

Nuclei in the Cosmos School
2025

EXPERIMENTAL NUCLEAR PHYSICS

Richard Longland
North Carolina State U, USA

Outline

- 1 Experimental Yields
Count rates
- 2 Resonant reactions
Recap
Brief discussion of resonance theory
- 3 Indirect measurements
Transfer measurements
- 4 Peculiarities and details
Absolute cross sections
Target effects in transfer measurements
Astrophysical S Factor

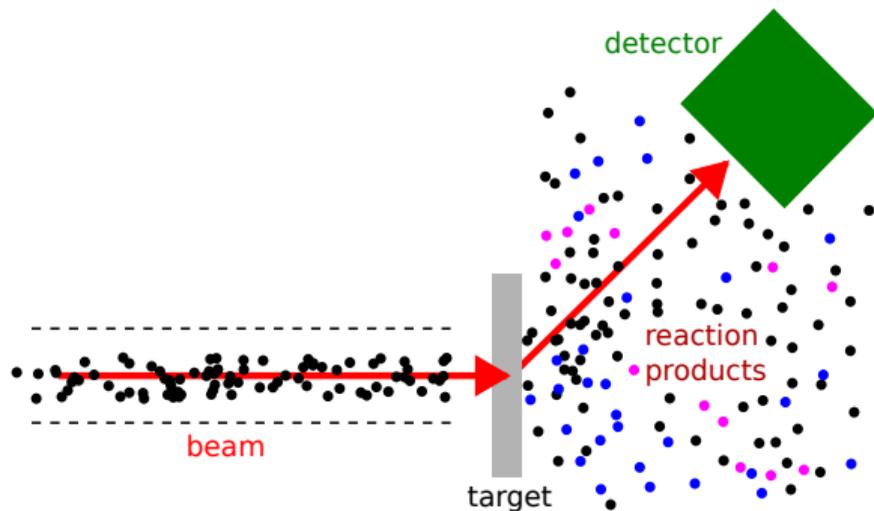
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Experimental yield

$$Y = \frac{N_R}{N_b}$$

- Detector doesn't measure all reaction products
- Reaction products aren't always emitted isotropically



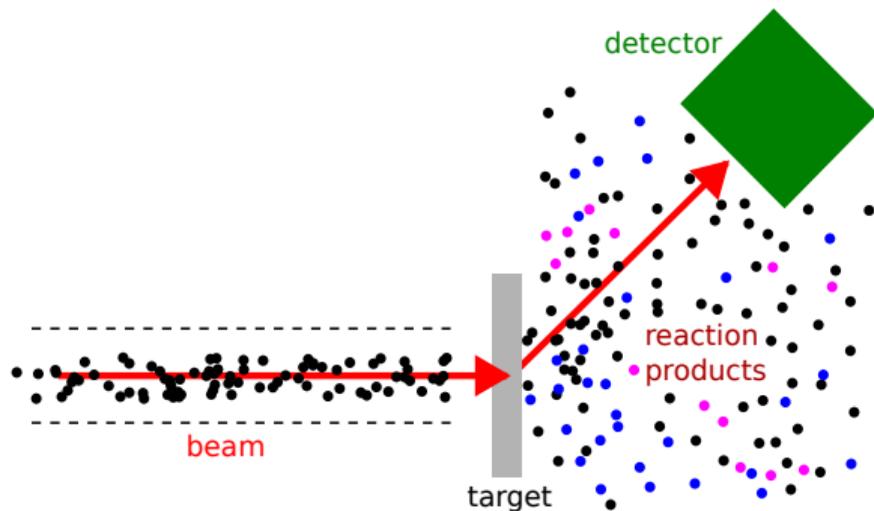
Experimental yield

$$Y = \frac{N_R}{N_b}$$

- Detector doesn't measure all reaction products
- Reaction products aren't always emitted isotropically
- Yield

$$Y = \frac{I}{N_b B \eta W}$$

- I : intensity of measured reaction product
- B : branching ratio if reaction product only carries part of strength



- η : detector efficiency
- W : Angular distribution correction

Count rates (for narrow resonance)

- Recall our two expressions for yield: experimental and theoretical

$$Y = \frac{I}{N_b B_\eta W} \quad \text{and} \quad Y_{\max} = \frac{\lambda_r^2 \omega \gamma}{2 \epsilon_r}$$

- Combine and find an expression for intensity of reaction products at top of yield curve

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- Combine and find an expression for intensity of reaction products at top of yield curve

$$I = \frac{\lambda_r^2 \omega \gamma}{2 \epsilon_r} N_b B \eta W$$

- For convenience, convert N_b to $I_b/q_b t$

- ▶ I_b is beam current
- ▶ q_b is beam charge in Coulombs
- ▶ Δt is length of experiment

$$\frac{I}{t} = \frac{\lambda_r^2 \omega \gamma}{2 \epsilon_r} \frac{I_b}{q_b} B \eta W$$

Example: $^{22}\text{Ne}(p,\gamma)^{23}\text{Na}$

$$\frac{I}{t} = \frac{\lambda_r^2 \omega_\gamma}{2 \epsilon_r} \frac{I_b}{q_b} B_\eta W$$

Narrow resonance at 35 keV dominates rate at low T

- $\omega_\gamma \sim 2 \times 10^{-15}$ eV
- Beam current: 2 mA
- Target effective stopping power:
 $\epsilon_r = 1.9 \times 10^{-14}$ eV cm²/atom
- Detector efficiency: $\eta = 100\%$
- Isotropic γ -ray emission: $W=1$

Count rate: $I/t = 1 \times 10^{-10}$ counts per hour!

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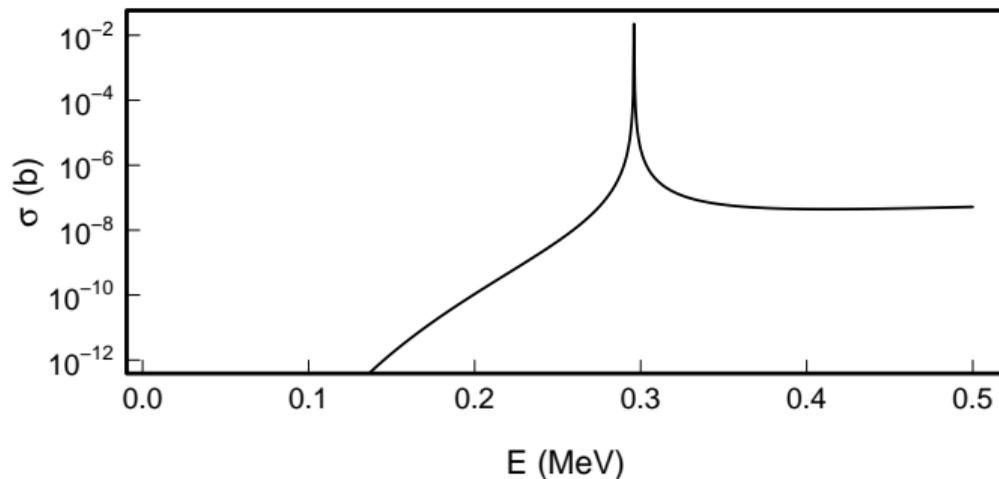
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Resonant reaction cross section



Either

$$\sigma(E) = \omega \frac{\Gamma_a \Gamma_b}{(E - E_r)^2 + \Gamma^2/4}$$

Or

$$\omega \gamma = \frac{\Gamma_a \Gamma_b}{\Gamma}$$

$$N_A \langle \sigma v \rangle = \sqrt{\frac{8}{\pi \mu}} \frac{N_A}{(kT)^{3/2}} \int_0^\infty \sigma(E) E e^{-E/kT} dE \quad N_A \langle \sigma v \rangle_{01} = N_A \left(\frac{2\pi}{\mu_{01} kT} \right)^{3/2} \hbar^2 \omega \gamma e^{-E_r/kT}$$

Definitions

$$\sigma(E) = \omega \frac{\Gamma_a \Gamma_b}{(E - E_r)^2 + \Gamma^2/4}$$

- Widths

- ▶ **Total width (FWHM):**

$$\Gamma = \Gamma_a + \Gamma_b + \dots$$

- ▶ **Partial width:**

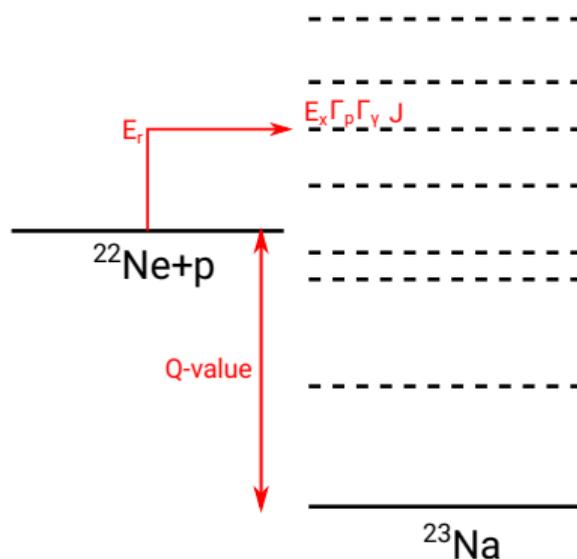
Γ_a . Corresponds to *probability of a level decaying through channel a*

