $C_{D^0\rho^+}(k)$  (difference from isospin weights)
- $D^*0\pi^+$  and  $D^0\rho^+$ : more appropriate to test both models



# Summary

## Properties of the two lightest $D_1$ states

- Description of their different widths once their masses are assumed: possible via heavy quark symmetry
- Explanation of masses and widths from the same dynamics: not trivial
- $a_{D^{(*)}\pi}^{(1/2)}$  from femtoscopy based on Alice data: disagreement with lattice QCD calculations and EFT predictions

## Our work

- Comprehension of the  $D_1$  states and characterization of  $a_{D^{*}\pi}^{(1/2)}$
- Approach: meson-meson interactions + bare quark model pole used as kernels to solve the Bethe-Salpeter equation
- Good description for the  $D_1(2420)$  and  $D_1(2430)$ , with two different scenarios for bare quark-model pole giving distinct  $a_{D^{*}\pi}^{(1/2)}$
- Correlation functions of the  $D^{*0}\pi^+$  and  $D^{*0}\rho^+$  channels for smaller source sizes: can bring useful information