- **Branching ratio:**

$$B_a = \frac{\Gamma_a}{\Gamma}$$

- ω :

$$\omega = \frac{2J + 1}{(2J_0 + 1)(2J_1 + 1)}$$



- **Resonance energy:** E_r
- **Q-value:** Energy released in a reaction

REVIEWS OF
MODERN PHYSICS

VOLUME 30, NUMBER 2, Part I

APRIL, 1958

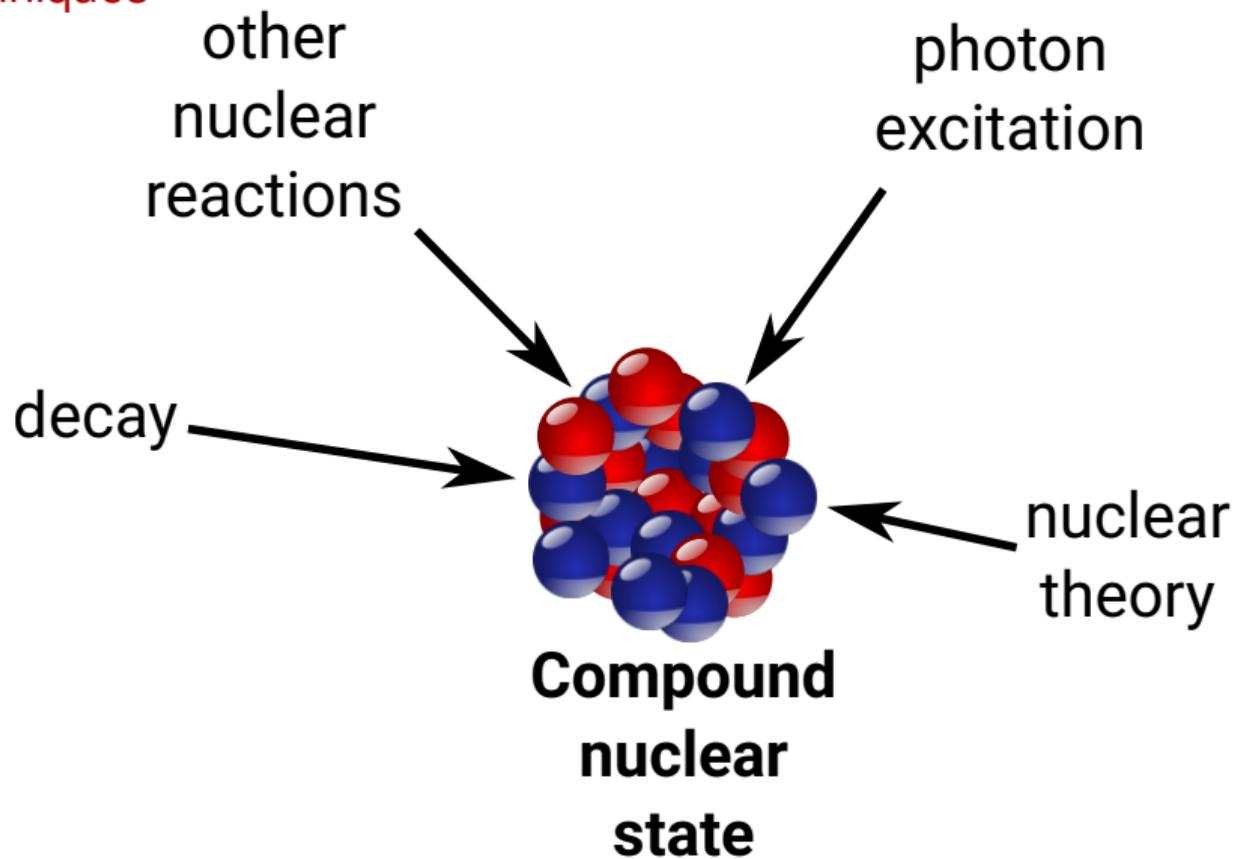
R-Matrix Theory of Nuclear Reactions

A. M. LANE, *Atomic Energy Research Establishment, Harwell, Berkshire, England*

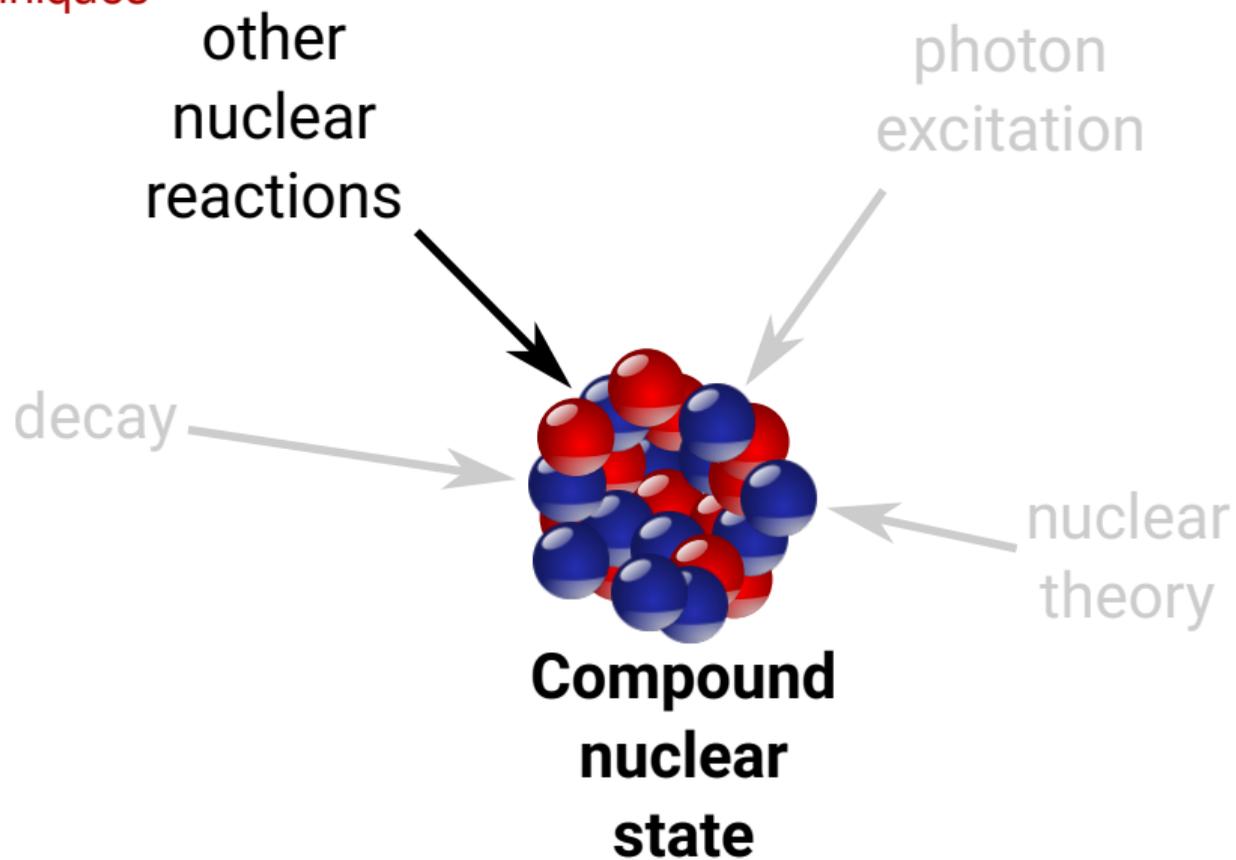
AND

R. G. THOMAS,* *Los Alamos Scientific Laboratory, Los Alamos, New Mexico*

Indirect techniques



Indirect techniques



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Determining proton partial widths

$$\sigma(E) = \omega \frac{\Gamma_p \Gamma_\gamma}{(E - E_r)^2 + \Gamma^2/4}$$

- Partial width calculated by

$$\Gamma_p = 2 \frac{\hbar^2}{\mu R^2} P_c C^2 S \theta_p^2$$

- Dimensionless Single-Particle Reduced Width

$$\theta_p^2 = \frac{R}{2} |u_p(R)|^2$$

- ▶ $u_p(R)$ is the radial wavefunction of a single particle at the channel radius

- R is the channel radius:
 $R = R_0(A_t^{1/3} + A_p^{1/3})$
- P_c is Penetration factor
- C^2 is isospin Clebsch-Gordon Coefficient
- S is the Spectroscopic Factor
 - ▶ Note: $C^2 S$ is colloquially the "Spectroscopic Factor"
 - ▶ How "single particley" the state is
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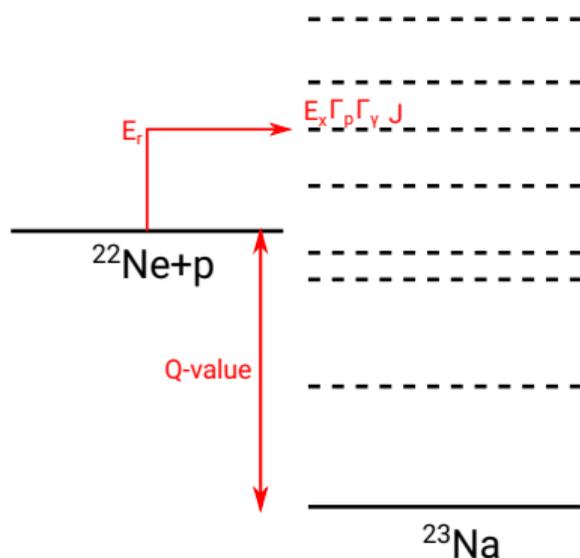
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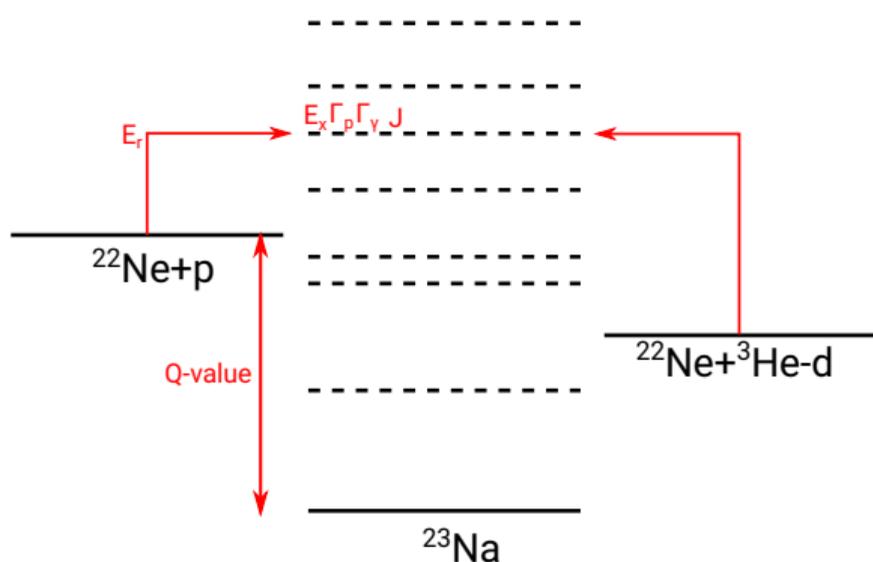


- ^3He is a deuteron+proton
- Transfer proton from ^3He to ^{22}Ne - **proton stripping**
- Extra degree of freedom in deuteron
 - ▶ Allows higher beam energy
 - ▶ Higher cross section
- Can measure
 - ▶ Energy of deuteron $\rightarrow E_r$
 - ▶ Angular distribution of deuteron $\rightarrow J$
 - ▶ Cross section $\rightarrow \Gamma_p$
- Requires some theory...

See [Hammache and de Séréville, Front. in Phys. 8 \(2021\) 602920](#)

Determining proton partial widths

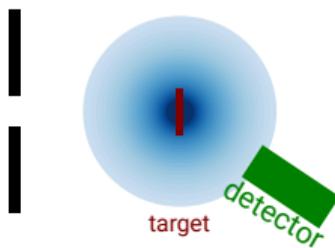
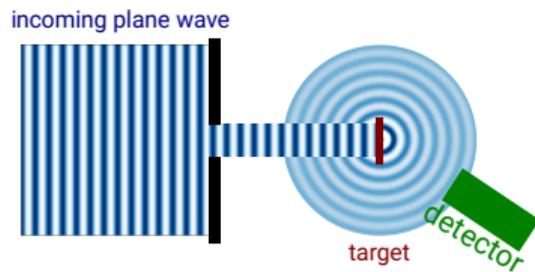
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Elastic scattering



Case for $\ell = 0$

- Total wave function far from the target

$$\Psi(\vec{r}) = N \left[e^{i\vec{k}\cdot\vec{r}} + f(\theta) \frac{e^{ikr}}{r} \right]$$

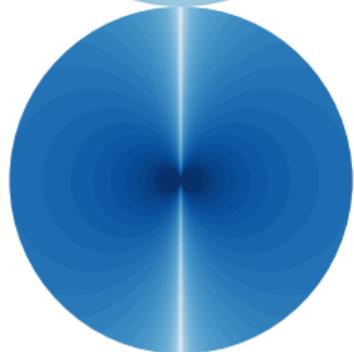
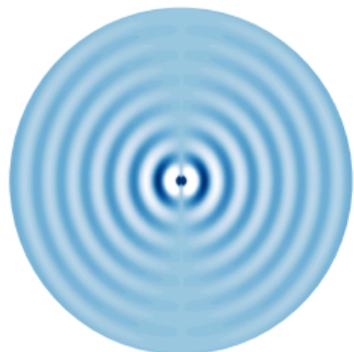
- To combine the coordinate systems, we expand the incoming wave in terms of partial waves:

$$e^{ikz} = \sum_{\ell=0}^{\infty} (2\ell + 1) i^{\ell} j_{\ell}(kr) P_{\ell}(\cos \theta)$$

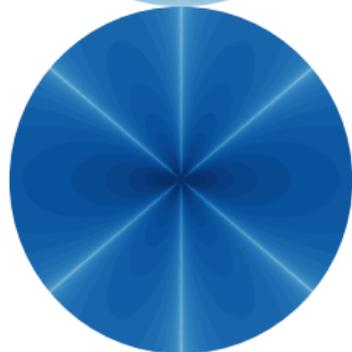
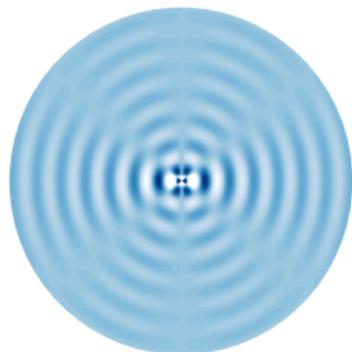
- The scattering amplitude becomes:

$$f(\theta) = \frac{1}{k} \sum_{\ell=0}^{\infty} (2\ell + 1) e^{i\delta_{\ell}} \sin \delta_{\ell} P_{\ell}(\cos \theta)$$

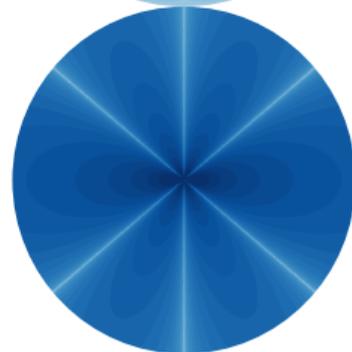
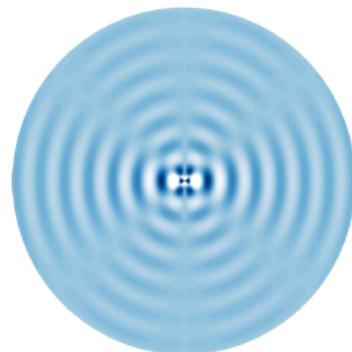
Elastic scattering



Case for $\ell=1$

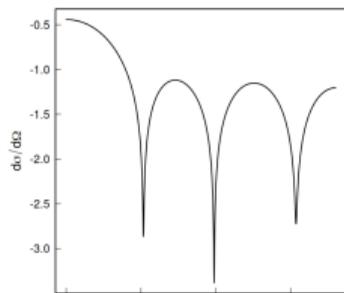
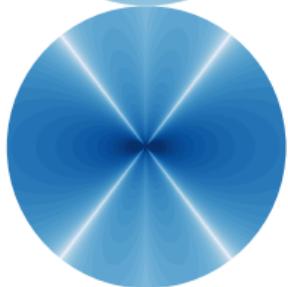
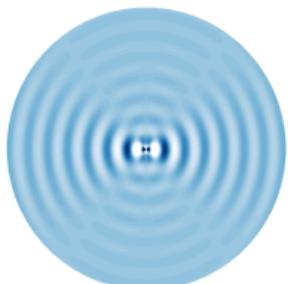


Case for $\ell=2$



Case for $\ell=3$

Elastic scattering



- The scattering amplitude is:

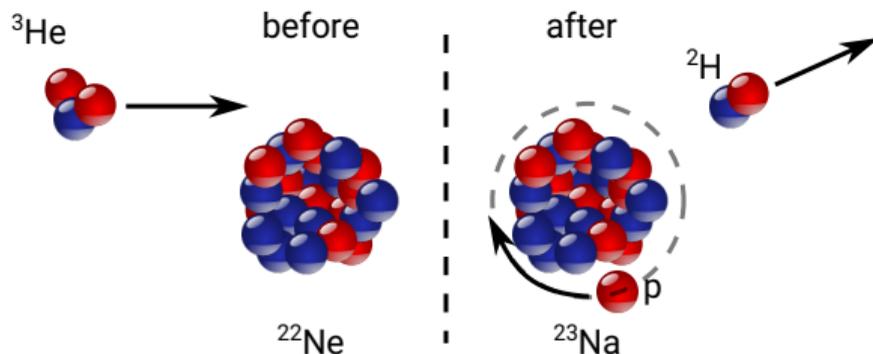
$$f(\theta) = \frac{1}{k} \sum_{\ell=0}^{\infty} (2\ell + 1) e^{i\delta_\ell} \sin \delta_\ell P_\ell(\cos \theta)$$

- Cross section measured by detector:

$$\frac{d\sigma}{d\Omega} = f^*(\theta) f(\theta)$$

- Traditionally, use cross section to find δ_ℓ , which derive from the shape of the nuclear potential

Transfer reactions

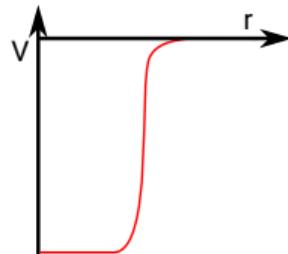
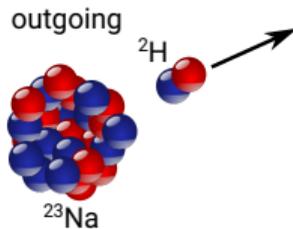
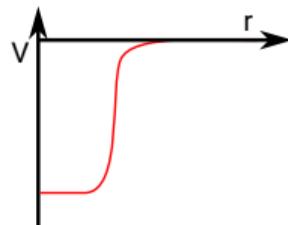
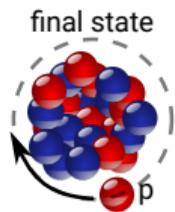
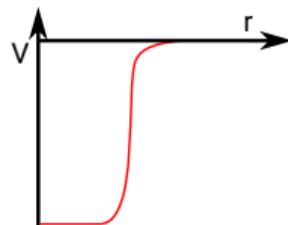
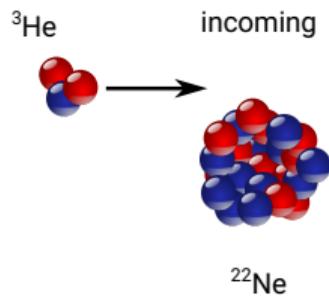


- Elastic scattering on previous slides is dominant
- Small perturbation causes direct transfer from initial state to final state
- Cross section:

$$d\sigma/d\Omega \propto |\langle \Psi_f^* | V | \Psi_i \rangle|^2$$

- Use partial wave expansion again, but now there are often only a few contributing terms $\rightarrow d\sigma/d\Omega$ tells us ℓ !
- Final state is described by core (${}^{22}\text{Ne}$) plus transferred nucleons
 - ▶ Projectile in optical potential of target
 - ▶ Perturbing nuclear potential (including transfer of nucleons)
 - ▶ Outgoing particle in potential of residual

Transfer reactions



Transfer reactions

$$\frac{d\sigma}{d\Omega_{exp}} = C^2 S_{proj} C^2 S_{targ} \frac{d\sigma}{d\Omega_{th}}$$

$$\Gamma_p = 2 \frac{\hbar^2}{\mu R^2} P_c C^2 S \theta_p^2$$

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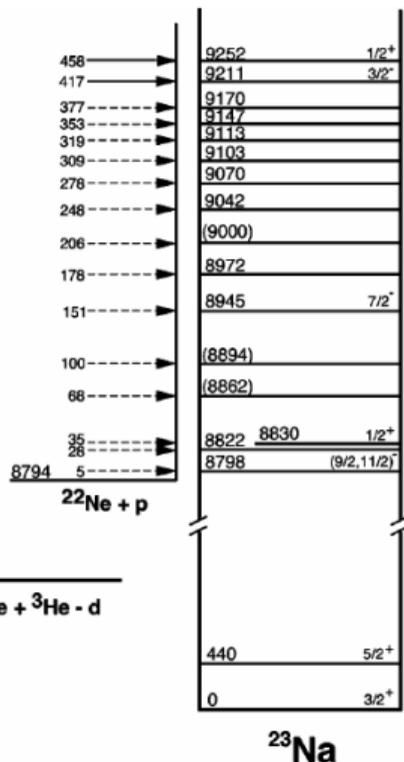
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- Experimental needs

- ▶ Accelerated beam of intermediate-energy light particles
- ▶ Target of interest
- ▶ Measure outgoing particles (elastic scattering and reaction products)
- ▶ Measure scattering at different angles
- ▶ Particle energy resolution compatible with level density (transfer to different final states)
 - ★ ~ 20 keV in this case of $^{22}\text{Ne}(p,\gamma)^{23}\text{Na}$

Transfer reactions - $^{22}\text{Ne}(p,\gamma)^{23}\text{Na}$ using $(^3\text{He},d)$

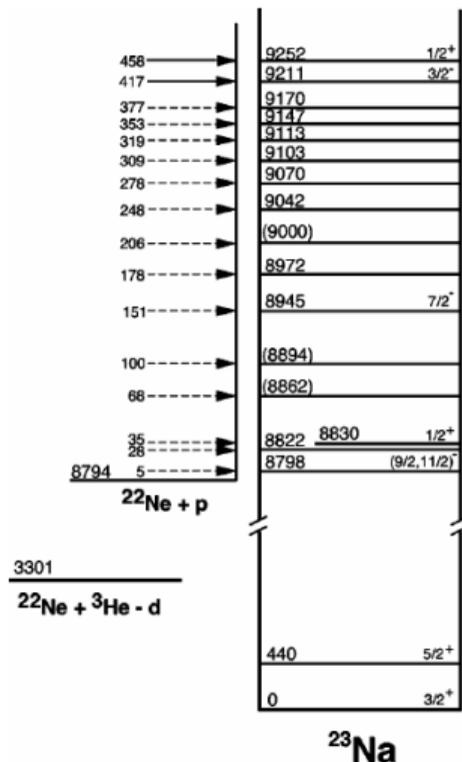
Hale et al., *Physical Review C* 65 (2001) 015801



- Implanted ^{22}Ne ions into $40 \mu\text{g}/\text{cm}^2$ carbon foils
 - ▶ Using conversions from yesterday, how thick is this?
- 20 MeV $^3\text{He}^{++}$ beam, 100 – 150 pA
- TUNL Enge split-pole spectrograph with 2 msr aperture
- Data collected from 5° to 35°

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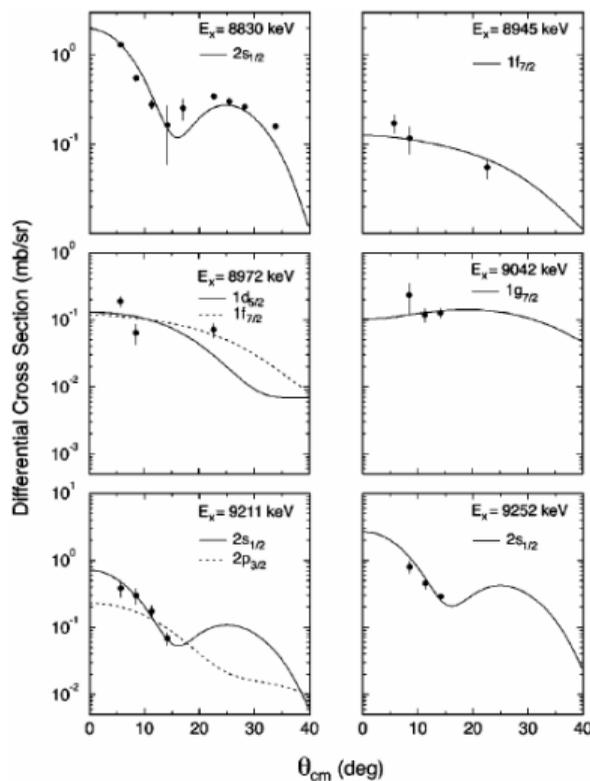


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- TUNL Enge split-pole spectrograph with 2 msr aperture
- Data collected from 5° to 35°
- Some questions:
 - ① How do we create a target?
 - ② How do we know how much neon is in there?
 - ③ What if the neon leaches out during our experiment?
 - ④ What yield $\rightarrow \sigma$ regime are we in?

Transfer reactions - $^{22}\text{Ne}(p,\gamma)^{23}\text{Na}$ using $(^3\text{He},d)$

Hale et al., Physical Review C 65 (2001) 015801

Hale et al., Physical Review C 70 (2004) 045802



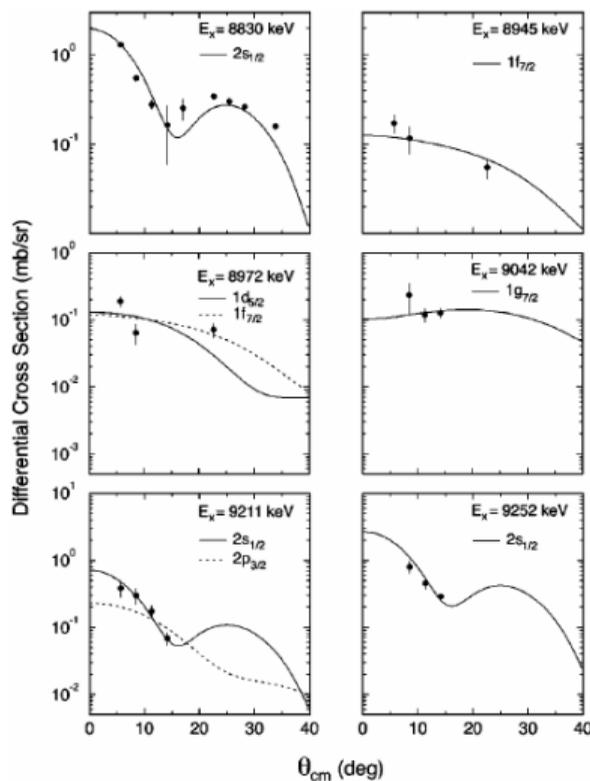
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- 35 keV resonance \equiv 8830 keV state in ^{23}Na
- 8830 keV: $\ell=0$, $C^2S = 0.039$

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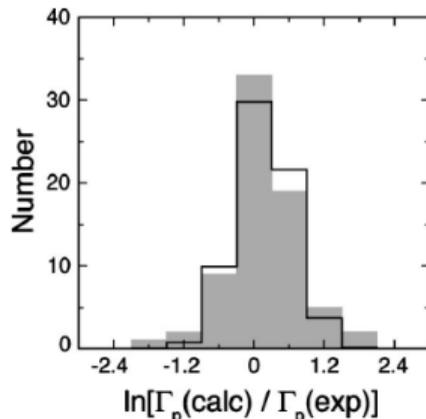
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- 8830 keV: $\ell=0$, $C^2S = 0.039$
- Uncertainties on these values? A factor of 1.6



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Resonance strength measurement

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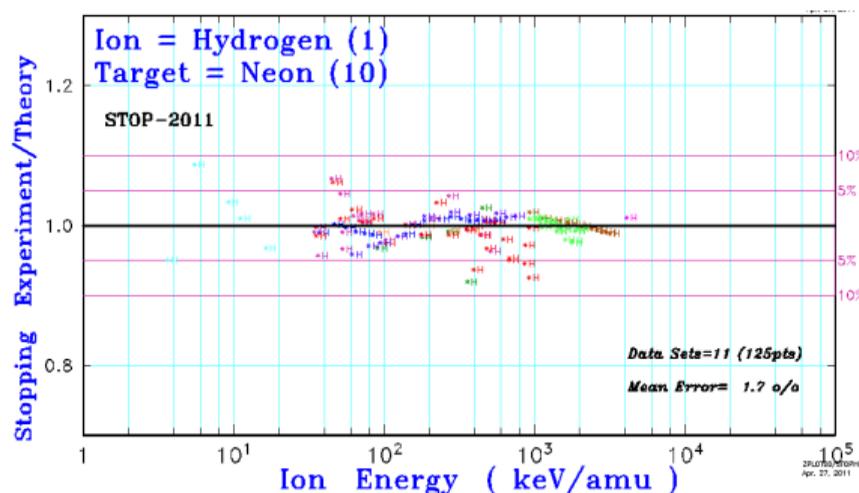
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- ϵ_r : depends on
 - ▶ stopping powers
 - ▶ assumptions about target composition
 - ▶ target stability
- Stopping powers
 - ▶ SRIM.org
 - ▶ Be careful to check where measurements are available

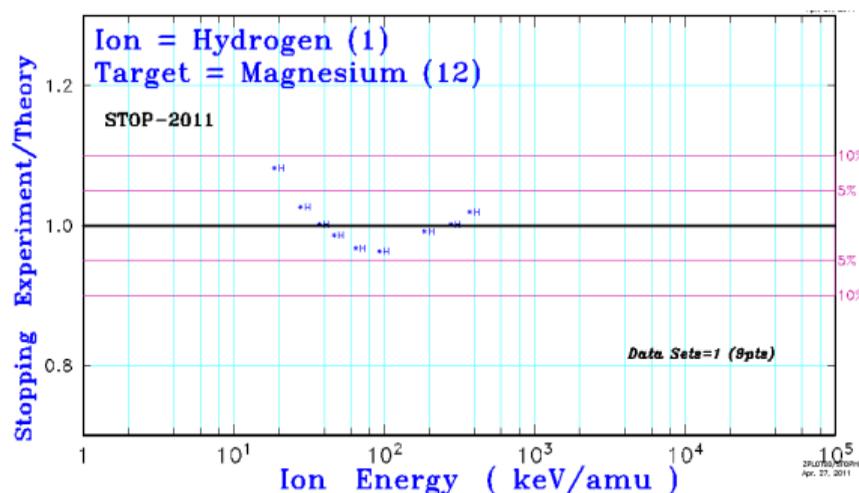


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 - ▶ Be careful to check where measurements are available
 - ▶ e.g. 1 MeV protons in magnesium
- e.g. what is the molecular model you're using?

WARNING - Target Layer Density

You have accepted a calculated density value for a compound.

These densities are not very accurate.

Would you like to **Continue** or **Re-enter the target density?**

Beam current

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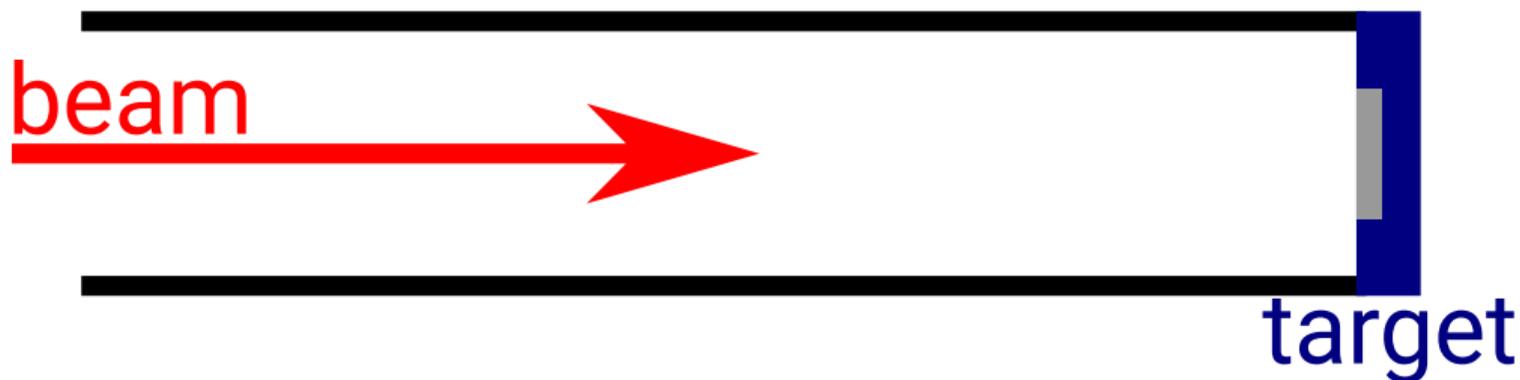
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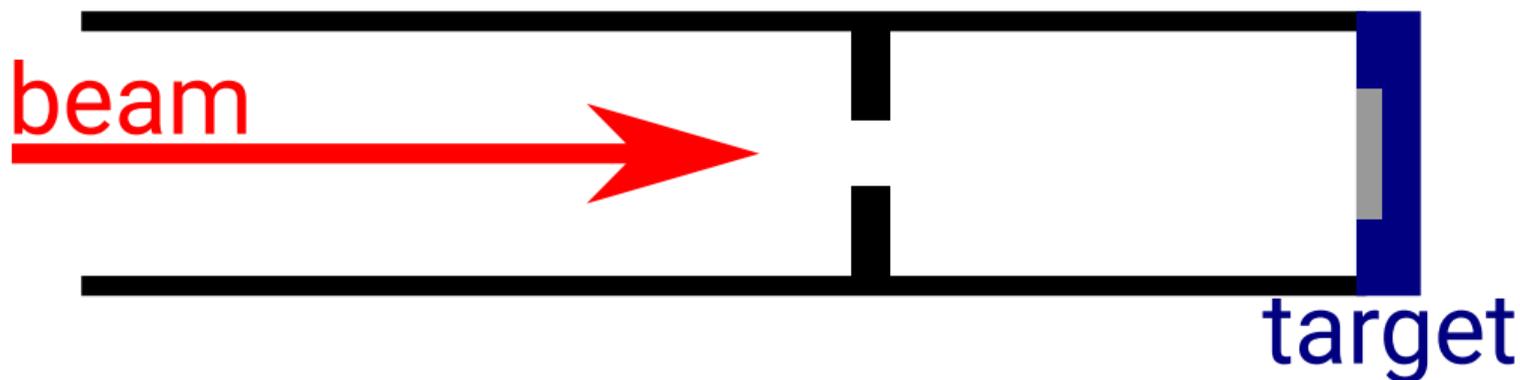


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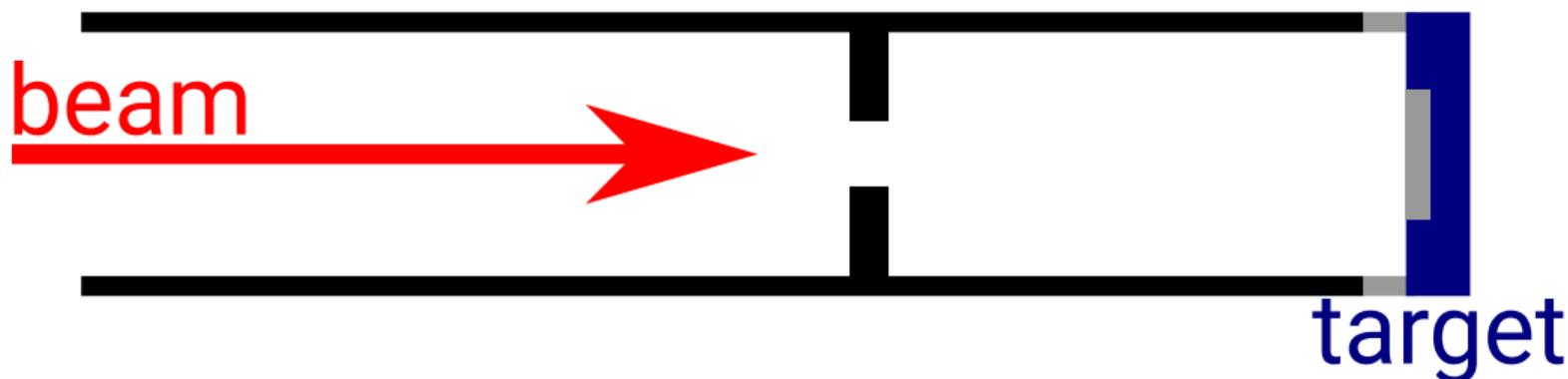


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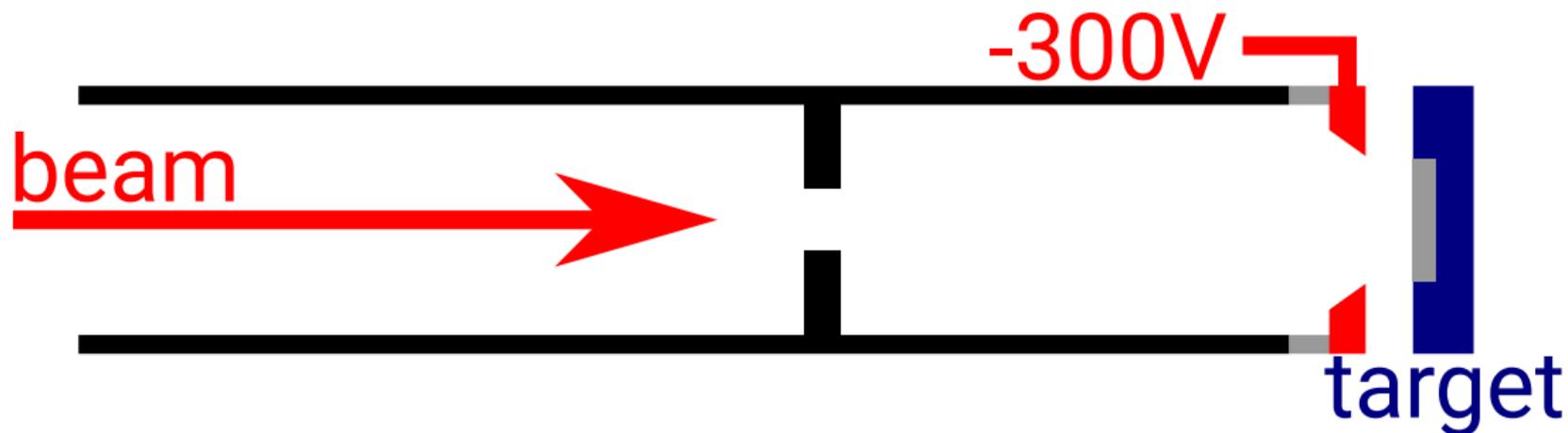


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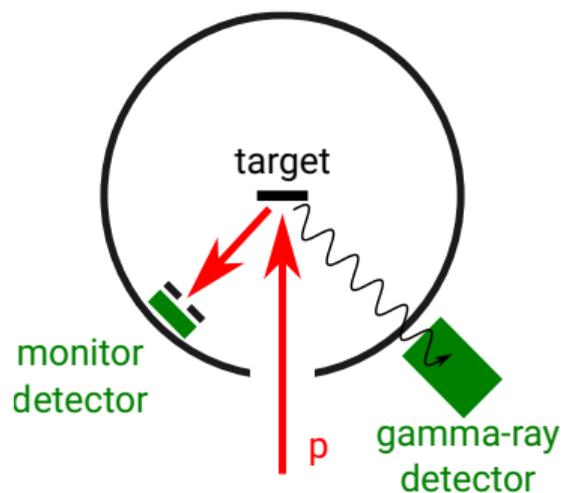
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- Beam current



Performing measurements relative to Rutherford scattering

- Low-energy: beam scatters according to Rutherford

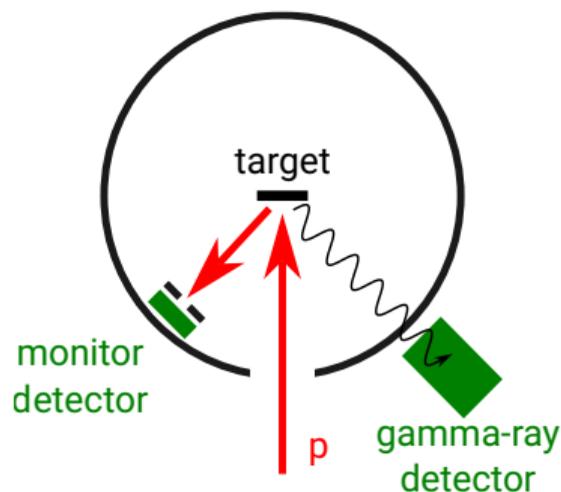


- Resonance strength from integrated yield

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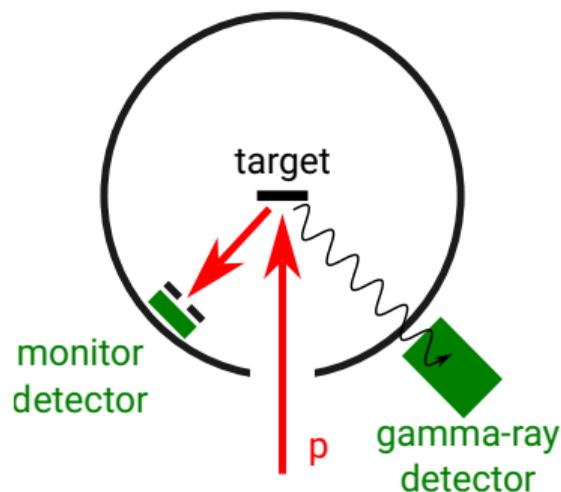
$$Y_{\text{Ruth}} = \frac{N_{p'}}{N_p \Omega_{\text{mon}}} = \int_{E_0 - \Delta E}^{E_0} \frac{\sigma(E)}{\epsilon(E)} dE \approx \sigma n_t$$

- Yield from reaction

$$A = \frac{1}{B_{\gamma} \eta_{\gamma} W_{\gamma}(\theta)} \int \frac{N_{\gamma}(E)}{N_p(E)} dE$$

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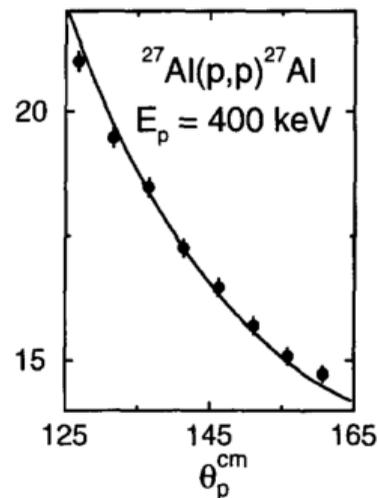
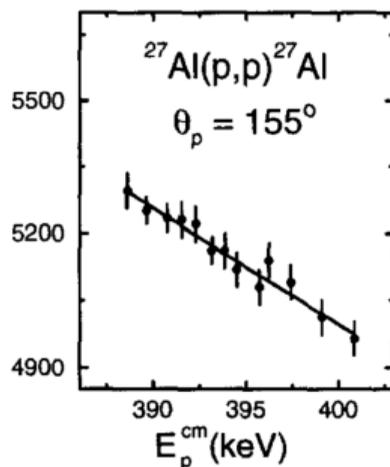
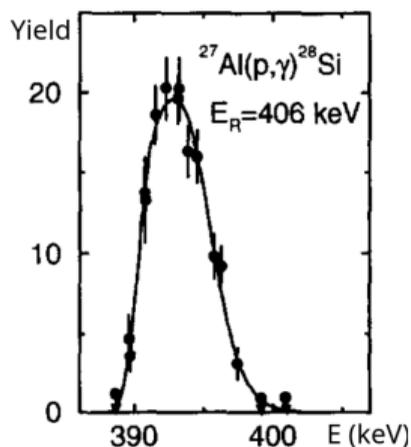
- Combining everything above

$$\omega_{\gamma} = \frac{2}{\lambda_r^2} \frac{1}{B_{\gamma} \eta_{\gamma} W_{\gamma}(\theta)} \Omega_{\text{mon}} \int \frac{N_{\gamma}(E)}{N_{p'}} \sigma_{\text{Ruth}} dE$$

Performing measurements relative to Rutherford scattering

$$\omega_{\gamma} = \frac{2}{\lambda_f^2} \frac{1}{B_{\gamma} \eta_{\gamma} W_{\gamma}(\theta)} \Omega_{\text{mon}} \int \frac{N_{\gamma}(E)}{N_{p'}} \sigma_{\text{Ruth}} dE$$

Powell et al., Nucl. Phys. A 644 (1998) 263



Absolute resonance strengths

Reaction	E_r^{lab}	$\omega\gamma$ (eV)	Uncertainty	Ref.
$^{23}\text{Na}(p,\gamma)^{24}\text{Mg}$	512	$8.75 (120) \times 10^{-2}$	14%	a
$^{23}\text{Na}(p,\alpha)^{20}\text{Ne}$	338	$7.16 (29) \times 10^{-2}$	4.1%	d
$^{30}\text{Si}(p,\gamma)^{31}\text{S}$	620	1.89 (10)	5.3%	a
$^{18}\text{O}(p,\gamma)^{19}\text{F}$	151	$9.77 (35) \times 10^{-4}$	3.6%	b
$^{27}\text{Al}(p,\gamma)^{28}\text{Si}$	406	$8.63 (52) \times 10^{-3}$	6.0%	c

a) Paine and Sargood Nucl. Phys. A 331 (1979) 389

b) Panteleo et al., Phys. Rev. C 104 (2021) 025802

c) Powell et al., Nucl. Phys. A 644 (1998) 263

d) Rowland et al., Phys. Rev. C 65 (2002) 064609

And many more

Target effects in transfer measurements

- How do we know how much neon is in there?
- From yesterday we know

$$\frac{dY}{d\Omega} = \frac{d\sigma}{d\Omega} \frac{\Delta E}{\epsilon_{\text{eff}}}$$

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- Elastic scattering

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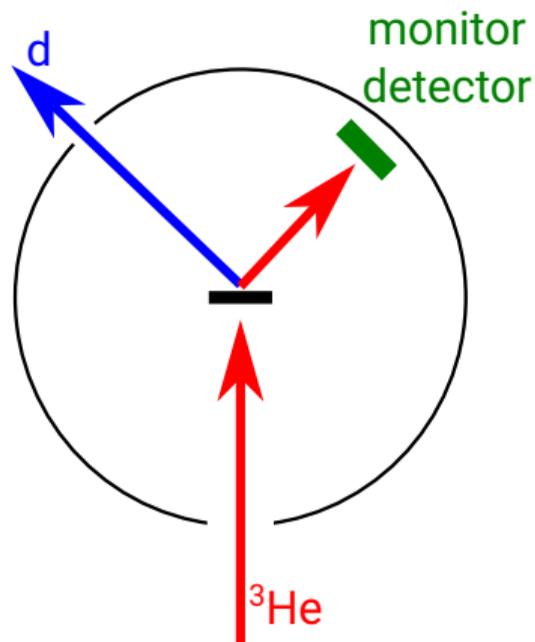
$$\frac{d\sigma}{d\Omega_e} = \frac{dY}{d\Omega_e} A$$

- We also know that elastic scattering approaches Rutherford scattering at 0°

$$\frac{d\sigma}{d\Omega_{\text{Ruth}}} = \left(\frac{Z_0 Z_1 e^2}{4E} \right)^2 \frac{1}{\sin^4(\theta/2)}$$

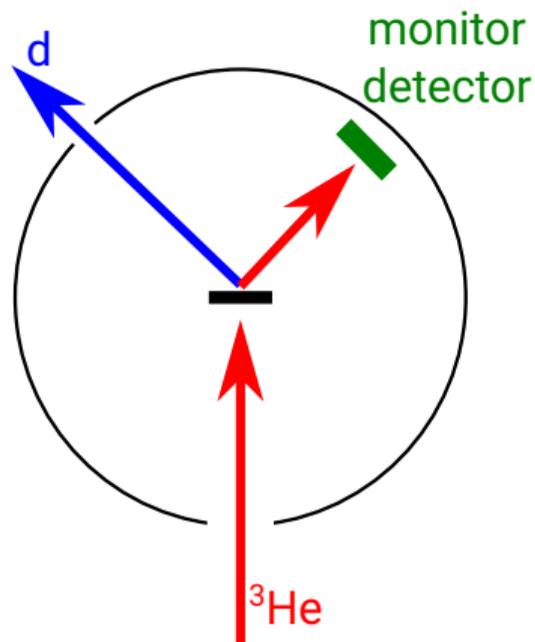
- Use elastic scattering and Rutherford scattering to find A

Targetry

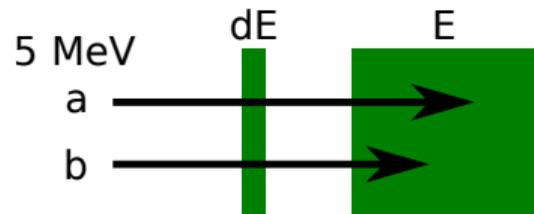


- What is neon leeches out during our experiment?
- Use a **monitor detector**
 - ▶ Fixed angle
 - ▶ Does not change throughout experiment
 - ▶ Measured elastically-scattered beam
 - ▶ Used to normalize A from previous slide

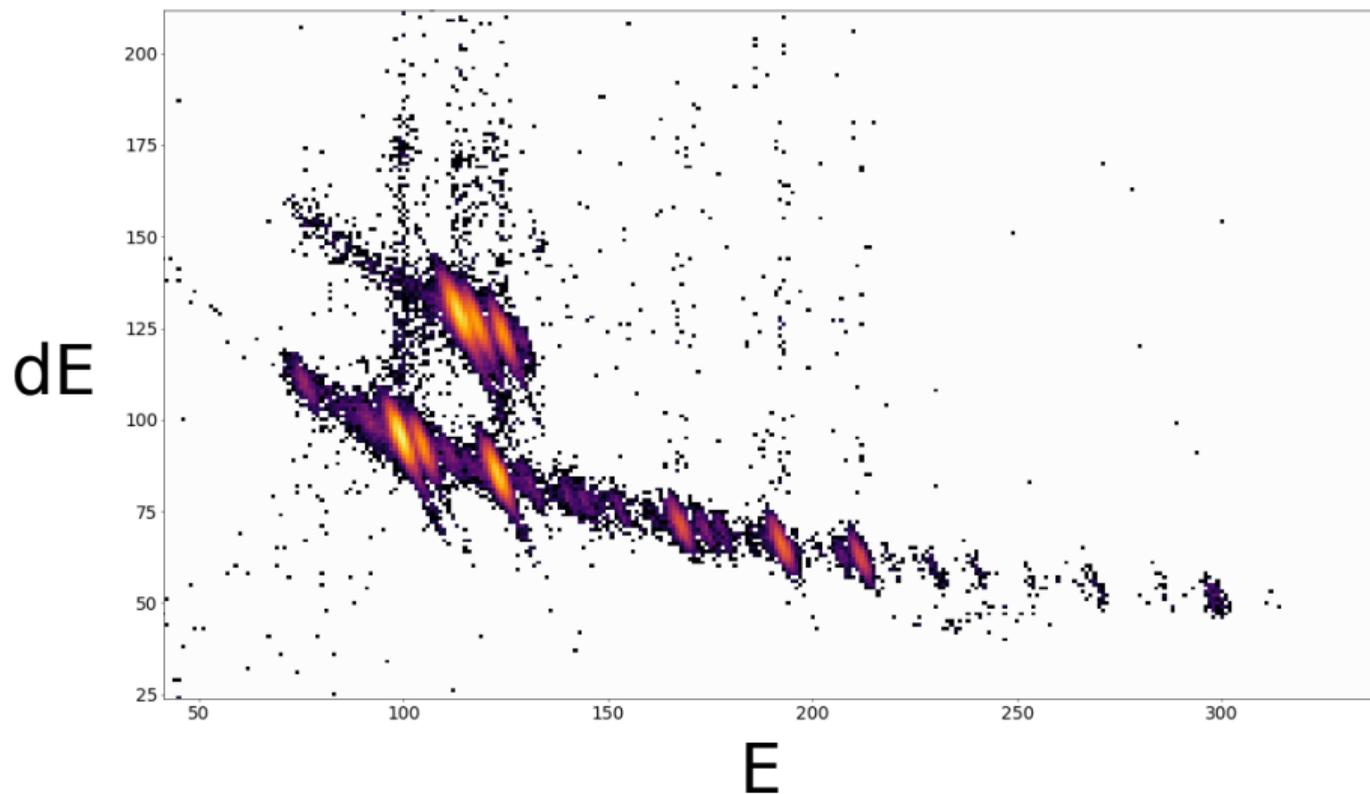
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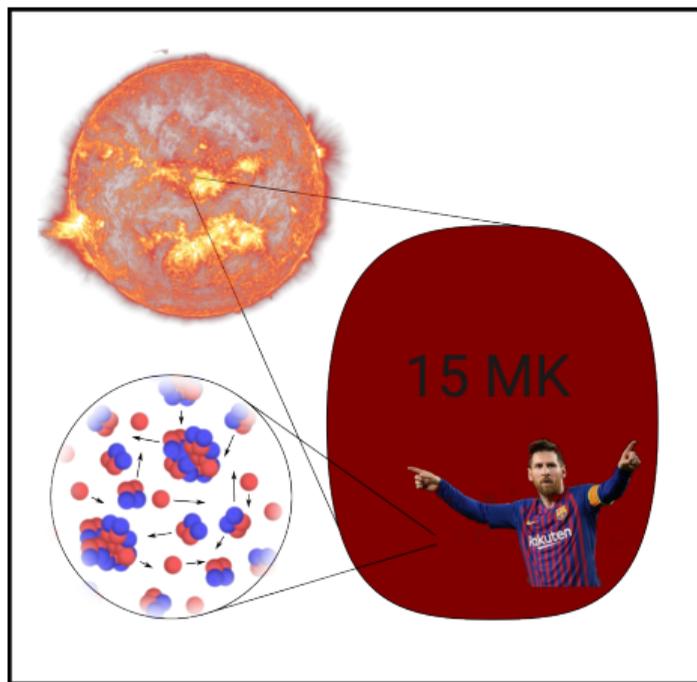


Silicon telescope spectrum



Astrophysical S Factors

Reaction rates and cross sections



- Particle velocities distributed according to a Maxwell-Boltzmann distribution

$$N_A \langle \sigma v \rangle_{01} = \left(\frac{8}{\pi \mu_{01}} \right) \frac{N_A}{(kT)^{3/2}} \times \int_0^{\infty} E \sigma(E) e^{-E/kT} dE$$

(cm³ mol⁻¹ s⁻¹)

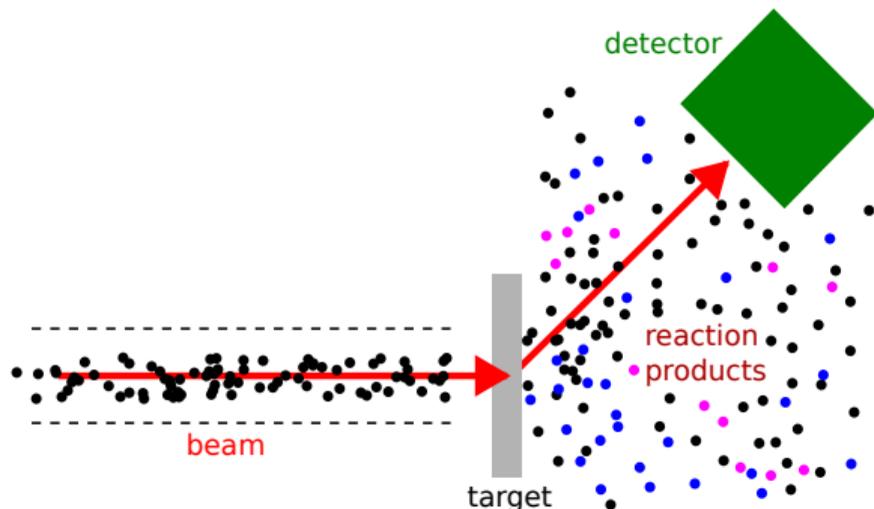
- For a known temperature, we only need to know $\sigma(E)$ to calculate reaction rate
- For the rest of my lectures, we will concern ourselves with *how*, exactly, to measure $\sigma(E)$

What, exactly, is $\sigma(E)$

Cross section

$$\sigma(E) \equiv \frac{\text{number of reactions per time}}{(\text{number of incident particles per area per time})(\text{number of target nuclei in the beam})}$$

- Number of reactions
 - ▶ We need a detector that can count outgoing radiation from our experiment (Faïrouz Hammache will cover details)
- Number of incident particles
 - ▶ Need a beam of particles (Faïrouz again!)
- Number of target nuclei
 - ▶ Need to create a target (yes, Faïrouz will cover this too!)



Astrophysical S factor

Please remember: S factor is a visual/convenience tool!

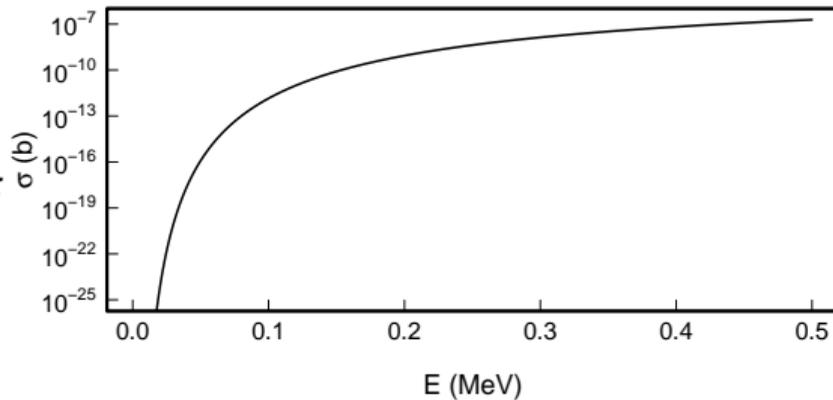
- Back to $^{16}\text{O}(p,\gamma)^{17}\text{F}$ reaction

$$\langle \sigma v \rangle = \sqrt{\frac{8}{\pi\mu}} \frac{1}{(kT)^{3/2}} \int_0^\infty \sigma(E) E e^{-E/kT} dE$$

- Remove $1/E$ and s-wave Coulomb barrier tunneling

$$\sigma(E) \equiv \frac{1}{E} e^{-2\pi\eta} S(E)$$

$$2\pi\eta = \frac{2\pi}{\hbar} \sqrt{\frac{\mu}{2E}} Z_0 Z_1 e^2$$



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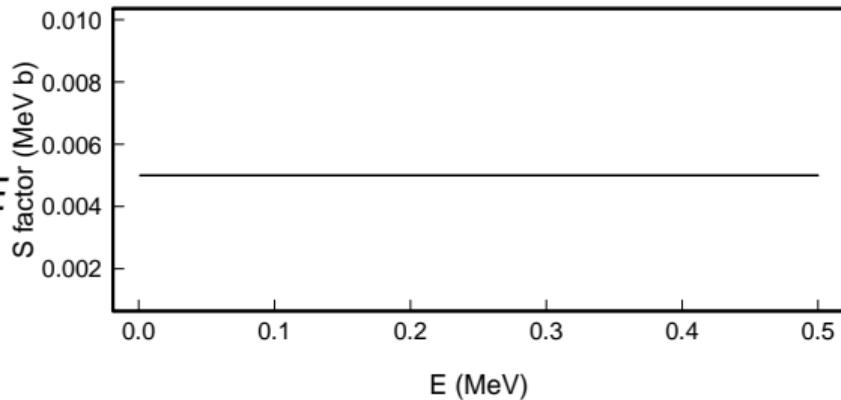
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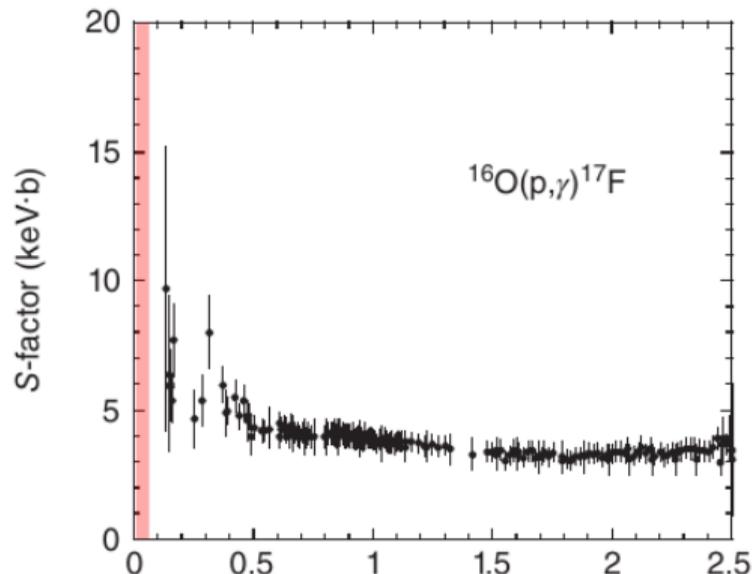
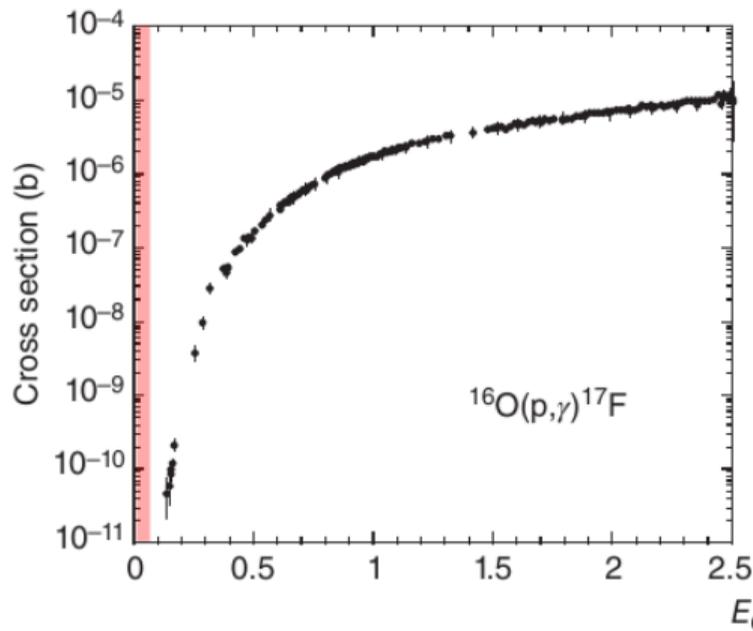
- S is **Astrophysical S Factor**

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Astrophysical S factor

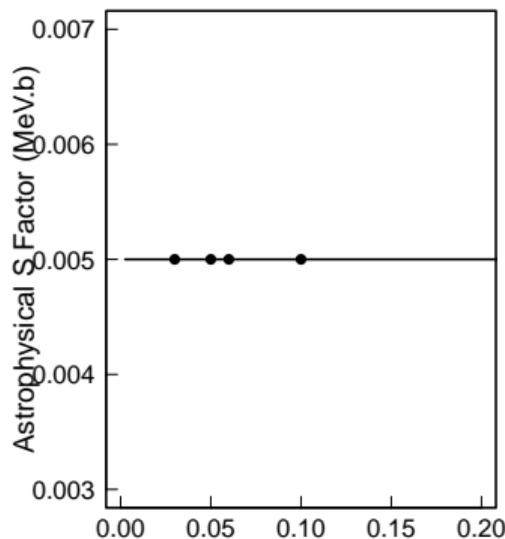
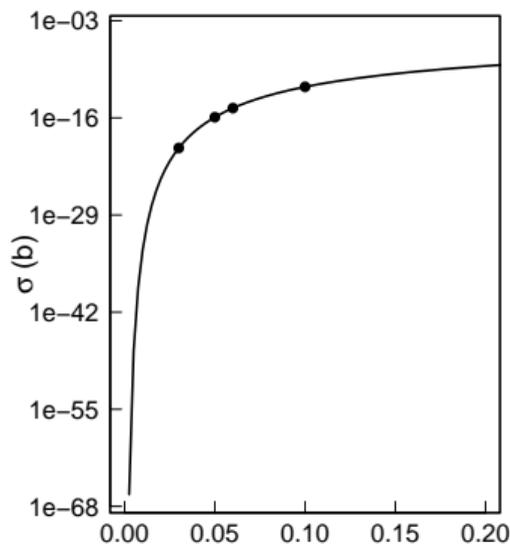
- Extrapolating and visualizing the cross section is much easier in terms of the astrophysical S factor.
- Recall that Gamow window is about 30 ± 15 keV



Astrophysical S Factor

- **Warning:** When calculating S factor from experimental data, you *must* use the correct effective energy

$$S(E) \equiv E e^{2\pi\eta} \sigma(E), \quad 2\pi\eta = \frac{2\pi}{\hbar} \sqrt{\frac{\mu}{2E}} Z_0 Z_1 e^2$$

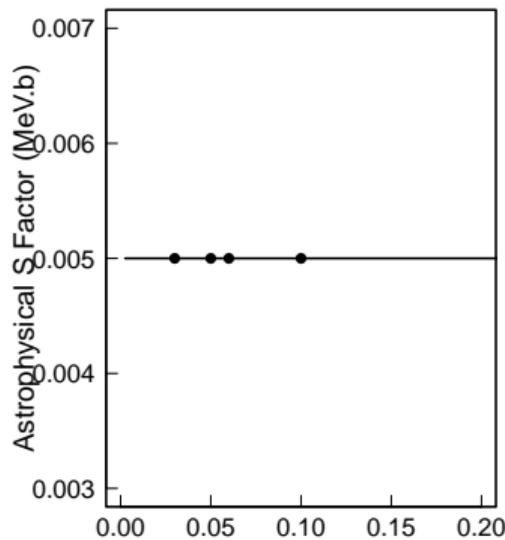
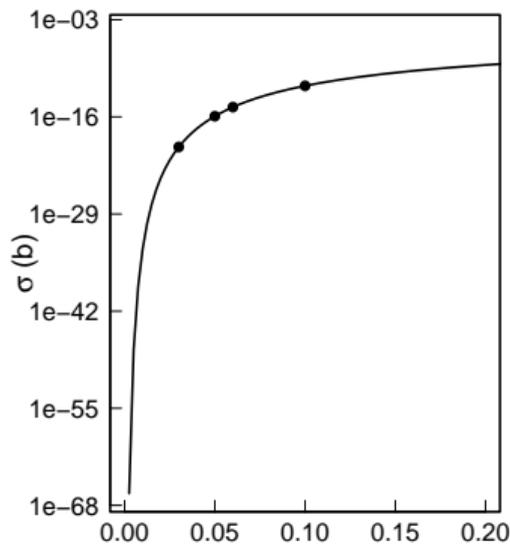


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